

DEPARTMENT OF MATHEMATICS



**5TH MEETING OF THE DEPARTMENT COUNCIL
TUESDAY, NOVEMBER 28, 2017**

**PROPOSED SCHEME OF STUDIES
B.SC, BS, M.SC, M.PHIL, PHD PROGRAMS**

Prepared By:

**Dr Shah Muhammad, Assistant Professor,
Department of Mathematics, MUST, Mirpur**

MIRPUR UNIVERSITY OF SCIENCE AND TECHNOLOGY (MUST)

ALLAMA IQBAL ROAD, MIRPUR-10250

MIRPUR, AZAD JAMMU & KASHMIR

Members of the Department Council

The following members attended the meeting:

Sr. #	Name	Designation	Signature
1	Dr. Rashida Hussain Chairperson, Department of Mathematics, MUST, Mirpur AJ&K	Convener/Member	
2	Prof. Dr. Rehana Asghar Dean, Faculty of Sciences, MUST, Mirpur, AJK	Observer	
3	Prof. Dr. Malik Zawwar Hussain, Department of Mathematics, University of Punjab, Lahore	Member	
4	Prof. Dr. Muhammad Mushtaq Dept. of Mathematics, UET Lahore	Member	
5	Dr. Muhammad Munir Associate Professor, Department of Mathematics, Post Graduate College, Abbottabad, KPK	Member	
6	Mr. Suleman Khan Assistant Prof. Dept. of Mathematics, MUST, Mirpur AJK	Member	
7	Dr. Shah Muhammad Assistant Prof. Dept. of Mathematics, MUST, Mirpur AJK	Member/Secretary	
8	Director AS & RB, MUST, Mirpur AJK	Observer	
9	The Registrar, MUST, Mirpur AJK	Observer	
10	The Controller of Examinations, MUST, Mirpur AJK	Observer	
11	Director QEC, MUST, Mirpur AJK	Observer	

Introduction

The department of mathematics at MUST, Mirpur, AJ&K, was established in 2009. The first intake of the M.Sc program was inducted in the Spring 2010. The M.Phil program was launched in the Spring 2011. In the Fall 2012, the department launched its BS program. The PhD program was started in the Spring 2015.

Mission Statement: The department of mathematics is committed to provide a supportive and conducive academic environment for learning through its various programs. The focus of these programs is to produce intellectual mathematicians equipped with critical thinking, problem solving skills, innovation, and high professional ethics who could bring positive changes in our society.

Faculty Buildup:

The faculty build up chart since the start of this program is given below.

Year	PhD	MS/MSc/BS	Total
Currently	8	16	24
2016-2017	6	16	22
2015-2016	6	17	23
2014-2015	6	10	16
2013-2014	3	9	12
2012-2013	3	12	15
2011-2012	2	11	13
2010-2011	2	9	11

Year-wise Enrollement Data:

The year-wise enrollement details for each program are given below.

Session/ Programs	Department of Mathematics												Total		
	BS			M.Sc			M.Phil.			Ph.D			Male	Female	Total
	Male	Female	Total	Male	Female	Total	Male	Female	Total	Male	Female	Total			
2017	12	31	43	19	31	50	6	11	17	1	--	1	38	71	109
2016	6	28	34	29	71	100	5	29	44	4	8	12	54	136	190
2015	11	27	38	22	25	47	5	26	31	1	2	3	39	80	119
2014	17	17	34	14	32	46	5	8	13	--	--	--	36	57	93
2013	14	13	27	8	38	46	5	9	14	--	--	--	27	60	87
2012	11	19	30	11	36	47	7	5	12	--	--	--	29	60	89
2011	--	--	--	21	26	47	8	7	15	--	--	--	29	33	62
2010	--	--	--	14	23	37	--	--	--	--	--	--	14	23	37

1. Scheme of Studies of BS Mathematics Program: General Breakup

Content		Description	Remarks
1.1	Awarding Institute/Body	Mirpur University of Science and Technology (MUST)	
1.2	Teaching Institute	Department of Mathematics, Mirpur University of Science and Technology (MUST), and affiliated colleges	
1.3	Final Award	Bachelor Studies in Mathematics	
1.4	Program Title	BS in Mathematics	
1.5	Starting Time for Program	Fall/Spring semester of each academic year	
1.6	Duration of the Program	8-12 Semesters	
1.7	Entrance Requirements	Intermediate or equivalent degree with mathematics (Min 45% marks)	
		No D-grade/3 rd Division in matric and intermediate	
		Entry Test conducted by the University with the following breakup: Mathematics: 30 %, English: 10%, two other subjects which the candidate have studied in intermediate with 30% weightage for each	
1.8	Merit Formula	Merit shall be determined on 20% of SSC, 50% of Intermediate and 30% of Entry Test marks.	
1.9	Total Credit Hours	Course Work: 127 Credit Hrs	
		Project (Compulsory): 6 Credit Hrs	
		Comprehensive Oral Examination: S/U	
		Conference/Seminar/Reading- I & II: S/U	

1.10 Program Educational Objectives:

The BS Mathematics program is aimed at imparting quality education of mathematics to the youth of Mirpur division and the surrounding districts, at an affordable cost. The program will give an opportunity to the talented youth to satiate their desire to learn and excel in mathematics. The program will meet the demand of skilled mathematicians in the local job market.

The objectives of the BS program also include: to teach students basic concepts of mathematics, to empower them with analytical and computational skills, to develop critical thinking, and to develop professional approach and work ethics. Moreover, the program is designed in such a way that the students can learn advanced mathematical concepts through the course work and the semester projects.

1.11 Program Learning Outcomes (PLOs):

The curriculum of the BS program is very diverse. During the first 4 semesters, beside some of the fundamental mathematics courses, the students also take many general and compulsory courses like

Physics, Mathematical Statistics, English, HR management, etc. These courses are so designed that students get useful knowledge and skills which will help them towards completion of their degrees.

1.12 Scope of the Program:

The mathematical experts are in demand across all kind of industries, the world over. Our graduates will be able to seek career opportunities in:

- a). Teaching at school, college, or higher level
- b). R&D and strategic organizations like PAEC, NESCOM, SUPARCO, etc.
- c). Banking sector, trading, and stock exchange businesses
- d). Higher studies in national and international universities and institutes
- e). Armed forces, civil services, oil and gas sector,

1.13 Program Structure and Features, Curriculum Units, Credit and Award Requirements

Sr. No.	Category	No. of Courses	Credit Hrs	Remarks
01	Compulsory Requirements	07	18	
02	General Courses	06	18	
03	Foundation Courses	16	48	
04	Major Courses	10	28	
05	Electives Courses	05	15	
06	Conference/Seminar/Reading I & II	02	S/U	
07	Project/Report	01	06	
08	Comprehensive Oral Examination	01	S/U	
Total		48	133	

1.14 Layout/Framework

Category	Course Title	Credit Hrs	Remarks
Compulsory	English-I	03	
	English-II	03	
	English-III	03	
	Introduction to Computers and Its Applications	03	
	Islamic Studies/Ethics	02	
	Arabic	02	
	Pakistan Studies	02	
General Courses	Physics-I	03	
	Physics-II	03	
	Mathematical Statistics I	03	
	Mathematical Statistics II	03	
	Introduction to Sociology/HR Management	03	
	Educational Psychology/Organizational Behavior/ Business Mathematics/ Entrepreneurship	03	

Foundation Courses	Calculus-I	04	
	Calculus-II	04	
	Calculus-III	04	
	Foundation of Mathematics	03	
	Linear Algebra-I	03	
	Linear Algebra-II	02	
	Differential Equations I	02	
	Mechanics I	03	
	Mechanics II	03	
	Differential Equations II	03	
	Abstract Algebra	03	
	Real Analysis-I	03	
	Complex Analysis	03	
	Metric Spaces	02	
	Topology	03	
	Scientific Programming	2+1	
Major Courses	Tensor Analysis	02	
	Differential Geometry-I	03	
	Real Analysis-II	03	
	Partial Differential Equations	03	
	Number Theory	02	
	Analytical Mechanics	03	
	Numerical Methods I	03	
	Mathematical Physics	03	
	Functional Analysis	03	
	Integral Equations	03	
	Project/Report	06	
	Comprehensive Oral Examination	S/U	
	Conference/Seminar/Reading- I and II	S/U	
Elective Courses	Elective-I	03	
	Elective-II	03	
	Elective-III	03	
	Elective-IV	03	
	Elective-V	03	

1.15 Semester-Wise Breakdown

Course Code	Course Title	Lec. Hrs.	Lab. Hrs.	Credit Hrs.
1st Year				
Semester-I				
ISL-1101	Islamic Studies	2	0	2
ENG-1102	English-I	3	0	3
COM-1103	Introduction to Computer and Its Applications	2	1	3
PHY-1104	Physics-I	3	0	3
MAT-1105	Calculus-I	4	0	4
MAT-1106	Foundation of Mathematics	3	0	3
Semester-II				
HUM-1201	Arabic	2	0	2
ENG-1202	English-II	3	0	3
HUM-1203	Pakistan Studies	2	0	2
PHY-1204	Physics-II	3	0	3
MAT-1205	Calculus-II	4	0	4
MAT-1206	Linear Algebra-I	3	0	3
2nd Year				
Semester-III				
ENG-2302	English-III	3	0	3
MAT-2303	Mathematical Statistics I	3	0	3
MAT-2304	Mechanics-I	3	0	3
MAT-2305	Calculus-III	4	0	4
MAT-2306	Linear Algebra-II	2	0	2
One Optional				
HUM-2301	Introduction to Sociology	3	0	3
HUM-2308	HR Management	3	0	3
Semester-IV				
MAT-2402	Differential Equations I	2	0	2
MAT-2403	Mathematical Statistics II	3	0	3
MAT-2404	Mechanics-II	3	0	3
MAT-2405	Metric Spaces	2	0	2
MAT-2406	Number Theory	2	0	2

One Optional

PSY-2401	Educational Psychology	3	0	3
HUM-2408	Organizational Behavior	3	0	3
MAT-2409	Business Mathematics	3	0	3
HUM-2410	Entrepreneurship	3	0	3

3rd Year**Semester-V**

MAT-3501	Real Analysis-I	3	0	3
MAT-3502	Differential Equations II	3	0	3
MAT-3503	Differential Geometry-I	3	0	3
MAT-3504	Analytical Mechanics	3	0	3
MAT-3505	Topology	3	0	3
MAT-3506	Abstract Algebra	3	0	3

Semester-VI

MAT-3601	Real Analysis-II	3	0	3
MAT-3602	Partial Differential Equations	3	0	3
MAT-3603	Numerical Methods-I	3	0	3
MAT-3604	Complex Analysis	3	0	3
MAT-3605	Tensor Analysis	2	0	2
MAT-3606	Scientific Programming	2	1	3

4th Year**Semester-VII**

MAT-4702	Mathematical Physics	3	0	3
MAT-4704	Functional Analysis	3	0	3
MAT-4715	Conference/Seminar/Reading-I		S/U	
MAT-4716	Project/Report	0	0	3+3

Two Optional Courses

MAT-4701	Measure Theory	3	0	3
MAT-4703	Numerical Methods II	3	0	3
MAT-4705	Fluid Mechanics I	3	0	3
MAT-4706	Operation Research	3	0	3
MAT-4707	Discrete Structures	3	0	3

MAT-4708	-----	3	0	3
MAT-4709	Quantum Mechanics-I	3	0	3
MAT-4710	Ring Theory	3	0	3
MAT-4711	Analytical Dynamics	3	0	3
MAT-4712	Introduction to Difference Equations	3	0	3
MAT-4713	Differential Geometry-II	3	0	3
MAT-4714	Electromagnetic Theory-I	3	0	3

Semester-VIII

MAT-4803	Integral Equations	3	0	3
MAT-4815	Conference/Seminar/Reading-II		S/U	
MAT-4816	Comprehensive Oral Examination		S/U	

Three Optional Courses

MAT-4801	Mathematical Systems Theory	3	0	3
MAT-4802	Mathematical Modeling	3	0	3
MAT-4804	Optimization Theory	3	0	3
MAT-4805	Fluid Mechanics II	3	0	3
MAT-4806	Algebraic Topology	3	0	3
MAT-4807	Special Functions	3	0	3
MAT-4808	Financial Mathematics	3	0	3
MAT-4809	Quantum Mechanics-II	3	0	3
MAT-4810	Introduction to Combinatorics	3	0	3
MAT-4811	Dynamical Systems	3	0	3
MAT-4812	Theory of Elasticity	3	0	3
MAT-4813	Special Theory of Relativity	3	0	3
MAT-4814	Electromagnetic Theory-II	3	0	3

1.16 Detail of Courses

Semester-I

Course Code: MAT-1105

Title: Calculus-I

Credit Hrs: 04

Course Outline:

Review Topics: Equations and inequalities: Solving linear and quadratic equations, linear inequalities. Division of polynomials, synthetic division. Roots of a polynomial, rational roots; Viète Relations. Descartes rule of signs. Solutions of equations with absolute value sign. Solution of linear and non-linear inequalities with absolute value sign.

Functions and Graphs: Domain and range of a function. Examples: polynomial, rational, piecewise defined functions, absolute value, functions, and evaluation of such functions. Operations with functions: sum, product, quotient and composition. Graphs of functions: linear, quadratic, piecewise defined functions.

Lines and System of Equations: Equation of a straight line, slope and intercept of a line, parallel and perpendicular lines. Systems of linear equations, solution of system of linear equations. Nonlinear systems: at least one quadratic equation.

Limits and Continuity: Functions, limit of a function. Graphical approach. Properties of limits. Theorems of limits. Limits of polynomials, rational and transcendental functions. Limits at infinity, infinite limits, one-sided limits. Continuity.

Derivatives: Definition, techniques of differentiation. Derivatives of polynomials and rational, exponential, logarithmic and trigonometric functions. The chain rule. Implicit differentiation. Rates of change in natural and social sciences. Related rates. Linear approximations and differentials. Higher derivatives, Leibnitz's theorem.

Applications of derivatives: Roll's Theorem, Cauchy's MVT, Increasing and decreasing functions. Relative extrema and optimization. First derivative test for relative extrema. Convexity and point of inflection. The second derivative test for extrema. Curve sketching. Indeterminate forms and L'Hopitals rule. Inverse functions and their derivatives.

Integration: Antiderivatives and integrals. Riemann sums and the definite integral. Properties of definite integral. The fundamental theorem of calculus. The substitution rule.

Text and Reference Books

1. H. Anton, *Calculus, A New Horizon*, 6th Edition, John Wiley and Sons, New York, 1999
2. J. Stewart, *Calculus, 3rd Edition*, Brooks/Cole, 1995.
3. G. B. Thomas and A.R. Finney, *Calculus, 10th Edition*, Addison Wesley, USA, 2002.
4. Dr. B. H. Edwards, *Calculus: 10th Edition*, Brooks/Cole, 2013.
5. S.M Yousaf, Muhammad Amin, *Calculus: 7th Edition*, Ilmi Kitab Khana.

Course Code: MAT-1106

Title: Foundation of Mathematics

Credit Hrs: 03

Course Outline: Sets and its Subsets, Operations on Sets, Some Fundamental Results, Cartesian Products of Sets, Binary Relations, Equivalence Relations, Partially Ordered Relations, Functions and Their Graph, Countable and Uncountable Sets, Upper Bounds, Lower Bounds, Supremum and Infimum,

Complex Numbers, Algebra of Complex Numbers, Modulus and Argument, Polar Form of a Complex Number, De Moivre's Theorem, Roots, Complex-Valued Functions

Binary Operations, Groups, Subgroups, Cyclic Groups, Groups of Permutations, Cycles, Transpositions, Order of a Permutation, Rings

Text and Reference Books

1. G. B. Thomas and A.R. Finney, *Calculus*, 10th Edition, Addison Wesley, USA, 2002.
2. J. A. Fraleigh, *A first course in Abstract Algebra*, Addison Wesley publishing Company, 1982.
3. S. Lang, *Algebra*, Addison Wesley, 1975.
4. T. Q. Sibley, *The Foundations of Mathematics*, 1st Edition, Wiley, 2008.
5. D. Tall, *The Foundations of Mathematics*, 2nd Edition, Oxford University Press, 2015.

Semester-II

Course Code: MAT-1205

Title: Calculus-II

Credit Hrs: 04

Course Outline:

Techniques of integration: Integrals of elementary, hyperbolic, trigonometric, logarithmic and exponential functions. Integration by parts, substitution and partial fractions. Approximate integration. Improper integrals. Reduction Formulas, Gamma functions.

Applications of integrals: Area between curves, average value. Volumes. Arc length. Area of a surface of revolution. Applications to Economics, Physics, Engineering and Biology.

Infinite series: Sequences and series. Convergence and absolute convergence. Tests for convergence: divergence test, integral test, p-series test, comparison tests, alternating series test, ratio test, root test. Power series. Convergence of power series. Representation of functions as power series. Differentiation and integration of power series. Taylor and McLaurin series. Approximations by Taylor polynomials.

Conic section, parameterized curves and polar coordinates: Curves defined by parametric equations. Calculus with parametric curves: tangents, areas, arc length. Polar coordinates. Polar curves, tangents to polar curves. Area and arc length in polar coordinates.

Text and Reference Books

1. H. Anton, *Calculus: A New Horizon*, 6th Edition, John Wiley and Sons, New York, 1999
2. J. Stewart, *Calculus*, 3rd Edition, Brooks/Cole, 1995.
3. G. B. Thomas and A. R. Finney, *Calculus*, 10th Edition, Addison Wesley, Reading, Ma, USA, 2002
4. M. Ryan, *Calculus*, 2nd Edition, For Dummies, 2016.
5. M. D. Spivak, *Calculus*, 4th Edition, Publish or Perish, 2008.

Course Code: MAT-1206

Title: Linear Algebra-I

Credit Hrs: 03

Course Outline: System of Linear Equations, Row Reduction, Echelon and Reduced Forms, Vector Equations and the Matrix Equation, Solution of Linear Systems and Applications, **Matrix Operations**, Inversion and Characterizations of Invertible Matrices, Matrix Factorization, Application of Matrices and Linear Equations, Determinants and Their Properties, Cramer's Rule, Volume and Linear Transformations, Fields, Vector Spaces, Subspaces, Linear Dependence and Independence, Linear Span of a Subset of a Vector Space, Bases and Dimensions, Rank and Nullity

Text and Reference Books

1. D. C. Lay, *Linear Algebra and its Applications*, Dorling Kindersley Publishing, 2003.
2. S. J. Leon, *Linear Algebra with Applications*, 6th Edition, Prentice Hall, 2002.
3. G. E. Shilov, *Linear Algebra*, Dover Publication, Inc., New York, 1997.
4. D. G. Zill and M. R. Cullen, *Advanced Engineering Mathematics*, PWS, Publishing Company, Boston, 1996.
5. G. Strang, *Linear Algebra*, 5th Edition, Wellesley-Cambridge Press, 2016.

Semester-III

Course Code: MAT-2303

Title: Mathematical Statistics I

Credit Hrs: 03

Course Outline: The postulates of probability, Some elementary theorems, Addition and multiplication rules, Baye's rule and future Baye's theorem, Random variables and probability functions, Uniform, Bernoulli and Binomial distribution, Hypergeometric and geometric distribution, Negative binomial and Poisson distribution, Uniform and exponential distribution, Gamma and beta distributions, Normal distribution, Moments and moment generating functions
Moments of binomial, hypergeometric, Poisson, gamma, beta and normal distributions

Text and Reference Books

1. M. H. De-Groot and M. J. Schervish, *Probability and Statistics*, 3rd Edition, Addison Wesley, 2002.
2. A. Papoulis, *Probability, Random Variables, and Stochastic Processes*, 3rd Edition, Mc-Graw Hill, 1991.
3. T. Sincich, *Statistics by Examples*, Dellen Publishing Company, 1990.
4. A. S. Hirahi. *A Course in Mathematical Statistics*, 4th Edition, Ilmi Kitab Khana, Lahore, Pakistan, 2012.
5. S. M. Chaudhry and S. Kamal, *Introduction to Statistical Theory Part-II*, Ilmi Kitab Khana, Lahore, Pakistan, 2012.

Course Code: MAT-2304

Title: Mechanics-I

Credit Hrs: 03

Course Outline:

Forces: Fundamental concepts and principles, Newtonian Mechanics, Inertial-non-inertial frames, Resultant of several concurrent forces, The parallelogram law of forces, Resolution of a forces, triangle of forces, Lamy's theorem, polygon of forces, Conditions of equilibrium for a particle, External and internal forces, principle of transmissibility, Resultant of like and unlike parallel forces, Moment of forces about a point, Varignon's theorem, Moment of a couple, equivalent couples, composition of couples, Reduction of coplanar forces to a force or a couple

Friction: Dry friction and fluid friction, Laws of dry friction, coefficients of friction, angle of friction, Equilibrium of a particle on a rough inclined plane, Particle on a rough inclined plane acted on by an external force, Conditions for sliding or titling

Virtual Work: Principle of virtual work, Problems involving tensions and thrust.

Text and Reference Books:

1. A. Bedford and W. Fowler, *Dynamics Engineering Mechanics*, Addison-Wesley, Reading, USA.
2. T. L. Chow, *Classical Mechanics*, John Wiley and Sons, New York, 1995.
3. H. Goldstein, *Classical Mechanics*, 2nd Edition, Addison Wesley, Reading, Ma, USA, 1980.
4. J. B. Marion, *Classical Dynamics of Particles and Fields*, 2nd Edition, Academic Press, New York, 1970.
5. J. R. Taylor, *Classical Mechanics*, University Science Books, 2005.

Course Code: MAT-2305

Title: Calculus-III

Credit Hrs: 04

Course Outline:

Multivariable functions and partial derivatives: Functions of several variables. Limits and Continuity. Partial derivatives, Composition and chain rule. Directional derivatives and the gradient vector. Implicit function theorem for several variables. Maximum and minimum values. Optimization problems. Lagrange Multipliers.

Vectors and analytic geometry in space: Coordinate system. Rectangular, cylindrical and spherical coordinates. The dot product, the cross product. Equations of lines and planes. Quadric surfaces.

Vector-valued functions: Vector-valued functions and space curves. Derivatives and integrals of vector valued functions. Arc length. Curvature, normal and binormal vectors.

Multiple integrals: Double integrals over rectangular domains and iterated integrals. Non-rectangular domains. Double integrals in polar coordinates. Triple integrals in rectangular, cylindrical and spherical coordinates. Applications of double and triple integrals. Change of variables in multiple integrals.

Vector calculus: Vector fields. Line integrals. Green's theorem. Curl and divergence. Surface integrals over scalar and vector fields. Divergence theorem. Stokes' theorem.

Text and Reference Books

1. H. Anton, *Calculus: A New Horizon*, 6th Edition, John Wiley and Sons, New York, 1999.
2. J. Stewart, *Calculus*, 3rd Edition, Brooks/Cole, 1995.
3. G. B. Thomas and A.R. Finney, *Calculus*, 10th Edition, Addison Wesley, Reading, Ma, USA, 2002.
4. M. Ryan, *Calculus*, 2nd Edition, For Dummies, 2016.
5. Dr. R. Larson, *Calculus*, 9th Edition, Brooks/Cole, 2009.

Course Code: MAT-2306

Title: LinearAlgebra-II

Credit Hrs: 02

Course Outline: Linear Transformations and the Matrix of Linear Transformations, Eigenvectors and eigenvalues, Diagonalization, Complex Eigenvalues, Inner Product Spaces, Length and Orthogonality, Orthogonal Sets and Orthogonal Projections, Gram-Schmidt Process, Symmetric Matrices, Diagonalization of Symmetric Matrices, Quadratic Forms

Text and Reference Books

1. D. C. Lay, *Linear Algebra and its Applications*, Dorling Kindersley Publishing, Inc., 2003.
2. S. J. Axler, *Linear Algebra*, Done Right, Springer-Verlag, 1996.
3. W. K. Nicholson, *Elementary linear algebra with applications*, 2nd Edition, PWS Publishing Company, 1994.
4. D.G. Zill and M. R. Cullen, *Advanced Engineering Mathematics*, PWS, Publishing Company, Boston, 1996.
5. M. J. Sterling, *Algebra II*, 2nd Edition, For Dummies, 2014.

Semester-IV

Course Code: MAT-2402

Title: Differential Equations I

Credit Hrs: 02

Course Outline:

Preliminaries: Introduction (Formulation and classifications of differential equations), existence and uniqueness of solutions, introduction of initial value and boundary value problems

First order ordinary differential equations: Basic concepts, Separable variables, Exact Equations, Homogeneous Equations, Linear equations, integrating factors. Some nonlinear first order equations with known solution, differential equations of Bernoulli and Riccati type, Clairaut equation, modeling with first-order ODEs,

Second and higher order Linear differential equations: Initial value and boundary value problems, Homogeneous and non-homogeneous equations, Superposition principle, homogeneous equations with constant coefficients, Linear independence and Wronskian, Nonhomogeneous equations, undetermined coefficients method, variation of parameters, Cauchy-Euler equation, Modeling.

Text and Reference Books

1. W. E. Boyce and R. de Prima, *Elementary Differential Equations*, 9th Edition, Wiley, 2008.
2. E. Kreyszig, *Advanced Engineering Mathematics*, 10th Edition, Wiley, 2011.
3. D. G. Zill, *Differential Equations with Boundary-Value Problems*, 8th Edition, Brooks Cole, 2012.
4. S.J. Farlows, *An Introduction to Differential Equations and Their Applications*, Dover Publications, 2006.
5. M. E. Taylor, *An Introduction to Differential Equations*, 14th Edition, American Mathematical Society, 2011.

Course Code: MAT-2403

Title: Mathematical Statistics II

Credit Hrs: 03

Course Outline: Distribution function technique, Transformation technique: One variable, several variables, Moment-generating function technique, The distribution of the mean, The distribution of the mean: Finite populations, The Chi-Square distribution., The t distribution, The F distribution, Regression and Correlation, Linear regression, The methods of least squares, Normal regression analysis, Normal correlation analysis, Multiple linear regression, Multiple linear regression (matrix notation)

Text and Reference Books

1. M. H. De-Groot and M. J. Schervish, *Probability and Statistics*, 3rd Edition, Addison Wesley, 2002.
2. A. Papoulis, *Probability, Random Variables, and Stochastic Processes*, 3rd Edition, Mc-Graw Hill, 1991.
3. T. Sincich, *Statistics by Examples*, Dellen Publishing Company, 1990.
4. A. S. Hirahi. *A Course in Mathematical Statistics*, 4th Edition, Ilmi Kitab Khana, Lahore, Pakistan, 2012.
5. S. M. Chaudhry and S. Kamal., *Introduction to Statistical Theory Part-II*, Ilmi Kitab Khana, Lahore, Pakistan, 2012.

Course Code: MAT-2404

Title: Mechanics-II

Credit Hrs: 03

Course Outline:

Kinematics: Rectilinear motion of particles. Uniform rectilinear motion, uniformly accelerated rectilinear motion. Curvilinear motion of particle, rectangular components of velocity and acceleration. Tangential and normal components. Radial and transverse components. Projectile motion. **Kinetics:**

Work, power, kinetic energy, Conservation Laws (conservative force fields. Conservation of energy Conservation of linear and angular momentum), impulse, torque. Non-conservative forces. **Simple**

Harmonic Motion: The simple harmonic oscillator, period, frequency. Resonance and energy. The damped harmonic oscillator, over damped, critically damped and under damped. Motion, forces and vibrations. **Central Forces and Planetary Motion:** Central force fields, Properties of Central Force Field, Equations of motion, potential energy, orbits. Kepler's law of planetary motion. Apsides and apsidal angles for nearly circular orbits. Motion in an inverse square field.

Planer Motion of Rigid Bodies: Introduction to rigid and elastic bodies, degree of freedom, translations, rotations, instantaneous axis and center of rotation, Rotation of a rigid body about a fixed axis, moments and products of inertia. Parallel and perpendicular axis theorem.

Text and Reference Books

1. A. Bedford and W. Fowler, *Dynamics Engineering Mechanics*, Addison-Wesley, Reading, USA.
2. T. L. Chow, *Classical Mechanics*, John Wiley and Sons, New York, 1995.
3. H. Goldstein, *Classical Mechanics*, 2nd Edition, Addison Wesley, Reading, Ma, USA, 1980.
4. J. B. Marion, *Classical Dynamics of Particles and Fields*, 2nd Edition, Academic Press, New York, 1970.
5. J. R. Taylor, *Classical Mechanics*, Null Edition, University Science Books, 2005.

Course Code: MAT-2405

Title: Metric Spaces

Credit Hrs: 02

Course Outline: Preliminary Concepts, Definition and Examples of Metric Spaces, Open and Closed Spheres and Sets, Convergent Sequences, Cauchy Sequences, Cantor's Intersection Theorem, Complete Metric Spaces, Dense and Nowhere Dense Subsets, Continuous and Uniform Continuous Functions and Their Properties,

Text and Reference Books

1. C. W. Patty, *Foundation of Topology*, 2nd Edition, The Jones and Bartlett Publishers, 2009.
2. J. Dugundji, *Topology*, W.M. C. Brown Publisher, 1990.
3. E. Kreyszig, *Introductory Fundamental Analysis with Applications*, John Wiley and Sons, 1978.
4. M. O. Searcoid, *Metric Spaces*, 2007 Edition, Springer, 2006.
5. P. K. Jain, *Metric Spaces*, 2nd Edition, Alpha Science Intl Ltd, 2004.

Course Code: MAT-2406

Title: Number Theory

Credit Hrs: 02

Course Outline: Divisibility, Euclidean Algorithm, GCD and LCM of two Integers, Properties of Prime Numbers, Fundamental Theorem of Arithmetic (UFT), Congruence Relation, Residue System, Euler's Phi-Function, Solution of System of Linear Congruence, Congruences of Higher Degree, Chinese Remainder Theorem, Fermat's Little Theorem, Wilson's Theorem and Applications, Primitive Roots and Indices, Integers Belonging to a Given Exponent (mod p), Primitive Roots of Prime and Composite Moduli, Indices

Text and Reference Books

1. G. A. Jones and J. M. Jones, *Elementary Number Theory*, Springer-Varlog, London Limited, 1998.
2. M. B. Nathanson, *Methods in Number Theory*, Springer-Verlag, New York, 2000.
3. A.N. Parshin and I.R. Shafarevich, *Number Theory-I, Fundamental Problems, Ideas and Theories*, Springer-Verlag, Berlin Heidelberg, 1995.
4. K. H. E. Rosen, *Elementary Number theory and its Applications*, 4th Edition, Addison Wesley, Reading, Ma, USA, 2000.
5. T. Andreescu and D. Andrica, *Number theory*, 2009 Edition, Birkhauser, 2009.

Semester-V

Course Code: MAT-3501

Title: Real Analysis-I

Credit Hrs: 03

Course Outline: Supremum and Infimum, Completeness Properties of the Real Numbers, Limits and Continuity, Properties of Continuous Functions on Closed Bounded Intervals, Derivatives in One Variable, The Mean Value Theorem, Sequences and Series of Functions, Power Series, Pointwise and Uniform Convergence, Riemann Integrations

Text and Reference Books

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Real Analysis*, Mc-Graw Hill, 1995.
3. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3rd Edition, John Wiley and Sons, 1999.
4. R. L. Brabenec, *Introduction to Real Analysis*, PWS Publishing Company, 1994.
5. E. D. Gaughan, *Introduction to Analysis*, 5th Edition, Brooks/Cole, 1997.

Course Code: MAT-3502

Title: Differential Equations II

Credit Hrs: 03

Course Outline:

Review of first order linear and nonlinear odes and higher order linear odes and their solution techniques. **Basic theory** of systems of first order linear equations, Homogeneous linear system with constant coefficients, Non homogeneous linear system, **Series Solution and its Limitations**, The Frobenius Method, **Sturm-Liouville** (S-L) System and Boundary-Value Problems, Solution of the Bessel, The Hypergeometric, The Legendre and the Hermite Equations, Properties of the Bessel, the Legendre and the Hermite Functions

Text and Reference Books

1. E. A. Coddington and N. Levinson, *Theory of Ordinary Differential Equations*, Mc-Graw Hill, New York, Toronto and London, 1955.
2. W. E. Boyce and R. de Prima, *Elementary Differential Equations*, 9th Edition, Wiley, 2008.
3. P. Hartmen, *Ordinary Differential Equations*, John Wesley and Sons, New York, 1964.
4. D. G. Zill and M. R. Cullen, *Differential Equations with Boundary-Value Problems*, 3rd Edition, PWS Publishing Company, 1997.
5. V. I. Arnold and R. Cooke, *Ordinary Differential Equations*, 2006 Edition, Springer, 2006.

Course Code: MAT-3503

Title: Differential Geometry-I

Credit Hrs: 03

Course Outline: Historical Background, Motivation and Applications, Index Notation and Summation Convention, Space Curves, The Tangent Vector Field, Reparametrization; Arc Length, Curvature, Principal Normal, Binormal, Torsion, The Osculating, The Normal and the Rectifying Planes, The Frenet-Serret Theorem, Spherical Images, Sphere Curves, Spherical Contacts, Fundamental Theorem of Space Curves, Line Integrals and Green's Theorem, Local Surface Theory, Coordinate Transformations, The Tangent and the Normal Planes, Parametric Curves, The First Fundamental Form and the Metric Tensor, Normal and Geodesic Curvatures, Gauss's Formulae, Christoffel Symbols of First and Second Kinds, Parallel Vector Fields Along a Curve and Parallelism, The Second Fundamental Form and the Weingarten Map, Principal, Gaussian, Mean and Normal Curvatures, Dupin Indicatrices, Conjugate and Asymptotic Directions, Isometries and the Fundamental Theorem of Surfaces

Text and Reference Books

1. M. P. Do Carmo, *Differential Geometry of Curves and Surfaces*, Prentice Hall, 1976.
2. A. Goetz, *Introduction to Differential Geometry*, Addison Wesley, 1970.
3. R. S. Millman and G. D. Parker, *Elements of Differential Geometry*, Prentice Hall, 1977.
4. A. N. Pressley, *Elementary differential geometry*, 2nd Edition, Springer-Verlag, 2012.
5. D. J. Struik, *Lectures on Classical Differential Geometry*, Addison Wesley, Massachusetts, 1977.

Course Code: MAT-3504

Title: Analytical Mechanics

Credit Hrs: 03

Course Outline: Kinematics of Particles, Motion in Resisting Medium, Variable Mass Problem, Euler's Theorem and Chasles' theorem, **Moving Coordinate System:** Motion Relative to the Rotating Earth, **The Motion of a System of Particles:** Work, Power, Energy, center of mass, Generalized Coordinates, Lagrange's and Hamilton's Equations, Hamiltonian Principle, Simple Applications, Properties of a Rigid Body, Motion under No Forces, **Motion of Rigid Bodies in Three Dimensions:** General motion of rigid bodies in space. The momental ellipsoid and equimomental systems. Angular momentum vector and rotational kinetic energy. Principal axes and principal moments of inertia. Determination of 16 principal axes by diagonalizing the inertia matrix. **Euler Equations of Motion of a Rigid Body:** Force free motion. Free rotation of a rigid body with an axis of symmetry. Free rotation of a rigid body with three different principal moments. The Eulerian angles, angular velocity and kinetic energy in terms of Euler angles. Motion of a spinning top and gyroscopes-steady precession, sleeping top.

Text and Reference Books

1. G. R Fowles, G.L. Cassiday, *Analytical Mechanics*, 7th Edition, Thomson Brook Cole, 2005.
2. B. Jafferson, T. Beadsworth, *Further Mechanics*, Oxford University Press, 2001.
3. Louis N. Hand, *Analytical Mechanics*, 1st Edition, Cambridge University Press, 1998.
4. Dr. C. Helrich, *Analytical Mechanics*, 1st Edition, Springer, 2016.
5. J. S. Torook, *Analytical Mechanics*, 1st Edition, Wiley-Interscience, 1999.

Course Code: MAT-3505

Title: Topology

Credit Hrs: 03

Course Outline: Overview of Metric Spaces, Convergence, and Continuity in Metric Spaces, Topological Spaces, Sub-Spaces, Closed Sets, Closures and Interiors of Sets, Boundary of a Set, Limit Point, Bases and Sub-bases, Neighborhood Base, First and Second Countable Spaces, Continuous Functions and Homeomorphism, Product Topology

T_0 , T_1 , T_2 Spaces and Their Characterizations and Basic Properties, Regular and Completely Regular Spaces, Normal and Completely Normal Spaces, Compact / Countable Spaces and Their Properties, Connected Spaces

Text and Reference Books

1. C. W. Patty, *Foundation of Topology*, 2nd Edition, The Jones and Bartlett Publishers, 2009.
2. J. Dugundji, *Topology*, W.M. C. Brown Publisher, 1990.
3. J. R. Munkres, *Topology: A First Course in Topology*, 2nd Edition, Prentice Hall Inc. Englewood Cliffs, New Jersey, 2005.
4. G. F. Simmons, *Introduction to Topology and Modern Analysis*, Tata Mc-Graw Hill, 1963.
5. Munkres, *Topology*, 2nd Edition, Pearson India, 2015.

Course Code: MAT-3506

Title: Abstract Algebra

Credit Hrs: 03

Course Outline: Sets and Structures, Basic Axioms and Order of a Group, Subgroups, Subgroups Generated by Subset of a Group, System of Generators, Cyclic Group, Cosets, Lagrange's Theorem, Permutations, Even and Odd Permutations, Cycles, Lengths of Cycles, Transpositions, Symmetric and Alternating Group, Normalizers and Centralizers of a Subset of a Group, Centre of a Group, Normal Subgroup, Quotient Groups, Conjugacy Relation between Elements and Subgroups, Homomorphism and Isomorphism between Groups, Homomorphism and Isomorphism Theorems,

Text and Reference Books

1. J. B. Fraleigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. I. N. Herstein, *Topics in Algebra*, 2nd Edition, John-Wiley & Sons, 1975.
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. D. S. Dummit and R. M. Foote, *Abstract Algebra*, 3rd Edition, Wiley, 2003.
5. J. A. Gallian, *Contemporary abstract algebra*, D.C. Heath, 1986.

Semester-VI

Course Code: MAT-3601

Title: Real Analysis-II

Credit Hrs: 03

Course Outline:

The Riemann-Stieltjes Integrals: Definition and existence of integrals. Properties of integrals. Fundamental theorem of calculus and its applications. Change of variable theorem. Integration by parts. **Functions of Bounded Variation:** Definition and examples. Properties of functions of bounded variation. **Improper Integrals:** Types of improper integrals, tests for convergence of improper integrals. Beta and gamma functions. Absolute and conditional convergence of improper integrals. **Sequences and Series of Functions:** Power series, definition of point-wise and uniform convergence. Uniform convergence and continuity. Uniform convergence and differentiation. Examples of uniform convergence.

Text and Reference Books

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Mathematical Analysis*, Mc-Graw Hill, New York, 1987.
3. T. M. Apostol, *Mathematical Analysis*, 6th Edition, Addison Wesley, 1982.
4. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3rd Edition, John Wiley and Sons, 1999.
5. S. Lang, *Real Analysis*, Springer-Verlag, London, 1987.

Course Code: MAT-3602

Title: Partial Differential Equations

Credit Hrs: 03

Course Outline:

First order PDEs: Introduction, formation of PDEs, solutions of PDEs of first order, The Cauchy's problem for quasilinear first order PDEs, First order nonlinear equations, Special types of first order equations, **Second order PDEs:** Basic concepts and definitions, Mathematical problems, Linear operators, Superposition, Mathematical models: The classical equations, the vibrating string, the vibrating membrane, conduction of heat solids, canonical forms and variable, PDEs of second order in two independent variables with constant and variable coefficients, Cauchy's problem for second order PDEs in two independent variables

Methods of separation of variables and Green's Functions: Solutions of elliptic, parabolic and hyperbolic PDEs in Cartesian and cylindrical coordinates

Text and Reference Books

1. P. Duhaure and D. Zachmann, *Partial Differential Equations*, Mc-Graw Hill, 1986.
2. J. Fritz, *Partial Differential Equations*, Spriger-Verlag, New York, 1979.
3. R. Haberman, *Elementary Applied Partial Differential Equations*, Prentice Hall Inc., 1983.
4. M. Humi and W.B. Miller, *Boundary Value Problems and Partial Differential Equations*, PWS-Kent Publishing Company, Bostan, 1992.
5. E. Zauderer, *Partial Differential Equations of Applied Mathematics*, John Wiley and Sons, Englewood Cliff, New York, 1983.

Course Code: MAT-3603

Title: Numerical Methods-I

Credit Hrs: 03

Course Outline: Computer Arithmetic, Approximations and Errors; Methods for the Solution of Non-Linear Equations and Their Convergence: Bisection Method, Regula-Falsi, Fixed Point Iteration, Newton-Raphson, Secant and Householder's Method, Error Analysis for Iterative Methods Interpolation and Polynomial Approximation: Lagrange Interpolation, Newton's Divided Difference, Forward-Difference and Backward-Difference Formulae, Hermite Interpolation, Numerical Integration and Error Estimates: Rectangular Rule, Trapezoidal Rule, Simpson's One-Three and Three-Eight Rules. Numerical Solution of Systems of Algebraic Linear Equations: Gauss-Elimination Method, Gauss-Jordan Method, Matrix Inversion, LU-Factorization, Doolittle's, Crout's, Cholesky's Methods, Gauss-Seidel and Jacobi Methods, Matrix Norms, Method of Least Squares, Eigenvalues and Eigenvectors: Power Method

Text and Reference Books

1. K. E. Atkinson, *An Introduction to Numerical Analysis*, 2nd Edition, John Wiley and Sons, New York, 1989.
2. R.L. Burden and J.D. Faires, *Numerical Analysis*, 5th Edition, PWS Publishing Company, 1993.
3. S.C. Chapra and R.P. Canale, *Numerical Methods for Engineers*, Mc-Graw Hill, New York, 1988.
4. A. Greenbaum and T. P. Chartier, *Numerical Methods*, 2012 Edition, Princeton University Press, 2012.
5. J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.

Course Code: MAT-3604

Title: Complex Analysis

Credit Hrs: 03

Course Outline: The Algebra and the Geometry of Complex Numbers, Complex Functions, Parametric Curves in the Complex Plane, Linear Mappings, Special Power Functions, Reciprocal Functions, Limit and Continuity, Complex Functions as Vector Fields, Derivative, Analytic Functions, Cauchy-Riemann Equations, Complex Exponential, Logarithmic, Trigonometric, Hyperbolic Functions and Their Derivatives, Harmonic Functions, Contour Integrals, the Cauchy-Goursat Theorem, Cauchy Integral Formulas, the Morera Theorem, Maximum Modulus Principle, The Liouville Theorem, Fundamental Theorem of Algebra, Convergence of Sequences and Series, The Taylor and the Laurent Series, Uniqueness of Representation, Zeros of Analytic Functions Residues, Poles and the Residue Theorem, Evaluation of Improper Integrals, Integrals Around a Branch Point, The Argument Principle and the Rouché's Theorem

Text and Reference Books

1. R.V. Churchill and J.W. Brown, *Complex Variables and Applications*, 5th Edition, Mc-Graw Hill, New York, 1989.
2. E. Hille, *Analytic Function Theory*, Vol. I and II, Chelsea Publishing Company, New York, 1974.
3. J. E. Marsden, *Basic Complex Analysis*, W. H. Freeman and Company, 1982.
4. D. G. Zill, and P. D. Shanahan, *A First Course in Complex Analysis with Applications*, Jones and Bartlet Publishers, Sudbury, Massachusetts, 2008.
5. L. V. Ahlfors, *Complex Analysis*, 3rd Edition, McGraw Hill Education (India) Private Limited, 2013.

Course Code: MAT-3605

Title: Tensor Analysis

Credit Hrs: 02

Course Outline: Introduction to general tensors, Summation Convention, Kronecker Delta, Levi-Civita Symbol, Vectors as Quantities Transforming Under Rotations with Notation, The Spherical-Polar and the Cylindrical-Coordinate Meshes, Alternating Symbol, Relation between Alternating Symbol and Kronecker Delta, Tensors of First, Second and Higher Orders, Algebra of Tensors, Contraction of Tensor, Quotient Theorem, Symmetric and Skew-Symmetric Tensors, Invariance Property, Isotropic Tensors, Differentiation of Tensors, Application of Tensors in Modeling Anisotropic Systems, Study of Physical Tensors, Diagonalization of Inertia Tensor as Aligning Coordinate Frame with Natural Symmetries of the System

Text and Reference Books

1. D.E. Bourne and P.C. Kendall, *Vector Analysis and Cartesian Tensors*, 2nd Edition, Thomas Nelson, 1977.
2. G. E. Hay, *Vector and Tensor Analysis*, Dover Publications, Inc., New York, 1979.
3. N.A. Shah, *Vector and Tensor Analysis*, A-One Publishers, Lahore, 2005.
4. I. S. Sokolnikoff, *Tensor Analysis: Theory and Application*, John Wiley and Sons, New York, 1951.
5. J. L. Synge and A. Schild, *Tensor Calculus*, Courier Dover Publications, 1978.

Course Code: MAT-3606

Title: Scientific Programming

Credit Hrs: 2+1

Course Outline (Matlab, Maple, and Mathematica): A list of contents is given below. However the instructor may add or remove some of the contents depending on the need of the students.

Curve sketching (only graphs of functions of one variable in Cartesian Coordinates) by using standard procedure, Intro to MATLAB (history, installation, interface, using product help, etc), MATLAB vs Maths syntax, sketching plane curves and surfaces in MATLAB, use of MATLAB in linear algebra, symbolic computations using MATLAB, creating script and function m-files, MATLAB codes for Bisection, Newton-Raphson, secant, Regula-Falsi, Jacobi, GS, Euler, and RK-4 methods. A brief introduction to Maple/Mathematica, comparison between similar features of MATLAB and Maple/Mathematica.

The following points are important for teaching this course:

1. The course should be taught in a computer lab setting
2. At the completion of this course, the students must be able to utilize the software to solve computationally difficult problems
3. The students should have a good command on at least two of the three programs mentioned above

Text and Reference Books

1. D. M. Etter, D. Kuncicky and D. Hull, *Introduction to Matlab-6*, Prentice Hall, 2001.
2. F. Garvan, *The Maple Book*, Chapman and Hall/CRC, 2002.
3. A. Gilat, *MATLAB: An Introduction with Applications*, 5th Edition, Wiley, 2014.
4. L. Nichal, *Maple*, 1st Edition, Nancy Paulsen Books, 2014.
5. S. Kaufmann, *Mathematica as a Tool: An Introduction with Practical Examples*, Springer-Verlag, 1994.

Semester-VII

Course Code: MAT-4701

Title: Measure Theory

Credit Hrs: 03

Course Outline: Definition and Examples of Algebra and σ -Algebra, Basic Properties of Measurable Spaces, Definition and Examples of Measure Spaces, Outer Measure, Lebesgue Measure, Measurable Sets, Complete Measure Spaces, Measurable Functions: Some Equivalent Formulations of Measurable Functions, Examples of Measurable Functions, Various Characterizations of Measurable Functions, Properties that Hold Almost Everywhere, Definition of Lebesgue Integral, Basic Properties of Lebesgue Integrals, Comparison between Riemann Integration and Lebesgue Integration, L_2 -Spaces

Text and Reference Books

1. D. L. Cohn, *Measure Theory*, Birkhauser, 1980.
2. P. R. Halmos, *Measure Theory*, D. Van Nostrand, 1950.
3. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
4. T. Tao, *An Introduction to Measure Theory*, American Mathematical Society, 2011.
5. P. R. Halmos, *Measure Theory, 2nd Edition*, Springer, 1978.

Course Code: MAT-4702

Title: Mathematical Physics

Credit Hrs: 03

Course Outline: Definition and Properties of Laplace and Inverse Laplace Transforms, s-shifting property of LT, existence and uniqueness theorem, LT of derivatives and integrals and solution of ivps, unite step function and t-shifting property of LT, solution of circuit problems by using LT, Dirac Delta Function and its properties, LT of periodic functions, Convolution Theorem, Convolution of discontinuous functions, solution of integral equations by LT, differentiation and integration of LT, Laguerre's equation and polynomials, Applications of Laplace Transforms to systems of ODEs and PDEs, Fourier Series of 2π and $2L$ periodic functions, Convergence and sum of FS, even and odd functions and half-range expansions of FS, solution of odes and pdes by using FS, Fourier Integrals, Fourier Sine and Cosine integrals, Fourier sine and cosine transforms, Fourier sine and cosine transforms of derivatives, existence of FT, FT of derivatives, Convolution theorem, Discrete and Fast Fourier Transforms, solution of odes and pdes by using FT.

Text and Reference Books

1. E. Kreyszig, *Advanced Engineering Mathematics*, 10th Edition, Wiley, 2011.
2. E. L. Butkov, *Mathematical Physics*, Addison Wesley, 1973.
3. R. P. Kanwal, *Linear Integral Equations*, Academic Press, 1971.
4. T. Myint-U and L. Denbnath, *Partial Differential Equations*, Elsevier Science Publishing, 1987.
5. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Vol. II, Mc-Millan Publishing Company, Inc., New York, 1968.

Course Code: MAT-4703

Title: Numerical Methods-II

Credit Hrs: 03

Course Outline: IVP for ODEs: Elementary theory of ivps, Introduction to Single-Step Numerical Methods for solution of ivps, Picard's method, Euler's Method, Second and higher order Taylor's methods, RK-methods (mid-point, modified Euler, Heun's, and RK-4 methods), Multi-Step methods for numerical solutions of odes (2-, 3-, 4-, and 5-step Adam-Bashforth and Adam-Moulton methods), Extension of Euler and RK-4 methods for numerical solutions of higher order odes and system of first order odes, stability, consistency, and convergence of SS and MS methods, stiff odes, region of absolute stability and A-Stability, BVPs for odes: Discussion on Problem Behavior and Stability, Shooting method and finite difference methods for Linear and Non-Linear BVPs, Rayleigh-Ritz method for Linear and Non-Linear BVPs.

Text and Reference Books

1. U. Ascher and L. Petzold, *Computer Methods for ODEs and DAEs*, SIAM, 1998.
2. R.L. Burden and J.D. Faires, *Numerical Analysis*, 5th Edition, PWS Publishing Company, 1993.
3. U. Ascher, R. Mattheij and R. Russell, *Numerical Solution of BVPs for ODEs*, Prentice Hall, 1988.
4. J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.
5. A. Greenbaum and T. P. Chartier, *Numerical Methods, 2012 Edition*, Princeton University Press, 2012.

Course Code: MAT-4704

Title: Functional Analysis

Credit Hrs: 03

Course Outline: Definition and Examples of Normed Spaces, Banach Spaces, Characterization of Banach Spaces, Bounded Linear Transformations, Bounded Linear Operators, Functional and Their Examples, Various Characterization of Bounded (Continuous) Linear Operator, The Space of All Bounded Linear Operators, The Open Mapping and Closed Graph Theorems, The Dual (Conjugate) Spaces, Reflexive Spaces, Hahn-Banach Theorem (Without Proof), Some Important Consequences of the Hahn- Banach Theorem. Inner Product Spaces, Hilbert Spaces, Orthonormal Bases, Convexity in Hilbert Spaces, Operators in Hilbert Spaces, Invariant Sub-Spaces, Decomposition of Hilbert Spaces, Finite Dimensional Spectral Theory and Spectral Mapping Theorem.

Text and Reference Books

1. E. Kreyszig, *Introductory Fundamental Analysis with Applications*, John Wiley and Sons, 2007.
2. I. J. Maddox, *Elements of Functional Analysis*, Cambridge University Press, 1988.
3. W. Rudin, *Functional Analysis*, Mc-Graw Hill, 2016.
4. G. F. Simmon, *Introduction to Topology and Modern Analysis*, Mc-Graw Hill, New York, 2004.
5. A. Majeed, *Elements of Topology and Functional Analysis*, Ilmi Kitab Khana, 2014.

Course Code: MAT-4705

Title: Fluid Mechanics-I

Credit Hrs: 03

Course Outline: Fields and Continuum Concepts, Lagrangian and Eulerian Specifications, Local, Convective and Total Rates of Change, Conservation of Mass, Equation of Continuity, Boundary Conditions, Nature of Force in a Fluid Field and Their Effects: Surface and Body Forces, Stress at a Point, Viscosity and Newton's Viscosity Law, Viscous and Inviscid Flows, Laminar and Turbulent Flows, Compressible and Incompressible Flows

Irrotational Fluid Motion: Velocity Potential from an Irrotational Velocity Field, Streamlines. Vortex Lines and Vortex Sheets, Kelvin's Minimum Energy Theorem, Conservation of Linear Momentum, Bernoulli's Theorem and Its Applications, Circulations, Rate of Change of Circulation (Kelvin's Theorem), Axially Symmetric Motion, Stokes Stream Function

Two-Dimensional Motion: Stream Function, Complex Potential and Complex Velocity, Uniform Flows, Sources, Sinks and Vortex Flows, Flow in a Sector, Flow Around a Sharp Edge, Flow Due to a Doublet

Text and Reference Books

1. I. G. Curie, *Fundamentals of Mechanics of Fluids*, 3rd Edition, CRC, 2002.
2. I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
3. R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
4. H. Schlichting, K. Gersten, E. Krause and H. Oertel, Jr, *Boundary-Layer Theory*, 8th Edition, Springer-Verlag, 2004.
5. Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

Course Code: MAT-4706

Title: Operation Research

Credit Hrs: 03

Course Outline: Introduction to Operation Research and Real Life Phases, Introduction to Linear Programming (LP) with Examples, Graphical Solutions to Mathematical Model with Special Cases, Simplex Algorithm and its Different Cases, Big M Method and Two Phase Method, Scheduling and Blending Problems, The Transportation Problems, The Transshipment Problems, The Assignment Problems, Integer Programming, Network Models, Inventory Models

Text and Reference Books

1. Hillier and Lieberman, *Introduction to Operations Research*, 9th Edition, Mc-Graw Hill, 2010.
2. P. R. Murthy, *Operations Research*, New Age International (P) Limited Publishers, New Delhi, 2007.
3. Taha and Hamdy, *Operations Research*, 7th Edition, Mc-Millan Publishing Company, Inc., New York, 2003.
4. W. L. Winston, *Practical Management Science: Spreadsheet Modeling and Applications*
5. F. S. Hillier and G. J. Liberman, *Operations Research, 9th Edition*, McGraw-Hill Science/Engineering/Math, 2009.

Course Code: MAT-4707

Title: Discrete Structures

Credits: 3

Course Outlines: Set and Relations: Basic Notions, Set Operations, Venn Diagrams, Extended-Set Operations, Indexed Family of Sets, Countable and Uncountable Sets, Relations, Cardinality, Equivalence Relations, Congruence, Partitions, Partial Order, Representation of Relations, Mathematical Induction

Elementary Logic: Logics of Order Zero and One, Propositions and Connectives, Truth Tables, Conditionals and Bi-Conditionals, Quantifiers, Methods of Proof, Proofs Involving Quantifiers

Text and Reference Books

1. K. H. Rosen, *Discrete Mathematics and its Applications*, 12th Edition, Mc-Graw Hill, New York, 1999.
2. K. A. Ross and C. R. B. Wright, *Discrete Mathematics*, Prentice Hall, Englewood Cliffs, NJ, USA, 2003.
3. H. Fell and J. A. Aslam, *Discrete Structures*, 5th Edition, Cognella Academic Publishing, 2016.
4. S. S. Epp, *Discrete Mathematics with Applications*, 4th Edition, Brooks Cole, 2010.
5. B. Kolman and R. C. Busby, *Discrete Mathematical Structures*, 6th Edition, Pearson, 2017.

Course Code: MAT-4708

Title: Special Functions

Credit Hrs: 03

Course Outline: Infinite Products: introduction, Definition of an infinite product, A necessary condition for convergence, Associated series of logarithms, Convergences types, The Gamma and Beta Functions: The Euler constant, The Gamma function, A series for logarithmic differential of Gamma function, The order symbols o and O , Evaluation of certain infinite products, The Beta Function, Factorial function, Asymptotic Series: Definition of an asymptotic expansion, Algebraic properties, Term by term integration, Uniqueness, The Hypergeometric function : Simple integral form, The function $F(a,b;c,z)$ and its properties, The Hypergeometric differential equation, Logarithmic solution of the hypergeometric function, $F(a,b;c,z)$ as a function of parameters, Elementary series manipulation, Kummer Theorem, Generalized Hypergeometric functions, the exponential and binomial functions, A differential equation, Saalschutz theorem, Contour integral integrals of Barnes' type, the Barnes integrals and the generalized hypergeometric function, Bessel Functions and its properties, The Confluent Hypergeometric functions and its properties, Generating Functions.

Text and Reference Books

1. E. D. Rainville, *Special Functions*, 1st Edition, The Macemillean Company New York, 1965.
2. L. J. Slater, and D. Lit, *Confluent Hyper geometric Functions*, Cambridge University Press, London, 1960.
3. A. Erdelyi, *Higher Transcendental Functions*, Volume I, II, & III, McGraw Hill Book Company, Inc 1995.
4. J. E. Andrews, R. Asky and R. Roy, *Special Functions*, 1st Edition, Cambridge University Press, 2001.
5. S. C. Viola, *Special Functions*, 1st Edition, Springer, 2016.

Course Code: MAT-4709

Title: Quantum Mechanics-I

Credit Hrs: 03

Course Outline: Black Body Radiation, Photoelectric Effect, Compton Effect, Bohr's Theory of Atomic Structure, Wave-Particle Duality, The De Broglie Postulate, Heisenberg Uncertainty Principle, The Postulates of Quantum Mechanics, Operators, Eigen-functions and Eigenvalues: Observables and Operators. Measurement in Quantum Mechanics, The State Function and Expectation Values Time, Development of the Stat Function (Schrodinger Wave Equation), Solution to the Initial-Value Problem in Quantum Mechanics, Parity Operators
Function Spaces and Hermitian Operators: Particle in a Box, Dirac Notation, Hilbert Space. Hermitian Operators, Properties of Hermitian Operators, Additional One-Dimensional Problems: Bound and Unbound States: General Properties of the One Dimensional Schrodinger Equation, Unbound States, One-Dimensional Barrier Problems, The Rectangular Barrier, Tunneling

Text and Reference Books

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2001.
2. H. D. Dehmen, *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics: A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Co., 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

Course Code: MAT-4710

Title: Ring Theory

Credit Hrs: 03

Course Outline:

Rings: Definition, examples. Quadratic integer rings. Examples of non-commutative rings. The Hamilton quaternions. Polynomial rings. Matrix rings. Units, zero-divisors, nilpotents, idempotents. Subrings, Ideals. Maximal and prime Ideals. Left, right and two-sided ideals;

Operations with ideals. The ideal generated by a set. Quotient rings. Ring homomorphism. The isomorphism theorems, applications. Finitely generated ideals. Rings of fractions.

Integral Domain: The Chinese remainder theorem. Divisibility in integral domains, greatest common divisor, least common multiple. Euclidean domains. The Euclidean algorithm. Principal ideal domains. Prime and irreducible elements in an integral domain. Gauss lemma, irreducibility criteria for polynomials. Unique factorization domains. Finite fields. Polynomials in several variables. Symmetric polynomials. The fundamental theorem of symmetric polynomials.

Text and Reference Books

1. J. B. Fraieigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. B. Hartley and T. O. Hawkes, *Ring, Modules and Linear Algebra*, Chapman and Hall, 1980.
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. S. J. Leon, *Linear Algebra with Applications*, 6th Edition, Prentice Hall, 2002.
5. P. M. Cohn, *Introduction to Ring Theory*, 1st Edition, Springer, 2002.

Course Code: MAT-4711

Title: Analytical Dynamics

Credit Hrs: 03

Course Outline: Constraints, Generalized Coordinates, Generalized Forces, General Equation of Dynamics, Lagrange's Equations, Conservation Laws, Ignorable Coordinates, Explicit Form of Lagrange's Equation in Terms of Tensors. Hamilton's Principle of Least Action, Hamilton's Equations of Motion, Hamilton-Jacobi Method, Poisson Brackets (P.B's); Poisson's Theorem; Solution of Mechanical Problems by Algebraic Technique Based on (P.B's) Small Oscillations and Normal Modes, Vibrations of Strings, Transverse Vibrations Normal Modes, Forced Vibrations and Damping, Reflection and Transmission at a Discontinuity, Longitudinal Vibrations, Rayleigh's Principle

Text and Reference Books

1. F. Chorlton, *Textbook of Dynamics*, Van Nostrand, 1963.
2. W. Chester, *Mechanics*, George Allen and Unwin Ltd. London, 1979.
3. H. Goldstein, *Classical Mechanics*, Cambridge University Press, 1980.
4. G. Meirovitch, *Methods of Analytical Dynamics*, Mc-Graw Hill, 1970.
5. H. Baruh, *Analytical Dynamics*, 1st Edition, WCB/McGraw-Hill, 1998.

MAT-4712

Introduction to Difference Equations

Credit Hrs: 3

Course Outlines: First, second and higher order differences, Some properties of operators E and Δ , Equivalence of operators, Infinite Summations, The operator Δ^{-1} , Analogies between the Difference and Differential calculus, Generating functions and approximate summation, Difference equations, Linear and nonlinear difference equations, Homogenous and Non-homogenous difference equations, solutions of a Difference Equations, An existence and Uniqueness Theorem, Sequences, Solutions as sequences, Simple and Compound interest, Inventory Analysis, Approximating a Differential equations by a Difference equations, General results for linear Difference Equations, Applications, Linear Difference Equations with constant coefficients, Fundamental set of solutions, General solution of Homogenous equations, Particular solutions of complete difference equations, Limiting behavior of solutions, Examples from Social Sciences, General case of order n , Difference equation with variable coefficients, Linearizeable Nonlinear difference equations, Methods for solving Difference Equations, Equilibrium and stability of Solutions, First-order Equations and Cobweb Cycles, A Characteristic-Value Problem.

Recommended Books:

1. S. Goldberg, *Introduction to Difference Equations*, John Wiley & Sons, Inc. New York. London, 1958.
2. W. G. Kelley, A. C. Peterson, *Difference Equations: An Introduction with Applications*, Academic Press, USA, 2001.
3. Ronald E Micken, *Difference equations theory applications and advanced topics*, third edition, 2015.
4. S. Elydi, *Introduction to Difference Equations*, 3rd edition, Springer, 2005.
5. W. G. Kelly and A. C. Peterson, *Difference Equation: An Introduction with Applications*, 2nd edition, Academic Press, 2000.

Course Code: MAT-4713

Title: Differential Geometry-II

Credit Hrs: 03

Course Outline: Definition and Examples of Manifolds, Differential Maps, Sub-Manifolds, Tangents, Coordinate Vector Fields, Tangent Spaces, Dual Spaces, Multi-Linear Functions, Algebra of Tensors, Vector Fields, Tensor Fields, Integral Curves, Flows, Lie Derivatives, Brackets, Differential Forms, Introduction to Integration Theory on Manifolds, Riemannian and Semi-Riemannian Metrics, Flat Spaces, Affine Connections, Parallel Translations, Covariant Differentiation of Tensor Fields, Curvature and Torsion Tensors, Connection of a Semi-Riemannian Tensor, Killing Equations and Killing Vector Fields, Geodesics, Sectional Curvature

Text and Reference Books

1. R. Abraham, J. E. Marsden and T. Ratiu Manifolds, *Tensor Analysis and Applications*, Addison Wesley, 1983.
2. R. L. Bishop and S. I. Goldberg, *Tensor Analysis on Manifolds*, Dover Publications, Inc., New York, 1980.
3. M. P. Do Carmo, *Riemannian Geometry*, Birkhauser, 1992.
4. D. Langwitz, *Differential and Riemannian Geometry*, Academic Press, 1970.
5. E. Kreyszig, *Differential Geometry, 1st Edition*, Dover Publications, 1991.

Course Code: MAT-4714

Title: Electromagnetic Theory-I

Credit Hrs: 03

Course Outline: Electromagnetic Fields, Coulomb's Law, The Electric Field Intensity and Potential, Gauss's Law and Deductions, Poisson and Laplace Equations, Conductors and Condensers, Dipoles, The Linear Quadrupole, Potential Energy of a Charge Distribution, Dielectrics, The Polarization and Displacement Vectors, General Solutions of Laplace's Equation. Solutions of Laplace's Equation in Spherical Coordinates, Legendre's Equation, Legendre's Polynomials, Electromagnetic Fields, The Magnetostatic Law of Force, The Magnetic Induction, The Lorentz Force on a Point Charge Moving in a Magnetic Field, The Divergence of the Magnetic Field, The Vector Potential, The Conservation of Charge and Equation of Continuity, The Lorentz Condition, The Curl of The Magnetic Field, Ampere's Law and the scalar Potential, Steady and Slowly Varying Currents, Electric Current, Linear Conductors. Conductivity, Resistance, Kirchhoff's Laws, Current Density Vector, Magnetic Field of Straight and Circular Current, Magnetic Flux, Vector Potential, Forces on a Circuit in Magnetic Field

Text and Reference Books

1. D. Corrison and P. Lorrison, *Introduction to Electromagnetic Fields and Waves*, W.H. Freeman and company, London, 1962.
2. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
3. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
4. G. E. Owen, *Introduction to Electromagnetic Theory*, Dover, 2003.
5. J. R. Reitz, F. J. Milford and R. W. Christy, *Foundations, of Electromagnetic Theory*, Addison-Wesley Publishing, 1993.

Course Code: MAT-4715

Title: Conference/Seminar/Reading-I

Credit Hrs: S/U

Course Outline: The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also be trained on preparing papers and presentations for conferences and seminars.

Text and Reference Books

As per requirement of the students taking the course.

Course Code: MAT-4716

Title: Project/Report

Credit Hrs: 06

Course Outline:

The objective of this course is to train students to learn and use the tools required for writing their project reports and the tools for doing their research work. They will do the literature survey, work on some research problem (theoretical or practical) and write a project or review report by the end of the course.

Text and Reference Books

As per requirements of the topic of the Project.

Semester-VIII

Course Code: MAT-4801

Title: Mathematical Systems Theory

Credit Hrs: 03

Course Outline: Conservation laws and phenomenological principles, some principles and laws of thermodynamics, mechanics, and electromagnetism and their applications in modelling, Linearization, matrix exponentials and solution of linear differential equations, LTV systems, Impulse and step responses, Stability, controllability, and observability of LTI systems, Realization theory and Hankel matrices, Feedback and stabilizability, observers and state reconstruction, detectability, separation principle and compensation, disturbance rejection,

Laplace transforms and LTI systems, transfer functions and transfer matrices, transfer functions and minimal realizations of SISO and MIMO systems, Abstract systems description and behavioral modeling, polynomial representations of systems, brief discussion of nonlinear, descriptor, stochastic, distributed parameter, and discrete event systems, optimal control theory, parameter estimation, filter theory, model reduction, and adaptive and robust control

Text and Reference Books

1. G. J. Olsder, J. W. van der Woude, J. G. Mask, and D. Jeltsema, *Mathematical Systems Theory*, 4th Edition, VSSD, 2011.
2. I. D. Hinrichsen and A. J. Pritchard, *Mathematical Systems Theory*, Springer
3. J. W. Polderman and J. C. Willems, *Introduction to Mathematical Systems Theory*, 2nd Edition, Springer, 2008.
4. J. Zabczyk, *Mathematical Control Theory*, 1st Edition, Birkhauser, 2007.
5. E. D. Sontag, *Mathematical Control Theory*, 2nd Edition, Springer, 1998.

Course Code: MAT-4802

Title: Mathematical Modeling

Credit Hrs: 03

Course Outline: Introduction to modeling. Basic Guide line of mathematical modeling, Collection and interpretation of data, Technique of mathematical modeling, Classification of mathematical modeling, modeling through algebra, modeling through Geometry, modeling through Trigonometry, modeling through Calculus, Limitation of modeling, Development of Models', , Discrete and Continuous models,, Linear Growth and Decay Model, Non-linear Growth and decay models, Mathematical modeling in population dynamic, Traffic flow models.

Text and Reference Books

1. D. Edwards and M. Hamson, *Mathematical modeling Skills*, MacMillan Press Ltd., 1996
2. F. R. Giordano, M. D. Weir, and W. P. Fox, *A First Course in Mathematical modeling*, Thomson Brooks/Cole, 2003
3. J. N. Kapur, *Mathematical modeling*, New Age International Limited, 2015.
4. S. Banerjee, *Mathematical modeling (Modell analysis and Application)*
5. J. J. Batzel, M. Bachar, and F. Kappel, *Mathematical Modeling and Validation in Physiology*, 2013

Course Code: MAT-4803

Title: Integral Equations

Credit Hrs: 03

Course Outline: Linear integral equations of the first and second kind. Relationship between differential equation and Volterra integral equation. Neumann series. Fredholm Integral equation of the second kind with separable Kernels. Eigenvalues and eigenvectors. Iterated functions. Quadrature methods. Least square methods. Homogeneous integral equations of the second kind. Fredholm integral equations of the first kind. Fredholm integral equations of the second kind. Abel's integral equations. Hilbert Schmidt theory of integral equations with symmetric Kernels. Regularization and filtering techniques, Introduction to Wiener-Hopf Technique.

Text and Reference Books

1. J. J. Abdul, *Introduction to Integral Equations with Applications*, Marcel Dekker Inc. New York, 1985.
2. V. Lovitt, *Linear Integral Equations*, Dover Publications, Inc., New York, 1950.
3. B. Noble, *Methods Based on the Wiener-Hopf Technique*, Pergamon Press, 1988
4. F. Smith, *Integral Equations*, Cambridge University Press, 2003
5. F. G. Tricomi, *Integral Equations*, Interscience, 1957.

Course Code: MAT-4804

Title: Optimization Theory

Credit Hrs: 03

Course Outline: Linear Programming: Simplex Method, Duality Theory, Dual and Primal-Dual Simplex Methods Unconstrained Optimization: Optimality Conditions, One-Dimensional Problems, Multi-Dimensional Problems and the Method of Steepest Descent, Constrained Optimization with Equality Constraints, Optimality Conditions, Lagrange Multipliers, Hessians and Bordered Hessians, Inequality Constraints, the Kuhn-Tucker Theorem and Applications

Text and Reference Books

1. L. Elsgolts, *DEs and the Calculus of Variations*, Mir Publishers Moscow, 1970.
2. B. S. Gotfried and J. Weisman, *Introduction to Optimization Theory*, Prentice Hall, Englewood Cliffs, NJ, USA, 1973.
3. D. G. Luenberger, *Introduction to Linear and Non-Linear Programming*, Addison Wesley, Reading, Ma. USA, 1973.
4. H. T. Jongen and K. Meer, *Optimization Theory*, 2004 Edition, Springer, 2004.
5. A. Beck, *Introduction to Nonlinear Optimization: Theory, Algorithms, and Applications with MATLAB*, SIAM-Society for Industrial and Applied Mathematics, 2014.

Course Code: MAT-4805

Title: Fluid Mechanics-II

Credit Hrs: 03

Course Outline: Circular Cylinder without Circulation, Circular Cylinder with Circulation Blasius Theorem, Kutta Condition and the Flat-Plate Airfoil, Joukowski Airfoil, Vortex Motion, Karman's Vortex Street, Method of Images, Velocity Potential, Stoke's Stream Function, Solution of the Potential Equation, Uniform Flow Source and Sink, Flow Due to A Doublet Viscous Flows of Incompressible Fluids: Constitutive Equations, Navier-Stokes's Equations, Exact Solutions of Navier-Stokes's Equations, Steady Unidirectional Flow, Poiseuille Flow, Coquette Flow, Flow between Rotating Cylinders, Stoke's First Problem, Stoke's Second Problem
Simplified Approach to Fluid Flow Problems: Similarity from Differential Equations, Dimensional Analysis, One Dimensional Steady Compressible Flow

Text and Reference Books

1. I. G. Curie, *Fundamentals of Mechanics of Fluids*, 3rd Edition, CRC, 2002.
2. I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
3. R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
4. H. Schlichting, K. Gersten, E. Krause and H. Oertel, *Jr Boundary-Layer Theory*, 8th Edition, Springer-Verlag, 2004.
5. Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

Course Code: MAT-4806

Title: Algebraic Topology

Credit Hrs: 03

Course Outline: Path Wise Connectedness with Examples, Notion of Homotopy, Homotopy Classes and its Application, Path Homotopy, Path Homotopy Classes, Fundamental Groups, Covering Mapping with Examples, Covering Spaces, Lifting Properties of Covering Spaces and its Application, Fundamental Group of a Circle (s)

Text and Reference Books

1. M. J. Greeberge, *Algebraic Topology, A first Course*, Benjamin Commings, 1967.
2. C.A. Kosniowski, *First course in Algebraic Topology*, Cambridge University press, 1980.
3. A. H. Wallace, *Algebraic Topology*, Homology and Cohomology, Benjamin, 1968.
4. A. Hatcher, *Algebraic Topology*, 1st Edition, Cambridge University Press, 2001.
5. W. Fulton, *Algebraic Topology*, Springer, 1997.

Course Code: MAT-4807

Title: Special Functions

Credit Hrs: 03

Course Outline: Infinite Products: introduction, Definition of an infinite product, A necessary condition for convergence, Associated series of logarithms, Convergences types, The Gamma and Beta Functions: The Euler constant, The Gamma function, A series for logarithmic differential of Gamma function, The order symbols o and O , Evaluation of certain infinite products, The Beta Function, Factorial function, Asymptotic Series: Definition of an asymptotic expansion, Algebraic properties, Term by term integration, Uniqueness, The Hypergeometric function : Simple integral form, The function $F(a,b;c,z)$ and its properties, The Hypergeometric differential equation, Logarithmic solution of the hypergeometric function, $F(a,b;c,z)$ as a function of parameters, Elementary series manipulation, Kummer Theorem, Generalized Hypergeometric functions, the exponential and binomial functions, A differential equation, Saalschutz theorem, Contour integral integrals of Barnes' type, the Barnes integrals and the generalized hypergeometric function, Bessel Functions and its properties, The Confluent Hypergeometric functions and its properties, Generating Functions.

Text and Reference Books

1. E. D. Rainville, *Special Functions*, 1st Edition, The Macmillan Company New York, 1965.
2. L. J. Slater and D. Lit, *Confluent Hypergeometric Functions*, Cambridge University Press, London, 1960.
3. A. Erdelyi, *Higher Transcendental Functions*, Volume I, II, & III, McGraw Hill Book Company, Inc. 1953.
4. J. E. Andrews, R. Asky and R. Roy, *Special Functions*, 1st Edition, Cambridge University Press, 2001.
5. C. Viola, *Special Functions*, 1st Edition, Springer, 2016.

Course Code: MAT-4808

Title: Financial Mathematics

Credit Hrs: 03

Course Outline: First-order recurrences. The Cobweb model. Contours and isoquants. Optimisation in two variables. Vectors, preferences and convexity. Constrained optimization, elementary theory of the firm, Cobb-Douglas firm. Lagrangeans and the consumer, elementary theory of the consumer. Second-order recurrences, dynamics of economy, business cycles. Ordinary differential equations, continuous-time models, market trends and consumer demand.

Financial markets. Quantitative methods: binomial trees and arbitrage, spreadsheets to compute stocks and option trees. Continuous time models: Black-Scholes. Hedging. Bond models and interest rate options. Computational methods for bonds. Currency markets and foreign exchange risks.

Text and Reference Books

1. C. Ruckman, *Financial Mathematics*, 2nd edition, BPP Professional Education, 2005.
2. A. Solla, *Financial Mathematics*, 2015th edition, Create Space Independent Publishing Platform 2015.
3. K. J. Hastings, *Introduction to Financial Mathematics*, 1st edition, Chapman and Hall/CRC, 2015.
4. W. S. Chan, *Financial Mathematics for Actuaries*, 2nd edition, World Scientific Publishing Company, 2017.
5. G. Campolieti and R. N. Makarov, *Financial Mathematics*, 1st edition, Chapman and Hall/CRC, 2014.

Course Code: MAT-4809

Title: Quantum Mechanics-II

Credit Hrs: 03

Course Outline: Harmonic Oscillator and Problems in Three-Dimensions: The Harmonic Oscillator, Eigen-Functions of the Harmonic Oscillator, The Harmonic Oscillator in Momentum Space, Motion in Three Dimensions, Spherical Symmetric Potential and the Hydrogen Atom, Angular Momentum: Basic Properties, Eigenvalues of the Angular Momentum Operators, Eigen-Functions of the Orbital Angular Momentum Operators L_2 and L_z , Commutation Relations between Components of Angular Momentum and Their Representation in Spherical Polar Coordinates
The Scattering Cross-Section, Scattering Amplitude, Scattering Equation, Born Approximation, Partial Wave Analysis, Time Independent Perturbation of Non-Degenerate and Degenerate Cases, Time-Dependent Perturbations

Text and Reference Books

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2004.
2. H. D. Dehmen *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics, A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Company, 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

Course Code: MAT-4810

Title: Introduction to Combinatorics

Credit Hrs: 03

Course Outline: Two Basic Counting Principle, Permutations, Combinations, The Injective and Bijective Principles, Arrangements and Selections with Repetitions, Graphs in Combinatorics, The Binomial Theorem, Combinatorial Identities, Properties of Binomial Coefficients, Multinomial Coefficients, The Multinomial Theorem, The Pigeonhole Principle, Examples, Ramsay Numbers, The Principle of Inclusion and Exclusion, Generalization, Integer Solutions, Surjective Mapping. Stirling Numbers of the Second Kind, The Sieve - Eratosthenes, Euler Φ -Function, The Problem Des-Menages Ordinary Generating Functions, Modeling Problems, Partition of Integers, Exponential Generating Functions
Linear Homogeneous Recurrence Relations, Algebraic Solutions of Linear Recurrence Relations and Constant Functions, The Method of Generating Functions, A Non-Linear Recurrence Relation and Catalaa Numbers

Text and Reference Books

1. V. K. Balakrishnan, *Theory and Problems of Combinatorics*, Schaum's Outline Series, Mc-Graw Hill, Singapore, 1995.
2. C. C. Chen and K. M. Koh, *Principles and Techniques in Combinatorics*, World Scientific Publishing Company, Pvt. Ltd, Singapore, 1992.
3. C. L. Liu, *Introduction to Combinatorial Mathematics*, Mc-Graw Hill, New York, 1968.
4. A. Tucker, *Applied Combinatorics*, John Wiley and Sons, New York, 1985.
5. R. A. Brualdi, *Introductory Combinatorics*, 5th Edition, Pearson, 2009.

Course Code: MAT-4811

Title: Dynamical Systems

Credit Hrs: 03

Course Outline: Introduction: Preliminary ideas, Autonomous equations, Autonomous systems in plane, Flows and evolution. Linear systems: Linear changes of variables, Similarity types for 2×2 real matrices, Phase portraits for canonical systems in the plane, Classification of simple linear phase portraits in the plane, The evolution operators, Affine systems, Linear systems of dimension greater than two. Nonlinear systems in the plane: Local and global behavior, Linearization at a fixed point, The linearization theorem, Non-simple fixed points, Stability of fixed points, Ordinary points and global behavior, First integrals, Limit points and limit cycles. Flows on non-planar phase spaces: Fixed points, Closed orbits, Attracting sets and attractors, Further integrals. Applications: Linear models, Affine models, Nonlinear models, Relaxation oscillation, Piecewise modeling. Dynamical systems with mathematica: Differential equations, Planar systems, Interacting species, Limit cycles.

Text and Reference Books

1. Lynch S., *Dynamical systems with applications using mathematica*, Birkhauser Boston 2007.
2. Alligood T. K., Sauer D. T., Yorke A. J., *Chaos: An introduction to dynamical systems*, Springer 1996.
3. R. C. Robinson, *An introduction to dynamical systems*, 1st edition, Prentice Hall, 2004.
4. Arrowsmith K. D., Place M. C., *Dynamical systems, differential equations, maps and chaotic behavior*, Chapman & Hall, 1992.
5. D. K. Arrowsmith and C. M. Place, *An introduction to dynamical systems*, Cambridge University Press, 1st edition, 1990.

Course Code: MAT-4812

Title: Theory of Elasticity

Credit Hrs: 03

Course Outline: Cartesian Tensors, Analysis of Stress and Strain, Generalized Hooke's Law, Crystalline Structure, Point Groups of Crystals, Reduction in the Number of Elastic Moduli Due to Crystal Symmetry, Equations of Equilibrium, Boundary Conditions, Compatibility Equation, Plane Stress and Plane Strain Problems, Two Dimensional Problem in Rectangular and Polar Coordinates, Torsion of Rods and Beams

Text and Reference Books

1. E. Dieulesaint and D. Royer, *Elastic Waves in Solids*, John Wiley and Sons, New York, 1980.
2. Y. C. Funk, *Foundations of Solid Mechanics*, Prentice-Hall, Englewood Cliffs, 1965.
3. Sokolinikoff, *Mathematical Theory of Elasticity*, Mc-Graw Hill, New York.
4. S. P. Temoshenko and J. N. Goodier, *Theory of Elasticity*, 3rd Edition, Mcgraw Hill Education (India) Private Limited, 2015.
5. A. I. Lurie and A. Belyaev, *Theory of Elasticity*, 2005 Edition, Springer, 2005.

Course Code: MAT-4813

Title: Special Theory of Relativity

Credit Hrs: 03

Course Outline: Historical Background and Fundamental Concepts of Special Theory of Relativity, Lorentz Transformations (for Motion Along One Axis), Length Contraction, Time Dilation and Simultaneity, Velocity Addition Formulae, 3-Dimensional Lorentz Transformation, Introduction to 4-Vector Formalism, Lorentz Transformations in the 4-Vector Formalism, The Lorentz and Poincare Groups, Introduction to Classical Mechanics, Minkowski Space-Time and Null Cone, 4-Velocity, 4-Momentum and 4-Force, Application of Special Relativity to Doppler Shift and Compton Effect, Particle Scattering, Binding Energy, Particle Production and Decay, Electromagnetism in Relativity, Electric Current, Maxwell's Equations and Electromagnetic Waves, The 4-Vector Formulation of Maxwell's Equations, Special Relativity with Small Acceleration

Text and Reference Books

1. H. Goldstein, *Classical Mechanics*, Addison Wesley, New York, 1962.
2. D. Inverno, *Introducing Einstein's Relativity*, Oxford University Press, 1992.
3. J. D. Jackson, *Classical Electrodynamics*, John Wiley and Sons, New York, 1962.
4. A. Qadir, *Relativity: An Introduction to the Special Theory*, World, 1992.
5. W. Rindler, *Essential Relativity*, Springer -Verlag, 1977. Scientific, 1962.

Course Code: MAT-4814

Title: Electromagnetic Theory-II

Credit Hrs: 03

Course Outline: The Faraday Induction Law, Induced Electromotance in a Moving System, Inductance and Induced Electromotance, Energy Stored in a Magnetic Field, The Equations of Electromagnetism, Electromagnetic Waves: Plane Electromagnetic Waves in Free Space and Isotropic Media, The Poynting Vector in Free Space, Propagation of Electromagnetic Waves in NON-Conductors, Propagation of Plane Waves in Conducting Media, Reflection and Refraction of Plane Waves, Guided Waves, Coaxial Line, Hollow Rectangular Wave Guide, Radiation of Electromagnetic Waves, Electromagnetic Field of a Moving Charge

Text and Reference Books

1. D. Corrison and P. Lorrison, *Introduction to Electromagnetic Fields and Waves* W.H. Freeman and company, London, 1962.
2. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
3. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
4. G. E. Owen, *Introduction to Electromagnetic Theory*, Dover, 2003.
5. J. V. Stewart, *Intermediate Electromagnetic Theory*, World Scientific, 2001.

Course Code: MAT-4815 **Title:** Conference/Seminar/Reading-I **Credit Hrs:** S/U

Course Outline: The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also trained on preparing papers and presentations for conferences and seminars.

Text and Reference Books

As per requirement of the students taking the course.

Course Code: MAT-4816 **Title:** Comprehensive Oral Exam **Credit Hrs:** S/U

Course Outline: This exam will be conducted at the end of the 8th semester. One external examiners and two internal examiners will conduct this exam from each student.

9- Details of Allied Courses BS-4 Years Program

Course Code: ISL-1101

Title: Islamic Studies

Credit Hrs: 02

Contents: Introduction to Quranic Studies: Basic Concepts of Quran, History of Quran, Uloomul – Quran. Study of Selected Text of Holly Quran: Verses of Surah Al-Baqra Related to Faith (Verse No-284-286), Verses of Surah Al-Hujrat Related to Adab Al-Nabi (Verse No-1-18), Verses of Surah Al-Mumanoon Related to Characteristics of faithful (Verse No-1-11), Verses of Surah al-Furqan Related to Social Ethics (Verse No.63-77), Verses of Surah Al-Inam Related to Ihkam(Verse No-152-154). Study of Selected Text of Holly Quran: Verses of Surah Al-Ihzab Related to Adab al-Nabi (Verse No.6,21,40,56,57,58.), Verses of Surah Al-Hashar (18,19,20) Related to thinking, Day of Judgment, Verses of Surah Al-Saf Related to Tafakar,Tadabar (Verse No-1,14)

Seerat of Holy Prophet (S.A.W), Introduction to Sunnah, Introduction to Islamic Law & Jurisprudence,

Islamic Culture and Civilization, Islam and Science, Islamic Economic System, Political System of Islam, Islamic History: Period of Khlaft-E-Rashida, Ummayyads and Abbasids, Social System of Islam

Text and Reference books:

1. H.U. Muhammad, *Emergence of Islam*, IRI, Islamabad.
2. T. Ramadan, *Introduction to Islam*, 1st Edition, Oxford University Press, 2017.
3. A. Akgunduz, *Introduction to Islamic law*, IUR Press, 2010.
4. M. H. Kamali, *Principles of Islamic Jurisprudence*, 3rd edition, Islamic Texts Society, 2005.

Course Code: ENG-1102

Title: English-I

Credit Hrs: 03

Contents: Basics of Grammar, Parts of Speech and Use of Articles, Sentence Structure, Active and Passive Voice, Practice in Unified Sentence, Analysis of Phrase, Clause and Sentence Structure, Transitive and Intransitive Verbs, Punctuation and Spelling, **Comprehension:** Answers to questions on a given text, **Discussion:** General topics and every-day conversation (topics for discussion to be at the discretion of the teacher keeping in view the level of students), **Listening:** To be improved by showing documentaries/films carefully selected by subject teachers, Translation Skills: Urdu to English, **Paragraph Writing:** Topics to be chosen at the discretion of the teacher, **Presentation skills:** Introduction

Text and Reference books:

1. A. J. Thomson and A. V. Martinet, *Practical English Grammar*, Exercise 1, 3rd Edition, OUP, 1997.
2. A. J. Thomson and A. V. Martinet, *Practical English Grammar*, Exercises 2, 3rd Edition. OUP, 1997.
3. M. C. Boutin, S. Brinand and F. Grellet, *Intermediate Writing*, Oxford Supplementary Skills. 4th Impression 1993, 7 Pages20-27 and 35-41.
4. B. Tomlinson and R. Ellis, *Reading: Upper Intermediate*, Oxford Supplementary Skills, 1992.

Course Code: COM-1103 **Title:** Introduction to Computer and Its Applications **Credit Hrs:** 03

Contents: Content will be determined by the teacher with the following points in view: At the end of the semester student must be equipped with the following:

1. Basics of the hardware and operating system
2. MS Word, Excel, Power Point
3. Use of Internet
4. Installation of Softwares
5. Handling Emails

Text and Reference books:

1. D. D. W. Hajek, *Introduction to Computer*, Create Space Independent Publishing Platform, 2017.
2. G. B. Shelly, S. M. Freund and M. E. Vermaat, *Introduction to Computer*, 8th Edition, Course Technology, 2010.
3. Y. N. Patt and S. J. Patel, *Introduction to Computing Systems*, 2nd Edition, McGraw-Hill Education, 2003.
4. J. Zelle, *Python Programming: An Introduction to Computer Science*, 2nd Edition, Franklin, Beedle & Associates, 2010.

Course Code: PHY-1104 **Title:** Physics-I **Credit Hrs:** 03

Contents: Work and Energy, Impulse and Momentum, Circular Motion, Mass and Energy, Collisions, Center of Mass, Moment, Center of Gravity, Couples, Angular Motion, Kinetic Energy of Rotation, Moment of Inertia, Parallel Axis Theorem, Momentum, Angular Momentum and Energy, Elastic Restoring Forces, Circle of Reference, Harmonic Motion

Density, Pressure in a Fluid, Pressure Gauges, Pumps, Archimedes' Principle, Forces against a Dam, Surface Tension, Pressure Difference across a Surface Film, Contact Angle and Capillarity

Equation of Continuity, Bernoulli's Equation, Applications of Bernoulli's Equation, Viscosity, Poiseuilles's Law, Stokes' Law, Reynolds Number

Waves and Mathematical Description, Speed of a Transverse Wave and Longitudinal Wave, Adiabatic Character of a Longitudinal Wave, Water Waves, Superposition and Standing Waves, Longitudinal Standing Waves, Vibrations of Organ Pipes, Vibrations of Rods and Plates, Interference of Longitudinal Waves, Resonance, Sound Waves, Doppler Effect, Radiation from a Piston, Applications of Acoustic Phenomena

Text and Reference books:

1. F. W. Sears, M. W. Zemansky and H. D. Young, *University Physics*, 3th Edition, 1963.
2. R. A. Serway and J. W. Jewett, *Principles of Physics*, 5th Edition, Brooks Cole, 2012.
3. H. C. Ohanian and J. T. Market, *Physics for Engineers and Scientists*, 3rd Edition, W. W. Norton & Company, 2006.
4. R. D. Knight, *Physics for Scientists and Engineers*, 2th Edition, Addison-Wesley, 2007.

Course Code: HUM-1201

Title: Arabic

Credit Hrs: 02

Course Contents: Arabic to Urdu Translation, Urdu to Arabic Translation, Grammar, Comprehension.

Text and Reference Books: Lisan Ul Arabi, AIOU, Islamabad.

Course Code: ENG-1202

Title: English-II (Communication Skills)

Credit Hrs: 03

Contents: Paragraph Reading (Practice in writing a good, unified, and coherent paragraph), Essay Writing, CV and Job Application, Translation Skills, Study Skills (Skimming and Scanning, intensive and extensive, and speed reading, summary and précis writing, and comprehension), Academic Skills, Personality development (emphasis on content, style, and pronunciation)

Text and Reference Books:

1. A. J. Thomson and A. V. Martinet, *Practical English Grammar*, 3rd Edition, Oxford University Press, 1986.
2. M. Christine, S. Brinard, and F. Grellet, *Oxford Supplementary Skills*, 4th Impression, 1993.
3. R. Nolasco, *Upper Intermediate Writing*, *Oxford Supplementary Skills*, 4th Impression, 1992.
4. B. Tomlinson and R. Ellis, *Advanced Reading*, *Oxford Supplementary Skills*, 3rd Impression, 1991.

Course Code: HUM-1203

Title: Pak-Studies

Credit Hrs: 02

Contents: Historical Perspective: Ideological Rationale with Special Reference to Sir Syed Ahmed Khan, Allama Muhammad Iqbal and Quaid-i-Azam Muhammad Ali Jinnah, Factors Leading to Muslim Separatism, Indus Civilization, Muslim Advent, Location and Geo-physical Features. Political and Constitutional Phases: 1947-58, 1958-71, 1971-77, 1977-88, 1988-99, 1999 and onward Economic Institutions and Issues, Society and Social Structure, Ethnicity, Foreign Policy of Pakistan and Challenges and Futuristic Outlook of Pakistan

Text and Reference books:

1. B. S. Javed, *State & Society in Pakistan*, The Macmillan Press Ltd, 1980.
2. A. S. Zaidi, *Issue in Pakistan's Economy*, Karachi: Oxford University Press, 2000.
3. M. Safdar, *Pakistan Political Roots & Development*, Lahore, 1994.
4. W. Wayne, *The Emergence of Banglades.*, Washington, Institute of PPR, 1972.

Course Code: PHY-1204

Title: Physics-II

Credit Hrs: 03

Contents: Electric Charges, Coulomb's Law, Gauss's Law and Applications, Electrical Potential and Energy, Equipotential Surfaces, Potential Gradient, Electron Volt, Cathode Ray Oscilloscope, Capacitors, Effect of a Dielectric, Polarization and Displacement, Current, Resistance, Electromotive Force, Resistors in Series and Parallel, Kirchhoff's Rules, Ammeters and Voltmeters, Ohmmeter Magnetic Field and Flux, Motion of Charged Particles in Magnetic Fields, Thomson's Measurement of e/m , The Biot-Sarvart Law, Magnetic Field of a Long Straight Conductor and Circular Loop, Ampere's Law and Applications, Electromotive Force, Faraday's Law, Induced Electric Fields, Lenz's Law. First Law of Thermodynamics, Energy and Work in Thermodynamics, Adiabatic, Isochoric, Isothermal, Isobaric and Throttling Processes, Differential Form of the First Law of Thermodynamics, Internal Energy of an Ideal Gas and Heat capacities, Adiabatic Process of an Ideal Gas, Second Law of Thermodynamics, Heat Engines, Internal-Combustion Engines, Steam Engines, The Refrigerator, The Carnot Cycle, The Kelvin Temperature Scale, Absolute Zero, Entropy and the Second Law of Thermodynamics, Energy Conversion, Kinetic Theory of Gases

Text and Reference books:

1. H. C. Ohanian and J. T. Market, *Physics for Engineers and Scientists*, 3rd Edition, W. W. Norton & Company, 2006.
2. F. W. Sears, M. W. Zemansky and H. D. Young, *University Physics*, 3th Edition, 1963.
3. R. A. Serway and J. W. Jewett, *Principles of Physics*, 5th Edition, Brooks Cole, 2012.
4. R. D. Knight, *Physics for Scientists and Engineers*, 2th Edition, Addison-Wesley, 2007.

Course Code: HUM-2301

Title: Introduction to Sociology

Credit Hrs: 03

Contents: Introduction, Scope and Subject Matter, Sociology as a Science, Historical back ground, Basic Concepts, Social Interaction: Levels of Social Interaction, Social Groups, Culture, Norms and Social Sanctions, Socialization & Personality, Deviance and Social Control, Collective Behavior

Text and Reference books:

1. Anderson, Margaret and Howard F. Taylor, *Sociology the Essentials*, Australia, Wadsworth, 2001.
2. Brown Ken, *Sociology*, UK: Polity Press, 2004.
3. J. Macionis John, *Sociology*, 10th Edition New Jersey: Prentice-Hall, 2006.
4. L.Tischler Henry, *Introduction to Sociology*, 7th Ed. New York: The Harcourt Press, 2002.

Course Code: ENG-2302

Title: English-II

Credit Hrs: 03

Contents: Presentation Skills, Essay Writing (Descriptive, narrative, discursive, argumentative), Academic Writing (How to write a proposal for research paper/term paper, how to write a research/term paper with emphasis on style, contents, language, form, clarity, consistency), Technical Report Writing, Progress report Writing.

Text and Reference Books:

1. J. Langan, *Advanced Writing*, Townsend Press, 2014.
2. J. Langan, *College Writing Skills*, Mc Graw Hill, 2004.
3. L. G. Kirszner and S. R. Mandell, *Patterns of College Writing*, 13th Edition, Bedford/St. Martin's, 2016.
4. A. J. Thomson and A. V. Martinent, *Practical English Grammar*, 3rd Edition, Oxford University Press, 1986.

Course Code: HUM-2308

Title: HR Management

Credit Hrs: 03

Course Contents:

Introduction to HRM, Human Resource Planning, Job Design and Analysis, Recruitment & Selection, Motivation & Reward System, Career Planning & Development, Training & Development, Performance Appraisal, Compensation Management & Employee Relation, Employee Health and Safety.

Text and Reference books:

1. R. A. Noe, P. M. Wright, J. R. Hollenbeck and B. Gerhart, *Human Resource Management*, 10th edition, McGraw-Hill Education, 2016.
2. R. L. Mathis and P. Meglich, *Human Resource Management*, 15th edition, South-Western College Pub, 2016.
3. B. Wolfe, *The Little Black Book of Human Resources Management*, Create Space Independent Publishing Platform, 2015.
4. J. H. Jackson, *Human Resource Management*, 14th Edition, South-Western College Pub, 2013.

Course Code: PSY-2401

Title: Educational Psychology

Credit Hrs: 03

Course Contents: Introduction, Nature and Application of Psychology with Special Reference to Pakistan, Historical Background (A Brief Survey), Methods of Psychological Study, Biological Basis of Behavior, Vision, Audition, Perception, Attention, Motives, Emotions, Learning, Memory, Tools of Thinking, Individual Differences

Text and Reference books:

1. L.D. Fernald and P.S. Fernald, *Introduction to psychology*, USA: W M C Brown Publishers, 2005.
2. W. E. Glassman, *Approaches to psychology*, Open University Press, 2000.
3. N. Hayes *Foundation of psychology*, 3rd Edition, Thomson Learning, 2000.
4. B. B. Lahey, *Psychology: An introduction*, 8th Edition, Mc Graw Hill Companies, Inc. (2004).

Course Code: HUM-2408

Title: Organizational Behavior

Credit Hrs: 03

Course Contents: An overview of the field of organizational behavior, Individual behaviour and learning in organizations, Theories of employee motivation and reward system, Communications in Organizations, Group Dynamics, Teambuilding and Decision Making, Organizational Conflict & Resolution strategies, Organizational change and development, Organizational culture and Organizational structure and design.

Text and Reference books:

1. J. Colquitt and J. LePine, *Organizational Behavior: Improving Performance and Commitment in the workspace*, 2014.
2. S. P. Robbins and T. A. Judge, *Organizational Behavior*, 15th edition, 2012.
3. T. A. Judge, *Organizational Behavior*, 13th edition, 2008.
4. R. W. Griffin, *Organizational Behavior : Managing People and Organizations*, 11th edition, 2012.

Course Code: ENG-2409

Title: Business Mathematics

Credit Hrs: 03

Contents: Basic mathematical concepts and their application in various business real numbers, Linear equations and their applications, System of linear equations, Functions (linear functions, quadratic and polynomial functions, exponential and logarithmic functions), Matrix algebra, Differentiation and Integration, Mathematics of finance, Ratios, Proportions and Percentages, Principle of simple Interest, Principle of compound Interest, Annuities, Loans and Mortgages, Investment decisions, Discrete and continuous variables, Linear equations and inequalities and graphs, Progression of Sequence and Series and their applications in business, Permutations, Combination and their applications in business and finance.

Text and Reference books:

1. Frank S. Budnick: *Applied Mathematics for Business and Economics and Social sciences*.
2. E. K. Bowen and G. D. Prichett, *Mathematics with applications in Management and Economics*, 6th Edition, McGraw-Hill Inc, 1986.
3. G. Clendenen and S. A. Salzman, *Business Mathematics*, 13th Edition, Pearson, 2014.
4. C. D. Miller, G. Clendenen and S. A. Salzman, *Business Mathematics*, 12th Edition, Pearson, 2011.

Course Contents:

Introduction: The concept of entrepreneurship, the economist view of entrepreneurship, The sociologist view, Behavioural approach, Entrepreneurship and Management. The Practice of Entrepreneurship: The process of entrepreneurship, Entrepreneurial Management, The entrepreneurial business, Entrepreneurship in service institutions, The new venture Entrepreneurship and Innovation: The innovation concepts, Importance of innovation for entrepreneurship, Sources of innovative opportunities, The innovation process, Risks involved in innovation Developing Entrepreneur: Entrepreneurial profile, Trait approach to understanding entrepreneurship, Factors influencing entrepreneurship, The environment, Socio cultural factors, Support systems Entrepreneurship Organization: Team work, Networking organization, Motivation and compensation, Value system Entrepreneurship and SMES: Defining SMEs, Scope of SMEs, Entrepreneurial, managers of SME, Financial and marketing problems of SMEs Entrepreneurial Marketing: Framework for developing entrepreneurial marketing, Devising entrepreneurial marketing plan, Entrepreneurial marketing strategies, Product quality and design Entrepreneurship and Economic Development: Role of entrepreneur in the economic development generation of services, Employment creation and training, Ideas, knowledge and skill development, The Japanese experience Case Studies of Successful Entrepreneurs

Recommended Books:

1. S. Mariotti and C. Glackin, *Small Business and Entrepreneurship*, 1st Edition, Prentice Hall, 2011.
2. D. B. Audretsch, M. C. Kelibach and E. E. Lehmann, *Entrepreneurship for Economic Growth*, 1st Edition, Oxford University Press, 2006.
3. Peter F. Drucker, *Innovation and Entrepreneurship*, Harper Business, 2006.
4. J. Bessant and J. Tidd, *Innovation and Entrepreneurship*, 3rd Edition, Wiley, 2015.

2. Scheme of Studies for MSc Mathematics: General Breakup

Content		Description	Remarks
2.1	Awarding Institute/Body	Mirpur University of Science and Technology (MUST)	
2.2	Teaching Institute	Department of Mathematics, Mirpur University of Science and Technology (MUST),	
2.3	Final Award	Master of Science in Mathematics	
2.4	Program Title	M.Sc in Mathematics	
2.5	Starting Time for Program	Fall/Spring Semester of each academic year	
2.6	Duration of the Program	4-6 Semesters	
2.7	Entrance Requirement	Bachelor or Equivalent Degree with Mathematics (Min 45% Marks)	
		No D-grade in academic career	
		Entry Test conducted by the University with the following breakup: Mathematics: 60 % (Maths A & B), English: 10%, 30% for one subject which the candidate have studied in B.Sc/B.A.	
2.8	Merit Formula	Merit shall be determined on 10% of HSSC, 10% of Intermediate, 50% Bachelor Degree and 30% of Entry Test marks.	
2.9	Total Credit Hours	Course Work: 59 Credit Hrs	
		Project (Compulsory): 6 Credit Hrs	
		Comprehensive Oral Examination: S/U	
		Conference/Seminars/Reading- I & II: S/U	

2.10 Program Educational Objectives:

The M.Sc Mathematics program is aimed at imparting quality education of mathematics to the youth of Mirpur division and the surrounding districts, at an affordable cost. The program will give an opportunity to the talented youth to satiate their desire to learn and excel in mathematics. The program will meet the demand of skilled mathematicians in the local job market.

The specific objectives of the M.Sc program include: to teach students basic concepts of mathematics, to empower them with analytical and computational skills, to develop critical thinking, and to develop professional approach and work ethics. Moreover, the program is designed in such a way that the students can learn advanced mathematical concepts through the course work and the semester projects.

2.11 Program Learning Outcomes (PLOs):

The curriculum of the two year M.Sc program is so designed that students learn analytical and computational skills for solving mathematical problems. The students are so trained through the class

room activities and assessments that can confidently do industrial, managerial, and teaching assignments.

2.12 Scope of the Program:

The mathematical experts are in demand across all kind of industries, the world over. Our graduates will be able to seek career opportunities in:

- a). Teaching at school, college, or higher level
- b). R&D and strategic organizations like PAEC, NESCOM, SUPARCO, etc.
- c). Banking sector, trading, and stock exchange businesses
- d). higher studies in national and international universities and institutes
- e). armed forces, civil services, oil and gas sector

2.13 Program Structure and Features: Curriculum Units, Credit and Award Requirements

Sr. No.	Category	No. of Courses	Credit Hrs	Remarks
01	Core Courses	15	44	
02	Electives Courses	05	15	
03	Conference?Seminar/Reading I & II	02	S/U	
04	Project	01	06	
05	Comprehensive Oral Examination	01	S/U	
Total		24	65	

2.14 Layout/Framework

Category	Course Title	Credit Hrs	Remarks
Core Courses	Ordinary Differential Equations	03	
	Abstract Algebra	03	
	Real Analysis-I	03	
	Complex Analysis	03	
	Topology	03	
	Scientific Programming	2+1	
	Tensor Analysis	02	
	Differential Geometry-I	03	
	Real Analysis-II	03	
	Partial Differential Equations	03	
	Analytical Mechanics	03	
	Numerical Methods I	03	
	Mathematical Physics	03	
	Functional Analysis	03	
	Integral Equations	03	
	Project	06	
	Comprehensive Oral Examination	S/U	
Conference/Seminar/Reading- I and II	S/U		
Elective Courses	Elective-I	03	
	Elective-II	03	
	Elective-III	03	
	Elective-IV	03	
	Elective-V	03	

2.15 Semester-Wise Breakdown

Course Code	Course Title	Lec. Hrs.	Lab. Hrs.	Credit Hrs.
Semester-I				
MAT-5101	Real Analysis-I	3	0	3
MAT-5102	Ordinary Differential Equations	3	0	3
MAT-5103	Differential Geometry-I	3	0	3
MAT-5104	Analytical Mechanics	3	0	3
MAT-5105	Topology	3	0	3
MAT-5106	Abstract Algebra	3	0	3
Semester-II				
MAT-5201	Real Analysis-II	3	0	3
MAT-5202	Partial Differential Equations	3	0	3
MAT-5203	Numerical Methods I	3	0	3
MAT-5204	Complex Analysis	3	0	3
MAT-5205	Tensor Analysis	2	0	2
MAT-5206	Scientific Programming	2	1	3
Semester-III				
MAT-6302	Mathematical Physics	3	0	3
MAT-6304	Functional Analysis	3	0	3
MAT-6316	Project	0	0	3+3
MAT-6315	Conference/Seminar/Reading-I	S/U		
<u>Two Optional Courses</u>				
MAT-6301	Measure Theory	3	0	3
MAT-6303	Numerical Methods II	3	0	3
MAT-6305	Fluid Mechanics-I	3	0	3
MAT-6306	Operation Research	3	0	3
MAT-6307	Number Theory	3	0	3
MAT-6308	Mathematical Statistics	3	0	3
MAT-6309	Quantum Mechanics-I	3	0	3
MAT-6310	Ring Theory	3	0	3
MAT-6311	Analytical Dynamics	3	0	3
MAT-6312	Introduction to Difference Equations	3	0	3
MAT-6313	Differential Geometry-II	3	0	3
MAT-6314	Electromagnetic Theory-I	3	0	3

Semester-IV

MAT-6403	Integral Equations	3	0	3
MAT-6416	Comprehensive Oral Examination	0	S/U	0
MAT-6415	Conference/Seminar/Reading-II	0	S/U	0

Three Optional Courses

MAT-6401	Mathematical Systems Theory	3	0	3
MAT-6402	Mathematical Modeling	3	0	3
MAT-6404	Optimization Theory	3	0	3
MAT-6405	Fluid Mechanics-II	3	0	3
MAT-6406	Algebraic Topology	3	0	3
MAT-6407	Special Functions	3	0	3
MAT-6408	Financial Mathematics	3	0	3
MAT-6409	Quantum Mechanics-II	3	0	3
MAT-6410	Introduction to Combinatorics	3	0	3
MAT-6411	Dynamical Systems	3	0	3
MAT-6412	Theory of Elasticity	3	0	3
MAT-6413	Special Theory of Relativity	3	0	3
MAT-6414	Electromagnetic Theory-II	3	0	3
MAT-6416	Special Functions	3	0	3

Note:- Elective course mentioned above without any pre-requisite can be taught in 3rd or 4th semester. These courses can only be offered on the availability of the relevant teacher

2.16 Details of the Courses in M.Sc Mathematics

Semester-I

Course Code: MAT-5101

Title: Real Analysis-I

Credit Hrs: 03

Course Outline: Supremum and Infimum, Completeness Properties of the Real Numbers, Limits of Numerical Sequences, Limits and Continuity, Properties of Continuous Functions on Closed Bounded Intervals, Derivatives in One Variable, The Mean Value Theorem, Sequences of Functions, Power Series, Point-Wise and Uniform Convergence, Riemann Integrations

Text and Reference Books

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Real Analysis*, Mc-Graw Hill, 1995.
3. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3rd Edition, John Wiley and Sons, 1999.
4. R. L. Brabenec, *Introduction to Real Analysis*, PWS Publishing Company, 1994.
5. S. Lang, *Real Analysis*, Springer-Verlag, London, 1987.

Course Code: MAT-5102

Title: Ordinary Differential Equations

Credit Hrs: 03

Course Outline: **Review** of first order linear and nonlinear odes and higher order linear odes and their solution techniques. **Basic theory** of systems of first order linear equations, Homogeneous linear system with constant coefficients, Non homogeneous linear system, **Sturm-Liouville** (S-L) System and Boundary-Value Problems, **Series Solution and its Limitations**, The Frobenius Method, Solution of the Bessel, The Hypergeometric, The Legendre and the Hermite Equations, Properties of the Bessel, the Legendre and the Hermite Functions

Text and Reference Books

1. E. A. Coddington and N. Levinson, *Theory of Ordinary Differential Equations*, Mc-Graw Hill, New York, Toronto and London, 1955.
2. W. E. Boyce and R. de Prima, *Elementary Differential Equations*, 9th Edition, Wiley, 2008.
3. P. Hartman, *Ordinary Differential Equations*, John Wesley and Sons, New York, 1964.
4. D. G. Zill and M. R. Cullen, *Differential Equations with Boundary-Value Problems*, 3rd Edition, PWS Publishing Company, 1997.
5. V. I. Arnold and R. Cooke, *Ordinary Differential Equations*, 2006 Edition, Springer, 2006.

Course Code: MAT-5103

Title: Differential Geometry-I

Credit Hrs: 03

Course Outline: Historical Background, Motivation and Applications, Index Notation and Summation Convention, Space Curves, The Tangent Vector Field, Reparametrization; Arc Length, Curvature, Principal Normal, Binormal, Torsion, The Osculating, The Normal and the Rectifying Planes, The Frenet-Serret Theorem, Spherical Images, Sphere Curves, Spherical Contacts, Fundamental Theorem of Space Curves, Line Integrals and Green's Theorem, Local Surface Theory, Coordinate Transformations, The Tangent and the Normal Planes, Parametric Curves, The First Fundamental Form and the Metric Tensor, Normal and Geodesic Curvatures, Gauss's Formulae, Christoffel Symbols of First and Second Kinds, Parallel Vector Fields Along a Curve and Parallelism, The Second Fundamental Form and the Weingarten Map, Principal, Gaussian, Mean and Normal Curvatures, Dupin Indicatrices, Conjugate and Asymptotic Directions, Isometries and the Fundamental Theorem of Surfaces

Text and Reference Books

1. M. P. Do Carmo, *Differential Geometry of Curves and Surfaces*, Prentice Hall, 1976.
2. A. Goetz, *Introduction to Differential Geometry*, Addison Wesley, 1970.
3. R. S. Millman and G. D. Parker, *Elements of Differential Geometry*, Prentice Hall, 1977.
4. A. N. Pressley, *Elementary differential geometry*, 2nd Edition, Springer-Verlag, 2012.
5. D. J. Struik, *Lectures on Classical Differential Geometry*, Addison Wesley, Massachusetts, 1977.

Course Code: MAT-5104

Title: Analytical Mechanics

Credit Hrs: 03

Course Outline: Kinematics of Particles, Motion in Resisting Medium, Variable Mass Problem, Euler's Theorem and Chasles' theorem, **Moving Coordinate System:** Motion Relative to the Rotating Earth, **The Motion of a System of Particles:** Work, Power, Energy, center of mass, Generalized Coordinates, Lagrange's and Hamilton's Equations, Hamiltonian Principle, Simple Applications, Properties of a Rigid Body, Motion under No Forces, **Motion of Rigid Bodies in Three Dimensions:** General motion of rigid bodies in space. The momental ellipsoid and equimomental systems. Angular momentum vector and rotational kinetic energy. Principal axes and principal moments of inertia. Determination of 16 principal axes by diagonalizing the inertia matrix. **Euler Equations of Motion of a Rigid Body:** Force free motion. Free rotation of a rigid body with an axis of symmetry. Free rotation of a rigid body with three different principal moments. The Eulerian angles, angular velocity and kinetic energy in terms of Euler angles. Motion of a spinning top and gyroscopes-steady precession, sleeping top.

Text and Reference Books

1. G. R Fowles, G.L. Cassiday, *Analytical Mechanics*, 7th Edition, Thomson Brook Cole, 2005.
2. B. Jafferson, T. Beadsworth, *Further Mechanics*, Oxford University Press, 2001.
3. Louis N. Hand, *Analytical Mechanics*, 1st Edition, Cambridge University Press, 1998.
4. Dr. C. Helrich, *Analytical Mechanics*, 1st Edition, Springer, 2016.
5. J. S. Torook, *Analytical Mechanics*, 1st Edition, Wiley-Interscience, 1999.

Course Code: MAT-5105

Title: Topology

Credit Hrs: 03

Course Outline: Overview of Metric Spaces, Convergence, and Continuity in Metric Spaces, Topological Spaces, Sub-Spaces, Closed Sets, Closures and Interiors of Sets, Boundary of a Set, Limit Point, Bases and Sub-bases, Neighborhood Base, First and Second Countable Spaces, Continuous Functions and Homeomorphism, Product Topology

T_0 , T_1 , T_2 Spaces and Their Characterizations and Basic Properties, Regular and Completely Regular Spaces, Normal and Completely Normal Spaces

Compact / Countable Spaces and Their Properties, Connected Spaces

Text and Reference Books

1. C. W. Patty, *Foundation of Topology*, 2nd Edition, The Jones and Bartlett Publishers, 2009.
2. J. Dugundji, *Topology*, W.M. C. Brown Publisher, 1990.
3. J. R. Munkres, *Topology: A First Course in Topology*, 2nd Edition, Prentice Hall Inc., New Jersey, 2005.
4. G. F. Simmons, *Introduction to Topology and Modern Analysis*, Tata Mc-Graw Hill, 1963.
5. Munkres, *Topology*, 2nd Edition, Pearson India, 2015.

Course Code: MAT-5106

Title: Abstract Algebra

Credit Hrs: 03

Course Outline: Sets and Structures, Basic Axioms and Order of a Group, Subgroups, Subgroups Generated by Subset of a Group, System of Generators, Cyclic Group, Cosets, Lagrange's Theorem, Permutations, Even and Odd Permutations, Cycles, Lengths of Cycles, Transpositions, Symmetric and Alternating Group, Normalizers and Centralizers of a Subset of a Group, Centre of a Group, Normal Subgroup, Quotient Groups, Conjugacy Relation between Elements and Subgroups, Homomorphism and Isomorphism between Groups, Homomorphism and Isomorphism Theorems,

Text and Reference Books

1. J. B. Fraleigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. I. N. Herstein, *Topics in Algebra*, 2nd Edition, John-Wiley & Sons, 1975.
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. D.S. Dummit and R. M. Foote, *Abstract Algebra*, 3rd Edition, Wiley, 2003.
5. J. A. Gallian, *Contemporary abstract algebra*, D.C. Heath, 1986.

Semester-II

Course Code: MAT-5201

Title: Real Analysis-II

Credit Hrs: 03

Course Outline: The Riemann-Stieltjes Integrals: Definition and existence of integrals. Properties of integrals. Fundamental theorem of calculus and its applications. Change of variable theorem. Integration by parts. **Functions of Bounded Variation:** Definition and examples. Properties of functions of bounded variation. **Improper Integrals:** Types of improper integrals, tests for convergence of improper integrals. Beta and gamma functions. Absolute and conditional convergence of improper integrals. **Sequences and Series of Functions:** Power series, definition of point-wise and uniform convergence. Uniform convergence and continuity. Uniform convergence and differentiation. Examples of uniform convergence.

Text and Reference Books

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Mathematical Analysis*, Mc-Graw Hill, New York, 1987.
3. T. M. Apostol, *Mathematical Analysis*, 6th Edition, Addison Wesley, 1982.
4. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3rd Edition, John Wiley and Sons, 1999
5. S. Lang, *Real Analysis*, Springer-Verlag, London, 1987.

Course Code: MAT-5202

Title: Partial Differential Equations

Credit Hrs: 03

Course Outline: Review of ODEs in More than One Variable, **First order PDEs:** Introduction, formation of PDEs, solutions of PDEs of first order, The Cauchy's problem for quasilinear first order PDEs, First order nonlinear equations, Special types of first order equations, **Second order PDEs:** Basic concepts and definitions, Mathematical problems, Linear operators, Superposition, Mathematical models: The classical equations, the vibrating string, the vibrating membrane, conduction of heat solids, canonical forms and variable, PDEs of second order in two independent variables with constant and variable coefficients, Cauchy's problem for second order PDEs in two independent variables

Methods of separation of variables and Green's Functions: Solutions of elliptic, parabolic and hyperbolic PDEs in Cartesian and cylindrical coordinates

Text and Reference Books

1. P. Duhaure and D. Zachmann, *Partial Differential Equations*, Mc-Graw Hill, 1986.
2. J. Fritz, *Partial Differential Equations*, Spriger-Verlag, New York, 1979.
3. R. Haberman, *Elementary Applied Partial Differential Equations* Prentice Hall Inc., 1983.
4. M. Humi and W.B. Miller, *Boundary Value Problems and Partial Differential Equations*, PWS-Kent Publishing Company, Bostan, 1992.
5. J. Kevorkean, *Partial Differential Equations: Analytical Solution Techniques (Texts in Applied Mathematics)*, 2nd Edition, 1839.

Course Code: MAT-5203

Title: Numerical Methods I

Credit Hrs: 03

Course Outline: Computer Arithmetic, Approximations and Errors; Methods for the Solution of Non-Linear Equations and Their Convergence: Bisection Method, Regula-Falsi, Fixed Point Iteration, Newton-Raphson, Secant and Householder's Method, Error Analysis for Iterative Methods Interpolation and Polynomial Approximation: Lagrange Interpolation, Newton's Divided Difference, Forward-Difference and Backward-Difference Formulae, Hermite Interpolation, Numerical Integration and Error Estimates: Rectangular Rule, Trapezoidal Rule, Simpson's One-Three and Three-Eight Rules

Numerical Solution of Systems of Algebraic Linear Equations: Gauss-Elimination Method, Gauss-Jordan Method, Matrix Inversion, LU-Factorization, Doolittle's, Crout's, Cholesky's Methods, Gauss-Seidel and Jacobi Methods, Matrix Norms, Method of Least Squares, Eigenvalues and Eigenvectors: Power Method

Text and Reference Books

1. K.E. Atkinson, *An Introduction to Numerical Analysis*, 2nd Edition, John Wiley and Sons, New York, 1989.
2. R.L. Burden and J.D. Faires, *Numerical Analysis*, 5th Edition, PWS Publishing Company, 1993.
3. S.C. Chapra and R.P. Canale, *Numerical Methods for Engineers*, Mc-Graw Hill, New York, 1988.
4. A. Greenbaum and T. P. Chartier, *Numerical Methods*, 2012 Edition, Princeton University Press, 2012.
5. J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.

Course Code: MAT-5204

Title: Complex Analysis

Credit Hrs: 03

Course Outline: The Algebra and the Geometry of Complex Numbers, Complex Functions, Parametric Curves in the Complex Plane, Linear Mappings, Special Power Functions, Reciprocal Functions, Limit and Continuity, Complex Functions as Vector Fields, Derivative, Analytic Functions, Cauchy-Riemann Equations, Complex Exponential, Logarithmic, Trigonometric, Hyperbolic Functions and Their Derivatives, Harmonic Functions, Contour Integrals, the Cauchy-Goursat Theorem, Cauchy Integral Formulas, the Morera Theorem, Maximum Modulus Principle, The Liouville Theorem, Fundamental Theorem of Algebra, Convergence of Sequences and Series, The Taylor and the Laurent Series, Uniqueness of Representation, Zeros of Analytic Functions Residues, Poles and the Residue Theorem, Evaluation of Improper Integrals, Integrals Around a Branch Point, The Argument Principle and the Rouché's Theorem

Text and Reference Books

1. R.V. Churchill and J.W. Brown, *Complex Variables and Applications*, 5th Edition, Mc-Graw Hill, New York, 1989.
2. E. Hille, *Analytic Function Theory*, Vol. I and II, Chelsea Publishing Company, New York, 1974.
3. J. E. Marsden, *Basic Complex Analysis*, W. H. Freeman and Company, 1982.
4. D. G. Zill, and P. D. Shanahan, *A First Course in Complex Analysis with Applications*, Jones and Bartlet Publishers, Sudbury, Massachusetts, 2008.
5. L. V. Ahlfors, *Complex Analysis*, 3rd Edition, McGraw Hill Education (India) Private Limited, 2013.

Course Code: MAT-5205

Title: Tensor Analysis

Credit Hrs: 02

Course Outline Introduction to general tensors, Summation Convention, Kronecker Delta, Levi-Civita Symbol, Vectors as Quantities Transforming Under Rotations with Notation, The Spherical-Polar and the Cylindrical-Coordinate Meshes, Alternating Symbol, Relation between Alternating Symbol and Kronecker Delta, Tensors of First, Second and Higher Orders, Algebra of Tensors, Contraction of Tensor, Quotient Theorem, Symmetric and Skew-Symmetric Tensors, Invariance Property, Isotropic Tensors, Differentiation of Tensors, Application of Tensors in Modeling Anisotropic Systems, Study of Physical Tensors, Diagonalization of Inertia Tensor as Aligning Coordinate Frame with Natural Symmetries of the System

Text and Reference Books

1. D.E. Bourne and P.C. Kendall, *Vector Analysis and Cartesian Tensors*, 2nd Edition, T. Nelson, 1977.
2. G. E. Hay, *Vector and Tensor Analysis*, Dover Publications, Inc., New York, 1979.
3. G. D. Smith, *Vector Analysis*, Oxford University Press, Oxford, 1962.
4. I. S. Sokolnikoff, *Tensor Analysis: Theory and Application*, John Wiley and Sons, 1951.
5. M. R. Spiegel, *Vector Analysis*, Mc-Graw Hill, New York, 1974.

Course Code: MAT-5206

Title: Scientific Programming

Credit Hrs: 2+1

Course Outline (MATLAB, Maple, Mathematica): A list of contents is given below. However the instructor may add or remove some of the contents depending on the need of the students.

Curve sketching (only graphs of functions of one variable in Cartesian Coordinates) by using standard procedure, Intro to MATLAB (history, installation, interface, using product help, etc), MATLAB vs Maths syntax, sketching plane curves and surfaces in MATLAB, use of MATLAB in linear algebra, symbolic computations using MATLAB, creating script and function m-files, MATLAB codes for Bisection, Newton-Raphson, secant, Regula-Falsi, Jacobi, GS, Euler, and RK-4 methods. A brief introduction to Maple/Mathematica, comparison between similar features of MATLAB and Maple/Mathematica.

The following points are important for teaching this course:

1. The course should be taught in a computer lab setting
2. At the completion of this course, the students must be able to utilize the software to solve computationally difficult problems
3. The students should have a good command on at least two of the three programs mentioned above

Text and Reference Books

1. D. M. Etter, D. Kuncicky and D. Hull, *Introduction to Matlab-6*, Prentice Hall, 2001.
2. F. Garvan, *The Maple Book*, Chapman and Hall/CRC, 2002.
3. S. Kaufmann, *Mathematica as a Tool: An Introduction with Practical Examples*, Springer-Verlag, 1994.
4. A. Gilat, *MATLAB: An Introduction with Applications*, 5th Edition, Wiley, 2014.
5. L. Nichal, *Maple*, 1st Edition, Nancy Paulsen Books, 2014.

Semester-III

Course Code: MAT-6301

Title: Measure Theory

Credit Hrs: 03

Course Outline: Definition and Examples of Algebra and σ -Algebra, Basic Properties of Measurable Spaces, Definition and Examples of Measure Spaces, Outer Measure, Lebesgue Measure, Measurable Sets, Complete Measure Spaces

Measurable Functions: Some Equivalent Formulations of Measurable Functions, Examples of Measurable Functions, Various Characterizations of Measurable Functions, Properties that Hold Almost Everywhere

Definition of Lebesgue Integral, Basic Properties of Lebesgue Integrals, Comparison between Riemann Integration and Lebesgue Integration, L_2 -Spaces

Text and Reference Books

1. D. L. Cohn, *Measure Theory*, Birkhauser, 1980.
2. P. R. Halmos, *Measure Theory*, D. Van Nostrand, 1950.
3. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
4. T. Tao, *An Introduction to Measure Theory*, American Mathematical Society, 2011.
5. P. R. Halmos, *Measure Theory*, 2nd Edition, Springer, 1978.

Course Code: MAT-6302

Title: Mathematical Physics

Credit Hrs: 03

Course Outline: Definition and Properties of Laplace and Inverse Laplace Transforms, s-shifting property of LT, existence and uniqueness theorem, LT of derivatives and integrals and solution of ivps, unite step function and t-shifting property of LT, solution of circuit problems by using LT, Dirac Delta Function and its properties, LT of periodic functions, Convolution Theorem, Convolution of discontinuous functions, solution of integral equations by LT, differentiation and integration of LT, Laguerre's equation and polynomials, Applications of Laplace Transforms to systems of ODEs and PDEs, Fourier Series of 2π and $2L$ periodic functions, Convergence and sum of FS, even and odd functions and half-range expansions of FS, solution of odes and pdes by using FS, Fourier Integrals, Fourier Sine and Cosine integrals, Fourier sine and cosine transforms, Fourier sine and cosine transforms of derivatives, existence of FT, FT of derivatives, Convolution theorem, Discrete and Fast Fourier Transforms, solution of odes and pdes by using FT.

Text and Reference Books

1. E. Kreyszig, *Advanced Engineering Mathematics*, 10th Edition, Wiley, 2011.
2. E. L. Butkov, *Mathematical Physics*, Addison Wesley, 1973.
3. R. P. Kanwal, *Linear Integral Equations*, Academic Press, 1971.
4. T. Myint-U and L. Denbnath, *Partial Differential Equations*, Elsevier Science Publishing, 1987.
5. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Vol. II, Mc-Millan Publishing Company, Inc., New York, 1968.

Course Code: MAT-6303

Title: Numerical Methods-II

Credit Hrs: 03

Course Outline: IVP for ODEs: Elementary theory of ivps, Introduction to Single-Step Numerical Methods for solution of ivps, Picard's method, Euler's Method, Second and higher order Taylor's methods, RK-methods (mid-point, modified Euler, Heun's, and RK-4 methods), Multi-Step methods for numerical solutions of odes (2-, 3-, 4-, and 5-step Adam-Bashforth and Adam-Moulton methods), Extension of Euler and RK-4 methods for numerical solutions of higher order odes and system of first order odes, stability, consistency, and convergence of SS and MS methods, stiff odes, region of absolute stability and A-Stability, BVPs for odes: Discussion on Problem Behavior and Stability, Shooting method and finite difference methods for Linear and Nonlinear BVPs, Rayleigh-Ritz method for Linear and Non-Linear BVPs.

Text and Reference Books

- 1 U. Ascher and L. Petzold, *Computer Methods for ODEs and DAEs*, SIAM, 1998.
- 2 R. L. Burden and J.D. Faires, *Numerical Analysis*, 5th Edition, PWS Publishing Company, 1993.
- 3 U. Ascher, R. Matteij and R. Russell, *Numerical Solution of BVPs for ODEs*, Prentice Hall, 1988.
- 4 J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.
- 5 A. Greenbaum and T. P. Chartier, *Numerical Methods*, 2012 Edition, Princeton University Press, 2012.

Course Code: MAT-6304

Title: Functional Analysis

Credit Hrs: 03

Course Outline: Definition and Examples of Normed Spaces, Banach Spaces, Characterization of Banach Spaces, Bounded Linear Transformations, Bounded Linear Operators, Functional and Their Examples, Various Characterization of Bounded (Continuous) Linear Operator, The Space of All Bounded Linear Operators, The Open Mapping and Closed Graph Theorems, The Dual (Conjugate) Spaces, Reflexive Spaces, Hahn-Banach Theorem (Without Proof), Some Important Consequences of the Hahn- Banach Theorem. Inner Product Spaces, Hilbert Spaces, Orthonormal Bases, Convexity in Hilbert Spaces, Operators in Hilbert Spaces, Invariant Sub-Spaces, Decomposition of Hilbert Spaces, Finite Dimensional Spectral Theory and Spectral Mapping Theorem.

Text and Reference Books

1. E. Kreyszig, *Introductory Fundamental Analysis with Applications*, John Wiley and Sons, 2007.
2. I. J. Maddox, *Elements of Functional Analysis*, Cambridge University Press, 1988.
3. W. Rudin, *Functional Analysis*, Mc-Graw Hill, 2016.
4. G. F. Simmon, *Introduction to Topology and Modern Analysis*, Mc-Graw Hill, New York, 2004.
5. A. Majeed, *Elements of Topology and Functional Analysis*, Ilmi Kitab Khana, 2014.

Course Code: MAT-6305

Title: Fluid Mechanics-I

Credit Hrs: 03

Course Outline: Fields and Continuum Concepts, Lagrangian and Eulerian Specifications, Local, Convective and Total Rates of Change, Conservation of Mass, Equation of Continuity, Boundary Conditions, Nature of Force in a Fluid Field and Their Effects: Surface and Body Forces, Stress at a Point, Viscosity and Newton's Viscosity Law, Viscous and Inviscid Flows, Laminar and Turbulent Flows, Compressible and Incompressible Flows

Irrotational Fluid Motion: Velocity Potential from an Irrotational Velocity Field, Streamlines. Vortex Lines and Vortex Sheets, Kelvin's Minimum Energy Theorem, Conservation of Linear Momentum, Bernoulli's Theorem and Its Applications, Circulations, Rate of Change of Circulation (Kelvin's Theorem), Axially Symmetric Motion, Stokes Stream Function

Two-Dimensional Motion: Stream Function, Complex Potential and Complex Velocity, Uniform Flows, Sources, Sinks and Vortex Flows, Flow in a Sector, Flow Around a Sharp Edge, Flow Due to a Doublet

Text and Reference Books

1. I. G. Curie, *Fundamentals of Mechanics of Fluids*, 3rd Edition, CRC, 2002.
2. I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
3. R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
4. H. Schlichting, K. Gersten, E. Krause and H. Oertel, Jr, *Boundary-Layer Theory*, 8th Edition, Springer-Verlag, 2004.
5. Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

Course Code: MAT-6306

Title: Operation Research

Credit Hrs: 03

Course Outline: Introduction to Operation Research and Real Life Phases, Introduction to Linear Programming (LP) with Examples, Graphical Solutions to Mathematical Model with Special Cases, Simplex Algorithm and its Different Cases, Big M Method and Two Phase Method, Scheduling and Blending Problems, The Transportation Problems, The Transshipment Problems, The Assignment Problems, Integer Programming, Network Models, Inventory Models

Text and Reference Books

1. Hillier and Lieberman, *Introduction to Operations Research*, 9th Edition, Mc-Graw Hill, 2010.
2. P. R. Murthy, *Operations Research*, New Age International (P) Limited Publishers, New Delhi, 2007.
3. Taha and Hamdy, *Operations Research*, 7th Edition, Mc-Millan Publishing Company, Inc., New York, 2003.
4. W. L. Winston, *Practical Management Science: Spreadsheet Modeling and Applications*.
5. F. S. Hillier and G. J. Liberman, *Operations Research*, 9th Edition, McGraw-Hill Science/Engineering/Math, 2009.

Course Code: MAT-6307

Title: Number Theory

Credit Hrs: 03

Course Outline: Divisibility, Euclidean Algorithm, GCD and LCM of two Integers, Properties of Prime Numbers, Fundamental Theorem of Arithmetic (UFT), Congruence Relation, Residue System, Euler's Phi-Function, Solution of System of Linear Congruence, Congruences of Higher Degree, Chinese Remainder Theorem, Fermat's Little Theorem, Wilson's Theorem and Applications, Primitive Roots and Indices, Integers Belonging to a Given Exponent (mod p), Primitive Roots of Prime and Composite Moduli, Indices

Text and Reference Books

1. G. A. Jones and J. M. Jones, *Elementary Number Theory*, Springer-Varlog, London Limited, 1998.
2. M. B. Nathanson, *Methods in Number Theory*, Springer-Verlag, New York, 2000.
3. A. N. Parshin and I.R. Shafarevich, *Number Theory-I, Fundamental Problems, Ideas and Theories*, Springer-Verlag, Berlin Heidelberg, 1995.
4. K. H. E. Rosen, *Elementary Number theory and its Applications*, 4th Edition, Addison Wesley, Reading, Ma, USA, 2000.
5. T. Andreesco and D. Andrica, *Number theory*, 2009 Edition, Birkhauser, 2009.

Course Code: MAT-6308

Title: Mathematical Statistics

Credit Hrs: 03

Course Outline: Set and Algebra of sets, Some elementary theorems of probability, Addition and multiplication rules, Baye's rule and future Baye's theorem, Random variables, probability functions, Cumulative distribution Function, Discrete and Continuous probability distribution, Moments and moment generating functions, Moments of binomial, hypergeometric, Poisson, gamma, beta and normal distributions and their characterizations. Joint probability functions and their properties, Bivariate Normal distribution, Transformation; Distribution function technique, Transformation technique: One variable, several variables, Moment-generating function technique, Sampling distributions and their properties, Regression and Correlation, Linear regression, The methods of least squares, Normal regression analysis, Normal correlation analysis, Multiple linear regression, Multiple linear regression (matrix notation)

Text and Reference Books

1. M. H. De-Groot and M. J. Schervish, *Probability and Statistics*, 3rd Edition, Addison Wesley, 2002.
2. A. Papoulis, *Probability, Random Variables, and Stochastic Processes*, 3rd Edition, Mc-Graw Hill, 1991.
3. T. Sincich, *Statistics by Examples*, Dellen Publishing Company, 1990.
4. A. S. Hirahi, *A Course in Mathematical Statistics*, 4th Edition, Ilmi Kitab Khana, Lahore, Pakistan, 2012.
5. I. Miller and M. Miller, *Mathematical Statistics with Applications*, 8th Edition, Pearson, 2012.

Course Code: MAT-6309

Title: Quantum Mechanics-I

Credit Hrs: 03

Course Outline: Black Body Radiation, Photoelectric Effect, Compton Effect, Bohr's Theory of Atomic Structure, Wave-Particle Duality, The De Broglie Postulate, Heisenberg Uncertainty Principle, The Postulates of Quantum Mechanics, Operators, Eigen-functions and Eigenvalues: Observables and Operators. Measurement in Quantum Mechanics, The State Function and Expectation Values Time, Development of the Stat Function (Schrodinger Wave Equation), Solution to the Initial-Value Problem in Quantum Mechanics, Parity Operators
Function Spaces and Hermitian Operators: Particle in a Box, Dirac Notation, Hilbert Space. Hermitian Operators, Properties of Hermitian Operators, Additional One-Dimensional Problems: Bound and Unbound States: General Properties of the One Dimensional Schrodinger Equation, Unbound States, One-Dimensional Barrier Problems, The Rectangular Barrier, Tunnel.

Text and Reference Books

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2004.
2. H. D. Dehmen, *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics: A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Co., 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

Course Code: MAT-6310

Title: Ring Theory

Credit Hrs: 03

Course Outline:

Rings: Definition, examples. Quadratic integer rings. Examples of non-commutative rings. The Hamilton quaternions. Polynomial rings. Matrix rings. Units, zero-divisors, nilpotents, idempotents. Subrings, Ideals. Maximal and prime Ideals. Left, right and two-sided ideals;

Operations with ideals. The ideal generated by a set. Quotient rings. Ring homomorphism. The isomorphism theorems, applications. Finitely generated ideals. Rings of fractions.

Integral Domain: The Chinese remainder theorem. Divisibility in integral domains, greatest common divisor, least common multiple. Euclidean domains. The Euclidean algorithm. Principal ideal domains. Prime and irreducible elements in an integral domain. Gauss lemma, irreducibility criteria for polynomials. Unique factorization domains. Finite fields. Polynomials in several variables. Symmetric polynomials. The fundamental theorem of symmetric polynomials.

Text and Reference Books

1. J. B. Fraieigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. B. Hartley and T. O. Hawkes, *Ring, Modules and Linear Algebra*, Chapman and Hall, 1980.
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. S. J. Leon, *Linear Algebra with Applications*, 6th Edition, Prentice Hall, 2002.
5. P. M. Cohn, *Introduction to Ring Theory*, 1st Edition, Springer, 2002.

Course Code: MAT-6311

Title: Analytical Dynamics

Credit Hrs: 03

Course Outline: Constraints, Generalized Coordinates, Generalized Forces, General Equation of Dynamics, Lagrange's Equations, Conservation Laws, Ignorable Coordinates, Explicit Form of Lagrange's Equation in Terms of Tensors. Hamilton's Principle of Least Action, Hamilton's Equations of Motion, Hamilton-Jacobi Method, Poisson Brackets (P.B's); Poisson's Theorem; Solution of Mechanical Problems by Algebraic Technique Based on (P.B's) Small Oscillations and Normal Modes, Vibrations of Strings, Transverse Vibrations Normal Modes, Forced Vibrations and Damping, Reflection and Transmission at a Discontinuity, Longitudinal Vibrations, Rayleigh's Principle

Text and Reference Books

1. F. Chorlton, *Textbook of Dynamics*, Van Nostrand, 1963.
2. W. Chester, *Mechanics*, George Allen and Unwin Ltd. London, 1979.
3. H. Goldstein, *Classical Mechanics*, Cambridge University Press, 1980.
4. G. Meirovitch, *Methods of Analytical Dynamics*, Mc-Graw Hill, 1970.
5. H. Baruh, *Analytical Dynamics*, 1st Edition, WCB/McGraw-Hill, 1998.

MAT-6312

Introduction to Difference Equations

Credit Hrs: 3

Course Outlines: First, second and higher order differences, Some properties of operators E and Δ ,

Equivalence of operators, Infinite Summations, The operator Δ^{-1} , Analogies between the Difference and Differential calculus, Generating functions and approximate summation, Difference equations, Linear and nonlinear difference equations, Homogenous and Non-homogenous difference equations, solutions of a Difference Equations, An existence and Uniqueness Theorem, Sequences, Solutions as sequences, Simple and Compound interest, Inventory Analysis, Approximating a Differential equations by a Difference equations, General results for linear Difference Equations, Applications, Linear Difference Equations with constant coefficients, Fundamental set of solutions, General solution of Homogenous equations, Particular solutions of complete difference equations, Limiting behavior of solutions, Examples from Social Sciences, General case of order n , Difference equation with variable coefficients, Linearizable Nonlinear difference equations, Methods for solving Difference Equations, Equilibrium and stability of Solutions, First-order Equations and Cobweb Cycles, A Characteristic-Value Problem.

Recommended Books:

1. S. Goldberg, *Introduction to Difference Equations*, John Wiley & Sons, Inc. New York. London, 1958.
2. W. G. Kelley, A. C. Peterson, *Difference Equations: An Introduction with Applications*, Academic Press, USA, 2001.
3. Ronald E Micken, *Difference equations theory applications and advanced topics*, third edition, 2015.
4. S. Elydi, *Introduction to Difference Equations*, 3rd edition, Springer, 2005.
5. W. G. Kelly and A. C. Peterson, *Difference Equation : An Introduction with Applications*, 2nd edition, Academic Press, 2000.

Course Code: MAT-6313

Title: Differential Geometry-II

Credit Hrs: 03

Course Outline: Definition and Examples of Manifolds, Differential Maps, Sub-Manifolds, Tangents, Coordinate Vector Fields, Tangent Spaces, Dual Spaces, Multi-Linear Functions, Algebra of Tensors, Vector Fields, Tensor Fields, Integral Curves, Flows, Lie Derivatives, Brackets, Differential Forms, Introduction to Integration Theory on Manifolds, Riemannian and Semi-Riemannian Metrics, Flat Spaces, Affine Connections, Parallel Translations, Covariant Differentiation of Tensor Fields, Curvature and Torsion Tensors, Connection of a Semi-Riemannian Tensor, Killing Equations and Killing Vector Fields, Geodesics, Sectional Curvature

Text and Reference Books

1. R. Abraham, J. E. Marsden and T. Ratiu, *Manifolds, Tensor Analysis and Applications*, Addison Wesley, 1983.
2. R. L. Bishop and S. I. Goldberg, *Tensor Analysis on Manifolds*, Dover Publications, Inc., New York, 1980.
3. M. P. Do Carmo, *Riemannian Geometry*, Birkhauser, 1992.
4. D. Langwitz, *Differential and Riemannian Geometry*, Academic Press, 1970.
5. D. Lovelock and H. Rund, *Differential Forms and Variational Principles*, John Wiley and Sons, 1975.

Course Code: MAT-6314

Title: Electromagnetic Theory-I

Credit Hrs: 03

Course Outline: Electromagnetic Fields, Coulomb's Law, The Electric Field Intensity and Potential, Gauss's Law and Deductions, Piosson and Laplace Equations, Conductors and Condensers, Dipoles, The Linear Quadrupole, Potential Energy of a Charge Distribution, Dielectrics, The Polarization and Displacement Vectors, General Solutions of Laplace's Equation. Solutions of Laplace's Equation in Spherical Coordinates, Legendre's Equation, Legendre's Polynomials, Electromagnetic Fields, The Magnetostatic Law of Force, The Magnetic Induction, The Lorentz Force on a Point Charge Moving in a Magnetic Field, The Divergence of the Magnetic Field, The Vector Potential, The Conservation of Charge and Equation of Continuity, The Lorentz Condition, The Curl of The Magnetic Field, Ampere's Law and the scalar Potential, Steady and Slowly Varying Currents, Electric Current, Linear Conductors. Conductivity, Resistance, Kirchhoff's Laws, Current Density Vector, Magnetic Field of Straight and Circular Current, Magnetic Flux, Vector Potential, Forces on a Circuit in Magnetic Field

Text and Reference Books

1. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
2. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
3. G. E. Owen, *Introduction to Electromagnetic Theory*, Dover, 2003.
4. J. R. Reitz, F. J. Milford and R. W. Christy, *Foundations, of Electromagnetic Theory*, Addison-Wesley Publishing Co., 1993.
5. J. V. Stewart, *Intermediate Electromagnetic Theory*, World Scientific, 2001.

Course Code: MAT-6315

Title: Conference/Seminar/Reading-I

Credit Hrs: S/U

Course Outline: The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also be trained on preparing papers and presentations for conferences and seminars.

Text and Reference Books

As per requirement of the students taking the course

Course Code: MAT-6316

Title: Project

Credit Hrs: 3+3

Course Outline:

The objective of this course is to train students to learn and use the tools required for writing their project report and the tools for doing their research work. They will do the literature survey, work on some research problem and write a project report by the end of the 4th semester.

Text and Reference Books

As per requirements of the topic of the project.

Semester-IV

Course Code: MAT-6401

Title: Mathematical Systems Theory

Credit Hrs: 03

Course Outline: Conservation laws and phenomenological principles, some principles and laws of thermodynamics, mechanics, and electromagnetism and their applications in modelling, Linearization, matrix exponentials and solution of linear differential equations, LTV systems, Impulse and step responses,

Stability, controllability, and observability of LTI systems, Realization theory and Hankel matrices, Feedback and stabilizability, observers and state reconstruction, detectability, separation principle and compensation, disturbance rejection,

Laplace transforms and LTI systems, transfer functions and transfer matrices, transfer functions and minimal realizations of SISO and MIMO systems,

Text and Reference Books

1. G. J. Olsder, J. W. van der Woude, J. G. Mask, and D. Jeltsema, *Mathematical Systems Theory*, 4th Edition, VSSD, 2011.
2. I. D. Hinrichsen and A. J. Pritchard, *Mathematical Systems Theory*, Springer, 2012.
3. J. W. Polderman and J. C. Willems, *Introduction to Mathematical Systems Theory*, 2nd Edition, Springer, 2008.
4. J. Zabczyk, *Mathematical Control Theory*, 1st Edition, Birkhauser, 2007.
5. E. D. Sontag, *Mathematical Control Theory*, 2nd Edition, Springer, 1998.

Course Code: MAT-6402

Title: Mathematical Modeling

Credit Hrs: 03

Course Outline: Introduction to modeling. Basic Guide line of mathematical modeling, Collection and interpretation of data, Technique of mathematical modeling, Classification of mathematical modeling, modeling through algebra, modeling through Geometry, modeling through Trigonometry, modeling through Calculus, Limitation of modeling, Development of Models', , Discrete and Continuous models,, Linear Growth and Decay Model, Non-linear Growth and decay models, Mathematical modeling in population dynamic, Traffic flow models.

Text and Reference Books

1. Banerjee, *Mathematical modeling (Modell analysis and Application)*
2. J. J. Batzel, M. Bachar, and F. Kappel, *Mathematical Modeling and Validation in Physiology*, 2013
3. D. Edwards and M. Hamson, *Mathematical modeling Skills*, MacMillan Press Ltd., 1996
4. F. R. Giordano, M. D. Weir, and W. P. Fox, *A First Course in Mathematical modeling*, Thomson Brooks/Cole, 2003
5. J. N. Kapur, *Mathematical modeling*, New Age International Limited, 2015.

Course Code: MAT-6403

Title: Integral Equations

Credit Hrs: 03

Course Outline: Linear integral equations of the first and second kind. Relationship between differential equation and Volterra integral equation. Neumann series. Fredholm Integral equation of the second kind with separable Kernels. Eigenvalues and eigenvectors. Iterated functions. Quadrature methods. Least square methods. Homogeneous integral equations of the second kind. Fredholm integral equations of the first kind. Fredholm integral equations of the second kind. Abel's integral equations. Hilbert Schmidt theory of integral equations with symmetric Kernels. Regularization and filtering techniques, Introduction to Wiener-Hopf Technique.

Text and Reference Books

1. J. J. Abdul, *Introduction to Integral Equations with Applications*, Marcel Dekker Inc. New York, 1985.
2. V. Lovitt, *Linear Integral Equations*, Dover Publications, Inc., New York, 1950.
3. B. Noble, *Methods Based on the Wiener-Hopf Technique*, Pergamon Press, 1988
4. F. Smith, *Integral Equations*, Cambridge University Press, 2003.
5. F. G. Tricomi, *Integral Equations*, Interscience, 1957.

Course Code: MAT-6404

Title: Optimization Theory

Credit Hrs: 03

Course Outline: Introduction to optimisation. Relative and absolute extrema. Convex, concave and unimodal functions. Constraints. Mathematical programming problems. Optimisation of one, two and several variables functions and necessary and sufficient conditions for their optima. **Optimisation by equality constraints:** Direct substitution method and Lagrange multiplier method, necessary and sufficient conditions for an equality constrained optimum with bounded independent variables. Inequality constraints and Lagrange multipliers. Kuhn-Tucker Theorem. Multidimensional optimisation by Gradient method. Convex and concave programming. Calculus of variation and Euler Lagrange equations. Functionals depending on several independent variables. Variational problems in parametric form. Generalised mathematical formulation of dynamics programming. Non-linear continuous models. Dynamics programming and variational calculus. Control theory.

Text and Reference Books

1. L. Elsgolts, *DEs and the Calculus of Variations*, Mir Publishers Moscow, 1970.
2. B. S. Gotfried and J. Weisman, *Introduction to Optimization Theory*, Prentice Hall, NJ, USA, 1973.
3. D. G. Luenberger, *Introduction to Linear and Non-Linear Programming*, Addison Wesley, USA, 1973.
4. D. A. Wismer and R. Chattergy, *Introduction to Nonlinear Optimization*, North Holland, New York, 1978.
5. A. Beck, *Introduction to Nonlinear Optimization: Theory, Algorithms, and Applications with MATLAB*, SIAM-Society for Industrial and Applied Mathematics, 2014.

Course Code: MAT-6405

Title: Fluid Mechanics-II

Credit Hrs: 03

Course Outline: Circular Cylinder without Circulation, Circular Cylinder with Circulation Blasius Theorem, Kutta Condition and the Flat-Plate Airfoil, Joukowski Airfoil, Vortex Motion, Karman's Vortex Street, Method of Images, Velocity Potential, Stoke's Stream Function, Solution of the Potential Equation, Uniform Flow Source and Sink, Flow Due to A Doublet
Viscous Flows Of Incompressible Fluids: Constitutive Equations, Navier-Stokes's Equations, Exact Solutions of Navier-Stokes's Equations, Steady Unidirectional Flow, Poiseuille Flow, Coquette Flow, Flow between Rotating Cylinders, Stoke's First Problem, Stoke's Second Problem
Simplified Approach to Fluid Flow Problems: Similarity from Differential Equations, Dimensional Analysis, One Dimensional Steady Compressible Flow

Text and Reference Books

1. I. G. Curie of Fluids, *Fundamentals of Mechanics*, 3rd Edition, CRC, 2002.
2. I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
3. R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
4. H. Schlichting, K. Gersten, E. Krause and H. Oertel, Jr, *Boundary-Layer Theory*, 8th Edition, Springer-Verlag, 2004.
5. Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

Course Code: MAT-6406

Title: Algebraic Topology

Credit Hrs: 03

Course Outline: Path Wise Connectedness with Examples, Notion of Homotopy, Homotopy Classes and its Application, Path Homotopy, Path Homotopy Classes, Fundamental Groups, Covering Mapping with Examples, Covering Spaces, Lifting Properties of Covering Spaces and its Application, Fundamental Group of a Circle (s)

Text and Reference Books

1. M. J. Greeberge, *Algebraic Topology*, A first Course, Benjamin Commings, 1967.
2. C.A. Kosniowski, *First course in Algebraic Topology*, Cambridge University press, 1980.
3. A. H. Wallace, *Algebraic Topology*, Homology and Cohomology, Benjamin, 1968.
4. A. Hatcher, *Algebraic Topology*, 1st Edition, Cambridge University Press, 2001.
5. W. Fulton, *Algebraic Topology*, Springer, 1997.

Course Code: MAT-6404

Title: Special Functions

Credit Hrs: 03

Course Outline: Infinite Products: introduction, Definition of an infinite product, A necessary condition for convergence, Associated series of logarithms, Convergences types, The Gamma and Beta Functions: The Euler constant, The Gamma function, A series for logarithmic differential of Gamma function, The order symbols o and O , Evaluation of certain infinite products, The Beta Function, Factorial function, Asymptotic Series: Definition of an asymptotic expansion, Algebraic properties, Term by term integration, Uniqueness, The Hypergeometric function : Simple integral form, The function $F(a,b;c,z)$ and its properties, The Hypergeometric differential equation, Logarithmic solution of the hypergeometric function, $F(a,b;c,z)$ as a function of parameters, Elementary series manipulation, Kummer Theorem, Generalized Hypergeometric functions, the exponential and binomial functions, A differential equation, Saalschutz theorem, Contour integral integrals of Barnes' type, the Barnes integrals and the generalized hypergeometric function, Bessel Functions and its properties, The Confluent Hypergeometric functions and its properties, Generating Functions.

Text and Reference Books

1. E. D. Rainville, *Special Functions*, 1st Edition, The Macemillean Company New York, 1965.
2. L. J. Slater, and D. Lit, *Confluent Hypergeometric Functions*, Cambridge University Press, London, 1960.
3. A. Erdelyi, *Higher Transcendental Functions*, Volume I, II, & III, McGraw Hill Book Company Inc., 1953.
4. J. E. Andrews, R. Asky and R. Roy, *Special Functions*, 1st Edition, Cambridge University Press, 2001.
5. C. Viola, *Special Functions*, 1st Edition, Springer, 2016.

Course Code: MAT-6408

Title: Financial Mathematics

Credit Hrs: 03

Course Outline: First-order recurrences. The Cobweb model. Contours and isoquants. Optimisation in two variables. Vectors, preferences and convexity. Constrained optimization, elementary theory of the firm, Cobb-Douglas firm. Lagrangeans and the consumer, elementary theory of the consumer. Second-order recurrences, dynamics of economy, business cycles. Ordinary differential equations, continuous-time models, market trends and consumer demand.

Financial markets. Quantitative methods: binomial trees and arbitrage, spreadsheets to compute stocks and option trees. Continuous time models: Black-Scholes. Hedging. Bond models and interest rate options. Computational methods for bonds. Currency markets and foreign exchange risks.

Text and Reference Books

1. C. Ruckman, *Financial Mathematics*, 2nd edition, BPP Professional Education, 2005.
2. A. Solla, *Financial Mathematics*, 2015th edition, Create Space Independent Publishing Platform 2015.
3. K. J. Hastings, *Introduction to Financial Mathematics*, 1st edition, Chapman and Hall/CRC, 2015.
4. W. S. Chan, *Financial Mathematics for Actuaries*, 2nd edition, World Scientific Publishing Company, 2017.
5. G. Campolieti and R. N. Makarov, *Financial Mathematics*, 1st edition, Chapman and Hall/CRC, 2014.

Course Code: MAT-6409

Title: Quantum Mechanics-II

Credit Hrs: 03

Course Outline: Harmonic Oscillator and Problems in Three-Dimensions: The Harmonic Oscillator, Eigen-Functions of the Harmonic Oscillator, The Harmonic Oscillator in Momentum Space, Motion in Three Dimensions, Spherical Symmetric Potential and the Hydrogen Atom, Angular Momentum: Basic Properties, Eigenvalues of the Angular Momentum Operators, Eigen-Functions of the Orbital Angular Momentum Operators L_2 and L_z , Commutation Relations between Components of Angular Momentum and Their Representation in Spherical Polar Coordinates, The Scattering Cross-Section, Scattering Amplitude, Scattering Equation, Born Approximation, Partial Wave Analysis, Time Independent Perturbation of Non-Degenerate and Degenerate Cases, Time-Dependent Perturbations

Text and Reference Books

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2004.
2. H. D. Dehmen, *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics, A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Company, 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

Course Code: MAT-6410

Title: Introduction to Combinatorics

Credit Hrs: 03

Course Outline: Two Basic Counting Principle, Permutations, Combinations, The Injective and Bijective Principles, Arrangements and Selections with Repetitions, Graphs in Combinatorics, The Binomial Theorem, Combinatorial Identities, Properties of Binomial Coefficients, Multinomial Coefficients, The Multinomial Theorem, The Pigeonhole Principle, Examples, Ramsay Numbers, The Principle of Inclusion and Exclusion, Generalization, Integer Solutions, Surjective Mapping. Stirling Numbers of the Second Kind, The Sieve - Eratosthenes, Euler Φ -Function, The Problem Des-Menages Ordinary Generating Functions, Modeling Problems, Partition of Integers, Exponential Generating Functions

Linear Homogeneous Recurrence Relations, Algebraic Solutions of Linear Recurrence Relations and Constant Functions, The Method of Generating Functions, A Non-Linear Recurrence Relation and Catalaa Numbers

Text and Reference Books

1. V. K. Balakrishnan, *Theory and Problems of Combinatorics, Schaum's Outline Series, Mc-Graw Hill, Singapore, 1995.*
2. C. C. Chen and K. M. Koh, *Principles and Techniques in Combinatorics, World Scientific Publishing Company, Pvt. Ltd, Singapore, 1992.*
3. C. L. Liu, *Introduction to Combinatorial Mathematics, Mc-Graw Hill, New York, 1968.*
4. A. Tucker, *Applied Combinatorics, John Wiley and Sons, New York, 1985.*
5. R. A. Brualdi, *Introductory Combinatorics, 5th Edition, Pearson, 2009.*

Course Code: MAT-6411

Title: Dynamical Systems

Credit Hrs: 03

Course Outline: Introduction: Preliminary ideas, Autonomous equations, Autonomous systems in plane, Flows and evolution. Linear systems: Linear changes of variables, Similarity types for 2×2 real matrices, Phase portraits for canonical systems in the plane, Classification of simple linear phase portraits in the plane, The evolution operators, Affine systems, Linear systems of dimension greater than two. Nonlinear systems in the plane: Local and global behavior, Linearization at a fixed point, The linearization theorem, Non-simple fixed points, Stability of fixed points, Ordinary points and global behavior, First integrals, Limit points and limit cycles. Flows on non-planar phase spaces: Fixed points, Closed orbits, Attracting sets and attractors, Further integrals. Applications: Linear models, Affine models, Nonlinear models, Relaxation oscillation, Piecewise modeling. Dynamical systems with mathematica: Differential equations, Planar systems, Interacting species, Limit cycles.

Text and Reference Books

1. Lynch S., *Dynamical systems with applications using mathematica*, Birkhauser Boston 2007.
2. Alligood T. K., Sauer D. T., Yorke A. J., *Chaos: An introduction to dynamical systems*, Springer 1996.
3. R. C. Robinson, *An introduction to dynamical systems*, 1st edition, Prentice Hall, 2004.
4. Arrowsmith K. D., Place M. C., *Dynamical systems, differential equations, maps and chaotic behavior*, Chapman & Hall, 1992.
5. D. K. Arrowsmith and C. M. Place, *An introduction to dynamical systems*, Cambridge University Press, 1st edition, 1990.

Course Code: MAT-6412

Title: Theory of Elasticity

Credit Hrs: 03

Course Outline: Cartesian Tensors, Analysis of Stress and Strain, Generalized Hooke's Law, Crystalline Structure, Point Groups of Crystals, Reduction in the Number of Elastic Moduli Due to Crystal Symmetry, Equations of Equilibrium, Boundary Conditions, Compatibility Equation, Plane Stress and Plane Strain Problems, Two Dimensional Problem in Rectangular and Polar Coordinates, Torsion of Rods and Beams

Text and Reference Books

1. E. Dieulesaint and D. Royer, *Elastic Waves in Solids*, John Wiley and Sons, New York, 1980.
2. Y. C. Funk, *Foundations of Solid Mechanics*, Prentice-Hall, Englewood Cliffs, 1965.
3. Sokolnikoff, *Mathematical Theory of Elasticity*, Mc-Graw Hill, New York.
4. S. P. Temoshenko and J. N. Goodier, *Theory of Elasticity*, 3rd Edition, Mcgraw Hill Education (India), 2015.
5. A. I. Lurie and A. Belyaev, *Theory of Elasticity*, 2005 Edition, Springer, 2005.

Course Code: MAT-6413

Title: Special Theory of Relativity

Credit Hrs: 03

Course Outline: Historical Background and Fundamental Concepts of Special Theory of Relativity, Lorentz Transformations (for Motion Along One Axis), Length Contraction, Time Dilation and Simultaneity, Velocity Addition Formulae, 3-Dimensional Lorentz Transformation, Introduction to 4-Vector Formalism, Lorentz Transformations in the 4-Vector Formalism, The Lorentz and Poincare Groups, Introduction to Classical Mechanics, Minkowski Space-Time and Null Cone, 4-Velocity, 4-Momentum and 4-Force, Application of Special Relativity to Doppler Shift and Compton Effect, Particle Scattering, Binding Energy, Particle Production and Decay, Electromagnetism in Relativity, Electric Current, Maxwell's Equations and Electromagnetic Waves, The 4-Vector Formulation of Maxwell's Equations, Special Relativity with Small Acceleration

Text and Reference Books

1. H. Goldstein, *Classical Mechanics*, Addison Wesley, New York, 1962.
2. D. Inverno, *Introducing Einstein's Relativity*, Oxford University Press, 1992.
3. J. D. Jackson, *Classical Electrodynamics*, John Wiley and Sons, New York, 1962.
4. A. Qadir, *Relativity: An Introduction to the Special Theory*, World Scientific, 1989.
5. W. Rindler, *Essential Relativity*, Springer-Verlag, 1977.

Course Code: MAT-6414

Title: Electromagnetic Theory-II

Credit Hrs: 03

Course Outline: The Faraday Induction Law, Induced Electromotance in a Moving System, Inductance and Induced Electromotance, Energy Stored in a Magnetic Field, The Equations of Electromagnetism, Electromagnetic Waves: Plane Electromagnetic Waves in Free Space and Isotropic Media, The Poynting Vector in Free Space, Propagation of Electromagnetic Waves in NON-Conductors, Propagation of Plane Waves in Conducting Media, Reflection and Refraction of Plane Waves, Guided Waves, Coaxial Line, Hollow Rectangular Wave Guide, Radiation of Electromagnetic Waves, Electromagnetic Field of a Moving Charge

Text and Reference Books

1. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
2. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
3. G. E. Owen, *Introduction to Electromagnetic Theory*, Dover, 2003.
4. J. R. Reitz, F. J. Milford and R. W. Christy, *Foundations, of Electromagnetic Theory*, Addison-Wesley Publishing Co., 1993.
5. J. V. Stewart, *Intermediate Electromagnetic Theory*, World Scientific, 2001.

Course Code: MAT-6415

Title: Conference/Seminar/Reading-II

Credit Hrs: S/U

Course Outline: The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also be trained on preparing papers and presentations for conferences and seminars.

Text and Reference Books

As per requirement of the students taking the course.

Course Code: MAT-6416

Title: Comprehensive Oral Examination

Credit Hrs: S/U

Course Outline:

There will be a comprehensive oral examination at the end of the 4th semester. This examination will be conducted by an external examiner and 2 internal examiners together. Questions may be asked from any course which the student has studied during M.Sc.

3. Scheme of Studies for M.Phil in Mathematics: General Breakup

Content		Description	Remarks
3.1	Awarding Institute/Body	Mirpur University of Science and Technology (MUST)	
3.2	Teaching Institute	Department of Mathematics, Mirpur University of Science and Technology (MUST),	
3.3	Final Award	Master of Philosophy in Mathematics	
3.4	Program Title	M.Phil in Mathematics	
3.5	Starting Time for Program	Fall/Spring Semester	
3.6	Duration of the Program	4-8 Semesters	
3.7	Eligibility Criteria	BS or MSc or Equivelent Degree in Mathematics with CGPA 2.50 or above (for semester system degree) or 2 nd division (for annual system)	
		No D-grade in academic career	
		NTS/ GAT General Test with minimum cumulative score of 50%	
		Qualify Entry Test conducted by the University: 90 minutes duration, MCQs from BS/MSc mathematics syllabus	
3.8	Merit Formula	Merit formulas are the following: For M.Sc: 15% of Intermediate, 20% of B.Sc, 20% of M.Sc, 35% of Entry Test marks, and 10% of interview conducted by the department. For BS: 15% of Intermediate, 40% of BS, 35% of Entry Test marks, and 10% of interview conducted by the department.	
3.9	Total Credit Hours	Course Work: 24 Credit Hrs	
		Seminar: 1 Credit Hrs	
		Thesis (Compulsory): 6 Credit Hrs	

3.10 Program Educational Objectives:

After graduation, our students will be equipped not only with advanced mathematical tools but will also acquire skill set needed to apply mathematics towards engineering problems. Moreover, our graduates will be able to:

- i. Collaborate with engineers, scientists and other professionals from industry and academia on research/projects.
- ii. Promote the culture of interdisciplinary novel research and produce fundamental & applied quality research in Pakistan

- iii. Contribute through publishing fundamental research in the emerging areas of science and engineering, like, systems and control, computational fluid dynamics, mathematical modelling, and complex analysis etc.

3.12 Program Learning Outcomes (PLOs):

The curriculum for MPhil program is so designed that the students undertaking research in this department will have a chance to learn not only the fundamental courses of mathematics but also advanced courses related to their area of specialization and interest. Fundamental and emerging specializations in the domain of mathematics, like systems and control, computational and theoretical fluid dynamics, advanced complex analysis, mathematical modelling of biological systems, and applied and theoretical statistics etc., will be offered as area of research for graduate students at this department. The mathematics department is also providing support to other engineering and sciences departments of MUST, so upon successful completion of the courses taught by mathematics faculty, students will be able to:

PLO-01: Apply knowledge of mathematics, science, and engineering fundamentals to the solution of complex problems involved in different areas of engineering and sciences.

PLO-02: Identify, formulate, search literature, and analyze mathematical models governing laws of physics and other engineering sciences.

PLO-03: Design solution strategy for mathematical models arising in aerospace engineering, electrical engineering, mechanical engineering, and other science and engineering disciplines.

PLO-04: Create, select, and apply appropriate techniques, resources, and modern engineering and IT tools, including prediction and modeling the physical phenomena with an understanding of the limitations.

PLO-05: Communicate effectively on mathematical activities with the engineering community and with society at large, such as being able to comprehend and write effective reports and design documentation, make effective presentations, and give and receive instructions effectively.

PLO-06: Apply ethical principles and exhibit commitment to professional ethics, responsibilities and norms of the profession.

3.13 Scope of the Program:

The mathematical experts are in demand across all kind of industries, the world over. The curriculum of MPhil mathematics is so designed that students in this department will have a chance to learn not only the fundamental courses of mathematics but also advanced courses and tools related to the emerging areas of applied mathematics like systems and control, mathematical modelling, computational fluid dynamics, complex analysis, statistics, etc. Some of the career opportunities for our graduates are listed in the following.

- a). Teaching at school, college, or higher level
- b). R&D and strategic organizations like PAEC, NESCOM, SUPARCO, KRL, etc.
- c). Banking sector, trading, and stock exchange businesses
- d). Higher studies in national and international universities and institutes
- e). Armed forces, civil services, oil and gas sector, etc.

3.14 Program Structure and Features, Curriculum Units, Credit and Award Requirements

Sr. No.	Category	No. of Courses	Credit Hrs	Remarks
01	Core Courses	04	12	
02	Elective Courses	04	12	
03	Seminar	01	01	
04	Thesis	01	06	
Total			31	

3.15 Semester-Wise Breakdown

Semester-I

Following advanced courses of Mathematics will be offered in this semester.

1. Core I
2. Core II
3. Elective I
4. Elective II

Semester-II

Following foundation courses of the specialized areas will be offered in this semester.

1. Core III
2. Core IV
3. Elective III
4. Elective IV

Semester-III

Students will start research work in this semester. Students will register in Thesis which will be concluded in Semester IV.

Semester-IV

Students will submit and defend their thesis at the end of this semester. The Seminar will also be graded in this semester. The students who can't finish their thesis by the end of the 4th semester, will seek approval from the relevant authority (AS&RB) for an extension to complete their degree.

3.16 List of Courses for M.Phil Program

A. Compulsory Requirements

Code	Course Title	Credit Hours
MAT-7001	Seminar	01
MAT-7002	Thesis	06
MAT-7003	*Research Methodology and Scientific Writing	S/U

*This course will be a non-credit course. This will be offered in 3rd semester when students start their thesis. This will be an S/U based course but students have to pass it for completing the degree requirements. Its assessments will be based on home assignments.

In the following, a list of core courses is given. A student will have to complete 12 credit hours (4 courses) of his/her course work from these courses.

Code	Course Title	Credit Hours
MAT-7004	Mathematical Analysis	03
MAT-7005	Advanced Mathematical Physics	03
MAT-7006	Riemannian Geometry	03
MAT-7007	Advanced Complex Analysis	03
MAT-7008	Mathematical Techniques	03
MAT-7009	Advanced Topology	03
MAT-7010	Advanced Abstract Algebra	03

B. Elective Courses (12 credit hrs)

In the following, a list of elective courses is given. A student will have to complete 12 credit hours of his/her course work from these courses.

Code	Course Title	Credit Hours
MAT-7011	Advanced Numerical Analysis	03
MAT-7012	Geometric Functions Theory	03
MAT-7013	Advanced Optimization Theory	03
MAT-7014	Advanced Mathematical Modeling	03
MAT-7015	Nonlinear Systems and Control	03
MAT-7016	Optimal Control	03
MAT-7017	Sampling Techniques	03
MAT-7018	Multivariate Analysis	03
MAT-7019	Finite Mixture Distributions	03
MAT-7020	Mathematical Techniques for Boundary Value Problems	03
MAT-7021	Non-Newtonian Fluid Mechanics	03
MAT-7022	Fundamentals of the Theory of Fluids	03

MAT-7023	Group Methods for Differential Equations	03
MAT-7024	Computer Applications in Mathematics	03
MAT-7025	Fundamentals of Finite Element Methods	03
MAT-7026	Advanced Integral Equations	03
MAT-7027	Approximation Theory	03
MAT-7028	Complex Analysis of Several Variables	03
MAT-7029	Advanced Analytical Dynamics	03
MAT-7030	Introduction to Robotics	03
MAT-7031	Stochastic Processes	03
MAT-7032	Estimation Theory	03
MAT-7033	Time Series	03
MAT-7034	Mathematical Ecology	03
MAT-7035	Biomathematics	03
MAT-7036	Advances in Discrete Mathematics and Applications	03
MAT-7037	Graph Theory	03
MAT-7038	Lie Algebra	03

\

3.17 Details of the Courses/Contents

Course Code: MAT-7003 **Title:** Research Methodology and Scientific Writing **Credit Hrs:** 03

Course Outline: Definition of Research, Types of Research, Selection of Problem, Formation of Hypothesis and Objective, Literature Review, Research Design: Experimental and Nonexperimental Research, Ethical issues in the Research Process, Components of Scientific Report, Various Methods of Data Presentation: Tables, Diagrams, Graphs and their interpretation; Citation and listing of references, Preparation of Scientific Reports by using a scientific writing tool (Latex, MS Word, Scientific workplace, etc), Plagiarism, Publication Procedures.

Text and Reference Books

1. McKnight, C. Magid, A. Murphy, J. T. McKnight, M. *Mathematics Education Research: A Guide for the Research Mathematician*. AMS production, 2000.
2. Andrew, C. O. and Hildebrand, P. E. *Applied Agricultural Research, Foundations and Methodology*, Western Press, 1993.
3. Borderns, K. and Abbott, B. B. *Research Design and Methods: A process Approach*. 8th edition, McGraw Hill Education, 2015.
4. Thomas, C. G. *Research Methodology and Scientific Writing*. Ane Books Pvt. Ltd., 2016.

Course Code: MAT-7004 **Title:** Advanced Mathematical Analysis **Credit Hrs:** 03

Course Outline: **Introduction to Fourier analysis:** Lebesgue measure, Fubini Theorem, Convolutions, Introduction to the Fourier Transform, **Introduction to Function spaces:** Introduction to Sobolev spaces and distributions, Foundations of Harmonic analysis and theory of maximal operators, Lebesgue points, **Introduction to Geometric measure theory:** Hausdorff metric, Hausdorff measure, Fractals, Hausdorff dimensions, Box dimension,

Text and Reference Books:

1. E. B. Davis, *Spectral Theory and Differential Operators*, Graduate text, Cambridge University Press, 1995.
2. E. H. Lieb and M. Loss, *Analysis, Graduate Studies in Mathematics*, Volume 14, AMS, 1997.
3. V. Maziya and S. Poborchi, *Differential Functions on bad domains*, World Scientific, 1997.
4. Steven R. L., *Analysis: With an Introduction to Proof*, 4th edition, Pearson, 2004.

Course Code: MAT-7005

Title: Advanced Mathematical Physics

Credit Hrs: 03

Course Outline: Nonlinear ordinary differential equations, Bernoulli's equation, Riccati equation, Lane-Emden equation, Nonlinear Pendulum, Duffing's equation, Pinney's equation, Perturbation theory, Bogoliubov-Krilov method. Linear partial differential equations, classification, initial and boundary values problems, Fourier analysis, Heat equation, Wave equation, Laplace equation etc. Integral equations, classification, integral transform, separable kernels, singular integral equations, Wiener-Hopf equations, Fredholm theory, series solutions. Variational methods, The Euler-Lagrange equations, Solutions to some famous problems, Sturm-Liouville Problem and variational principles, Rayleigh-Ritz Methods for partial differential equations. Matrix algebra, method of Faddeev, Cayley-Hamilton' theorem function of matrices. Functions of matrices, Kronecker and Tensor product, special matrices.

Text and Reference Books

1. G. Stephenson and P. M. Radmore, *Advanced Mathematical Methods for Engineering and Science Students*, Cambridge University Press, 2006.
2. K. T. Tang, *Mathematical Methods for Engineers and Scientists*, Volumes I, II & III, Springer, 2007.
3. M. Stone and P. Goldbart, *Mathematics for Physics*, Academic Press, 2005.
4. S.I. Hayek, *Advanced Mathematical Methods in Science and Engineering*, 2010.

Course Code: MAT-7006

Title: Riemannian Geometry

Credit Hrs: 03

Course Outline: Definition and examples of manifolds. Differential maps. Submanifolds. Tangents. Coordinate vector fields. Tangent spaces. Dual spaces. Multilinear functions. Algebra of tensors. Vector fields. Tensor fields. Integral curves. Flows. Lie derivatives. Brackets. Differential forms. Introduction to integration theory on manifolds. Riemannian and semi Riemannian metrics. Flat spaces. Affine connection. Parallel translations. Covariant differentiation of tensor fields. Curvature and Torsion tensors. Connection of a semi-Riemannian tensor. Killing equation and Killing vector fields. Geodesics. Conformal transformations and the Weyl tensor.

Text and Reference Books:

5. M. P. do Carmo, *Riemannian Geometry*, Birkhauser, Boston, 1992.
6. D. Langwitz, *Differential and Riemannian Geometry*, Academic Press, 1970.
7. R. L. Bishop and S. I. Goldberg, *Tensor Nalysis and Manifolds*, Dover Publication, Inc., 1980.
8. M. Berger , *A Panoramic View of Riemannian Geometry*, Springer, 2007.

Course Code: MAT-7007

Title: Advanced Complex Analysis

Credit Hrs: 03

Course Outline: An Overview of the Theory of a Complex Variables, Argument Principle, Rouché's Theorem, Conformal Mapping, Harwitz Theorems, Cauchy's Theorem on Partial Fraction Expansions, Inverse and Implicit Functions, Riemann Mapping Theorem, Univalent Functions, Basic Properties of Harmonic, Positive Harmonic and Subharmonic Functions, Poisson Integral Formula, Mittag-Leffler and Weierstrass Theorems, Infinite Products and Weierstrass Factorisation Theorem, Analytic Continuation, Special Functions Including Gamma Function, Riemann Zeta Function, Prime Number Theorem, Elliptic Functions

Text and Reference Books:

1. L. V. Ahlfors, *Complex Analysis*, M. G. Hill, 1979.
2. R.V. Churchill and J.W. Brown, *Complex Variables and Applications*, 5th Edition, M. Graw Hill, 1989.
3. J. B. Conway, *Functions of one Complex Variable*, Springer, 1979.
4. E. Hill, *Analytic Function Theory*, Vol. I and II, Chelsea Publishing Company, New York, 1974.

Course Code: MAT-7008

Title: Mathematical Techniques

Credit Hrs: 03

Course Outline: Green's function method with applications to wave-propagation. Solution of algebraic equations by perturbation methods. Evaluation of integrals by expansion of integrands. Laplace methods. The method of stationary phase. The methods of steepest descent. Solution of the linear damped oscillator equation by perturbation methods. The WKB approximation. Variational problems with variable end points. Corner conditions. Sufficient conditions for minimum. The Ritz method and its applications. A survey of transform techniques. Wiener-Hopf technique with applications to diffraction problems.

Text and Reference Books:

1. A. Nayfeh, *Perturbation Methods*, John Wiley & Sons, Inc., 1973.
2. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Volume I & II, The MacMillan Company, 1970.
3. B. Boble, *Methods Based on the Wiener-Hopf Technique for the Solution of Partial Differential Equations*, Pergamon Press, 1958.
4. J. Jordan and P. Smith, *Mathematical Techniques: An Introduction for the Engineering, Physical, and Mathematical Sciences*, Oxford University Press, 2008.

Course Code: MAT-7009

Title: Advanced Topology

Credit Hrs: 03

Course Outline: Convergence: Sequence and Nets, Filterbase in Space, Convergence, Properties of Filterbases, Closure in Terms of Filterbase, Continuity, Convergence in Cartesian Products, Adequacy of Sequences, Maximal Filterbase

Compactness: Compact Spaces, Special Properties of Compact, Countable Compactness, Compactness in Metric Spaces, Perfect Maps, Local Compactness, O-Compact Spaces, Compactification, K-Space, Baire Space Category

Function Spaces: The Compact Open Topology, Continuity of Composition, The Evaluation Map, Cartesian Products, Application to Identification Topologies, Basis for Z^Y , Compact Subsets of Z^Y Sequential Convergence in the C-Topology, Metric Topologies, Relation to the C-Topologies, Point-Wise Convergence, Comparison of Topologies in Z^Y

The Spaces $C(Y)$: Continuity of the Algebraic Operations, Algebras in $C(Y; C)$, Stone-Weierstrass Theorem, The Metric Space $C(Y)$, Embedding of Y in $C(Y)$, The Ring $C(Y)$.

The Complete Spaces: Cauchy Sequences, Complete Metrics and Complete Spaces, Cauchy Filterbases, Total Boundedness, Baire's Theorem for Complete Metric Spaces, Extension of Uniformly Continues Maps, Fixed Point Theorem for Complete Spaces, Complete Subspaces of Complete Spaces, Complete Gauge Structure.

Text and Reference Books

1. J. Dugundji, *Topology*, Allyn and Bascon, Boston, 1966.
2. J. L. Kelley, *General Topology*, Ishi Press, 2008.
3. J. R. Munkress, *Topology A First Course*, Prentice Inc. Englewood Cliffis, New Jessy, 2nd Edition, 2005.
4. S. Davis, *Topology*, 1st Edition, McGraw-Hill Math, 2004.

Course Code: MAT-7010

Title: Advanced Abstract Algebra

Credit Hrs: 03

Course Outline: Endomorphism and Automorphism of Groups, Simple Groups (Definition and Examples), Direct Product of Groups, Sylow Groups and Sylow Theorems, Normal Series of a Group, Refinement Theorem, Composition Series and Jordan Holder Theorem, Solvable and Nilpotent Groups, Finitely Generated Abelian Groups.

Text and Reference Books

1. P. M. Cohn, *Algebra*, Vol. I & II, John Wiley & Sons,
2. S. Lang, *Algebra*, Springer Verlag, 2002.
3. D.S. Dummit and R. M. Foote, *Abstract Algebra*, 3rd Edition, Wiley, 2003.
4. J. A. Gallian, *Contemporary abstract algebra*, D.C. Heath, 1986.

Course Code: MAT-7011

Title: Advanced Numerical Analysis

Credit Hrs: 03

Course Outline: Numerical Differentiation, Richardson's Extrapolation, Elements of Numerical Integration, Composite Numerical Integration, Romberg Integration, Adaptive Quadrature Methods, Gaussian Quadrature, Multiple Integrals, Improper Integrals
Discrete Least Squares Approximation, Orthogonal Polynomials and Least Squares Approximation, Chebyshev Polynomials and Economization of Power Series, Rational Function and Trigonometric Polynomial Approximations, Fast Fourier Transforms
Linear Algebra and Eigenvalues, The Power Method, Householder's Method
Fixed Points for Functions of Several Variables, Newton's Method, Quasi-Newton Methods, Steepest Descent Techniques, Homotopy and Continuation Methods
The Linear Shooting Method, The Shooting Method for Nonlinear Problems, Finite-Difference Methods for Linear Problems, Finite-Difference Methods for Nonlinear Problems, The Rayleigh-Ritz Method
Elliptic Partial Differential Equations, Parabolic Partial Differential Equations, Hyperbolic Partial Differential Equations, An Introduction to the Finite-Element Method

Text and Reference Books

1. R. L. Burden and I. D. Faires, *Numerical Analysis*, 9th Edition, PWS Publishing Company, 2011.
2. K.E. Atkinson, *An Introduction to Numerical Analysis*, 2nd Edition, John Wiley and Sons, New York, 1989.
3. U. Ascher, R. Matteij and R. Russell, *Numerical Solution of BVPs for ODEs*, Prentice Hall, 1988.
4. M. S. Allen, I. Herrea and George F., *Numerical Modeling in Science and Engineering*, Wiley-Interscience, 99 edition, 1988.

Course Code: MAT-7012

Title: Geometric Functions Theory

Credit Hrs: 03

Course Outline: Univalent Functions, Some Elementary Transformations of Univalent Functions and Their Properties, Growth and Distortion Theorems for Univalent Functions, Functions with Positive Real Part and Their Related Concepts, Star-Shaped Domains and Starlike Functions, Convex Domains and Convex Functions, Coefficient Bounds, Distortion and Growth Theorem, Functions with Bounded Mocanu Variations
Spirallike, Close-to-Convex and Quasi-Convex Functions, Functions with Bounded Boundary and Bounded Radius Rotations, Bazilevic Functions, Subordination and Convolution in Geometric Function Theory and Their Applications, Some Operators

Text and Reference Books

1. P.L. Duren, *Univalent Functions*, Grundlehren der Math. Wissen chaften, Springer-Verlag, New York-Berlin, 1983.
2. A. W. Goodman, *Univalent Functions*, Vol. I and II, Polygonal Publishing House, Washington, New Jersey, 1983.
3. D. G. Zill and P. D. Shanahan, *A First Course in Complex Analysis with Applications*, Jones and Bartlet Publishers, Sudbury, Massachusetts, 2008.
4. S. G. Krantz, *Explorations in Complex Geometric Function Theory Analysis*, 2006 Edition, Birkhäuser, 2005.

Course Code: MAT-7013 **Title:** Advanced Optimization Theory **Credit Hrs:** 03

Course Outline: Intro to mathematical optimization, objective of constraint functions, basic optimization concepts, mathematical prerequisites, convexity, gradient vectors, Hessian matrix, global and local minima, saddle points, optimality conditions, general structure for line search method, Wolfe conditions, Goldstein conditions, convergence of line search method, convergence of steepest descent method, Newton method, Quasi Newton method, Newton method with Hessian approximation, line search algorithm for Wolfe conditions, conjugate gradient method, Trust Region Method and Cauchy point, Newton point, Dogleg method.

Text and Reference Books

1. L. Elsgolts, *DEs and the Calculus of Variations*, Mir Publishers Moscow, 1970.
2. B. S. Gotfried and J. Weisman, *Introduction to Optimization Theory*, Prentice Hall, Englewood Cliffs, NJ, USA, 1973.
3. D. G. Luenberger, *Introduction to Linear and Non-Linear Programming*, Addison Wesley, Reading, USA, 1973.
4. D. A. Pierre, *Optimization Theory with Applications*, Dover Publications, 1986.

Course Code: MAT-7014 **Title:** Advanced Mathematical Modeling **Credit Hrs:** 03

Course Outline: Modeling through Differential Equations, Mathematical modeling through Ordinary Differential Equations, Mathematical modeling through system of Ordinary Differential equations of first order, Excursive of some modeling projects to demonstrate the variety of the require equations to formulate essential, control theory as modeling tool, Parameter estimation as optimization problem, Sensitivity analysis, Parameter estimation, Situation giving rise to Partial Differential Equations, Modeling through Delay differential and Differential–Difference equations

Text and Reference Books

1. Edwards, D. and Hamson, *Mathematical modeling Skills*, Macmillan Press Ltd, 1996.
2. Giordano, F.R., Weir, M.D. and Fox, W.P., *A First Course in Mathematical modeling*, Thomson Brooks/Cole, 2003.
3. J.N.Kapur, *Mathematical modeling*, New Age international (P) Limited, 2015.
4. M. M. Meerschaert, *Mathematical modeling*, 4th Edition, Academic Press, 2013.

Course Outline:

Analysis techniques for nonlinear systems: phase portraits and their symmetries, singular points, phase plan analysis of linear and nonlinear systems, existence of limit cycles,

Fundamentals of Lyapunov Theory: Nonlinear systems and equilibrium points, concept of stability, linearization and local stability, Lyapunov's direct method and stability analysis, Krasovskii and variable gradient methods, performance analysis, control design based on Lyapunov's direct method

Advanced Stability Analysis: Stability of non-autonomous systems, Linearization and Lyapunov's direct methods for nonlinear autonomous systems, Asymptotic properties of functions and their derivatives, Barbalat Lemma, positive real and strictly positive real transfer functions, Kalman-Yakubovich lemma, passivity of linear systems,

Describing Function Analysis: Fundamentals of describing function analysis, common nonlinearities in control systems and their describing functions, Nyquist criterion and its extensions, existence and stability of limit cycles, reliability of describing function analysis,

Nonlinear Control Systems Design: Feedback Linearization: Canonical form, Lie derivatives and Lie brackets, diffeomorphism and state transformations, the Frobenius theorem, input-state and input-output linearization of SISO systems, the normal forms and zero dynamics, local and global asymptotic stabilizations, tracking control and inverse dynamics, feedback linearization of multi-input systems,

Adaptive Control: Basic concepts in Adaptive Control, Adaptive control of first order systems, Adaptive control of linear systems of relative degree 1 and higher with full state-feedback and output feedback, Adaptive Control of nonlinear systems, robustness of adaptive control systems,

Text and Reference Books

1. H. K. Khalil, *Nonlinear Control*, Prentice Hall, 2002.
2. Slotine and Li, *Applied Nonlinear Control*, Prentice Hall, 1991.
3. A. Isidori, *Nonlinear Control Systems*, 3rd Edition, Springer, 1995.
4. B. Friedland, *Control System Design: An Introduction to State-Space Methods*, Dover Publications, 2005.

Course Code: MAT-7016

Title: Optimal Control

Credit Hrs: 03

Course Outline: Calculus of Variation: Principle of calculus of variation, Euler Equation in Calculus of variation, some important theoretical results of calculus of variation and mathematical examples

Optimal Control and the Minimum Principle: Application of calculus of variation in optimal control, simplest problem in the Calculus of variation, Necessary condition for optimality, Lagrange multipliers, and Hamiltonian equations, The minimum principle, solution of Zermelo's problem, Linear quadratic cost problem with finite and infinite horizon: theory and examples,

Optimal Control Theory and Dynamic Programming: Dynamic programming in discrete time, Principle of optimality and Bellman's equation, linear quadratic cost problem with finite and infinite horizon in the dynamic programming perspective: theory and examples,

Differential Games: Introduction, continuous time differential games, intro to Nash and Stackleberg equilibrium solutions concepts, solutions of Nash differential games: theory and examples

Text and Reference Books

1. D. Liberzon, *Calculus of Variations and Optimal Control Theory: A Concise Introduction*, Princeton University Press, 2012
2. G. Meisma, *Lecture Notes on Optimal Control*, University of Twente, Enschede, The Netherlands, 2013.
3. D. E. Krik, *Optimal Control Theory: An Introduction*, Dover Publications, 2004.
4. R. F. Stengel, *Optimal Control*, Dover Publications, 1994.

Course Code: MAT-7017

Title: Sampling Techniques

Credit Hrs: 03

Course Outline: Equal Probability Sampling: Simple Random Sampling and General Formula for The Derivation of Variance and Variance Estimator, Derivation of Variance and Estimated Variance for The Proportion in one Class to a Group of Classes, Derivation of Variance Estimator for Quantitative and Qualitative Characteristics, Stratified Sampling, Optimum Allocation Effect of Deviation From Optimum Allocation, Two Way Stratification, Controlled Selection, Construction of Strate, Gain Due to Stratification, Unequal Probability Sampling: Probability Proportional to Size Sampling, Sampling with Replacement, Cumulative Method, Hansen-Hurwitz (Multinomial), Pathak, Lahiri Selection Procedures, Sampling with Unequal Probability Sampling, Yates-Grundy, Midzuno-Sen-Ikeda, Brewer, Sampford, Dubin, Raj, Murthy, Rao-Hartly-Cochran Selection Procedures.

Text and Reference Books

1. W. G. Cochran, *Sampling Techniques*, John Wily and Sons, New York, 3rd Edition, 1977.
2. I. Kish, *Survey Sampling*, John Wiley and Sons, New York, 1965.
3. D. Raj, *Sampling Theory*, M. Graw Hill, New York, 1968.
4. P. V. Sukatme and B. V. Sukatme, *Sampling Theory of Surveys with Application*, Iowa State University Press, USA, 1970.

Course Code: MAT-7018

Title: Multivariate Analysis

Credit Hrs: 03

Course Outline: Introduction: Some Multivariate Problems and Techniques, The Data Matrix, Multivariate Normal Distribution Theory: Characterization and Properties, Linear Forms, The Wishart Distribution, The Hotelling T^2 Distribution, Maximum Likelihood Estimation and Other Techniques, Principal Component Analysis: Definition and Properties of Principal Components, Testing Hypothesis about Principal Components, Correspondence Analysis, Discarding of Variables, Principal Component Analysis in Regression. Factor Analysis: The Factor Model, Relationship between Factor Analysis and Principal Component Analysis. Canonical Correlation Analysis: Dummy Variable and Qualitative Data, Qualitative and Quantitative Data. Discriminant Analysis.

Text and Reference Books

1. M. Kshirsagar, *Multivariate Analysis*, M. Dekker, New York, 1972.
2. K. V. Mardia, J. T. Kent and J. M. Bibby, *Multivariate Analysis*, Academic Press, London, 1982.
3. A. C. Rencher and W. F. Christenson, *Methods of Multivariate Analysis*, 3rd Edition, Wiley, 2012.
4. K. V. Mardia, J. T. Kent and J. M. Bibby, *Multivariate Analysis*, 1st Edition, 1980.

Course Code: MAT-7019

Title: Finite Mixture Distributions

Credit Hrs: 03

Course Outline: Introduction: Basics Definition and Concepts, Statistical Problem Associated with Mixtures, Application of Finite Models, Mathematical Aspects of Mixture: Identifiability, Multimodality, Properties of General Mixture, Parameters of Mixture: Various Methods of Determining the Parameters of a Mixture.

Text and Reference Books

1. B. S. Everitt and D. J. Hand, *Finite Mixture Distribution*, Chapman and Hall London, 1981.
2. D. M. Titterington, A. F. M. Smith and U. E. Makov, *Statistical Analysis of Finite Mixture Distributions*, John Wiley and Sons, New York, 1985.
3. G. McLachlan and D. Peel, *Finite Mixture Models*, 1st Edition, Wiley Interscience, 2000.
4. S. F. Schnatter, *Finite Mixture and Markov Switching Models*, 2006 edition, Springer, 2006.

Course Code: MAT-7020

Title: Mathematical Techniques for BVPs

Credit Hrs: 03

Course Outline: Green's Function Method, Perturbation Method: Regular and Singular Perturbation Techniques with Application, Variational Methods, Wiener-Hopf Techniques with Applications to Diffraction Problems.

Text and Reference Books

1. R. Mitra and S. W. Lee, *Analytical Techniques in the Theory of Guided Waves*, Macmillan, 1971.
2. E. J. Hinch, *Perturbation Methods*, Cambridge University Press, 1991.
3. B. Noble, *Methods Based on the Wiener Hopf Techniques for the Solution of Partial Differential Equations*, 2nd Edition, American Mathematical Society, 1988.
4. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Society for Industrial and Applied Mathematics, 1987.

Course Code: MAT-7021

Title: Non-Newtonian Fluid Mechanics

Credit Hrs: 03

Course Outline: Classification of Non-Newtonian Fluids, Rheological Formulates (Time–Independent Fluids, Thyrrotrophic Fluids and Viscoelastic Fluids), Variable Viscosity Fluids. Cross Viscosity Fluids, The Deformation Rate, The Rivlin-Ericksen Fluid, Basic Equation of Memories in Rheological Models. The Linear Viscoelastic Liquid, Couette Flow, Poiseuille Flows, The Current Semi-Infinite Field. Axial Oscillatory Tube Flow, Angular Oscillatory Motion, Periodic Transients, Basic Equations in Boundary Layer Theory, Orders of Magnitude, Truncated Solutions for Viscoelastic Flow, Similarity Solutions. Turbulent Boundary Layers, Stability Analysis.

Text and Reference Books

1. G. Astarita and M. G. ,*Principles of Non-Newtonian Fluid mechanics*, McGraw-Hill 1974.
2. R. B. Bird, R. C. Armstrong and O. Hassager, *Dynamic of Polymeric liquids*, Vol. 1 and II, John Wiley and Sons, New York, 1987.
3. W. F. Robert and A. T. McDonald, *Introduction to Fluid Mechanics*, John Wiley and Sons, 1995.
4. W. R. Schowalter, *Mechanics of Non-Newtonian Fluids*, Pergamon Press, New York, 1978.

Course Code: MAT-7022

Title: Fundamentals of the Theory of Fluids

Credit Hrs: 03

Course Outline: Euler's Equations of Motion, Viscosity, Navier-Stokes Equations and Exact Solutions, Dynamical Similarity and Reynolds Number, Energy Equation, Boundary Layer Concept and Governing Equations, Magnetohydrodynamics (MHD) Equations, Fluid Drifts, Stability and Equilibrium Problems, Introduction to Turbulent Flow.

Text and Reference Books

1. G. Astarita and G. Merrucci, *Principles of Non-Newtonian Fluid mechanics*, M. Graw Hill, 1974.
2. R. B. Bird, R. C. Armstrong and O. Hassager, *Dynamic of Polymeric liquids*, Vol. I, 2nd Edition, John Wiley and Sons, New York, 1987.
3. J. Harris, *Rheology and Non-Newtonian Flow*, Longman Inc., New York, 1977.
4. Schowalter, *Mechanics of Non-Newtonian Fluids*, Pergamon Press, New York, 1978.

Course Code: MAT-7023 **Title:** Group Methods For Differential Equations **Credit Hrs:** 03

Course Outline: Basic concept of groups of transformation, Parameter Lie group of transformation (LGT), infinitesimal transformation (I.T), Infinitesimal generators, Lie's first fundamental theorem, Invariance, Canonical coordinates, Elongations, Multi-parameter Lie group of transformation (MLGT), Lie algebra, Solvable Lie algebra, Lie's second and third fundamental theorems.

Invariance of ODE's under (LGT) and (MLGT), Mapping solutions to other solutions from invariance of an ODE and PDE, Determining equations (I.T) of and n^{th} order ODE and system of PDE's, Determination of n^{th} order ODE invariant under a given group, Reduction of order by canonical coordinates and differential invariants, invariant solutions of ODE's and PDE's Separatrics and envelops. Neother's theorem and Lie-Backlund symmetries, Potential symmetries, Mapping of differential equations.

Text and Reference Books:

1. J. M. Hill, *Differential Equations and Group Methods*, CRC Press, Inc. New York, 1992.
2. L. P. Eisnhart, *Continuous Group of Transformation*, Dover Publication, Inc. New York, 1961.
3. P. E. Luther, *Continuous Group of Transformation*, Andesite Press, 2017.
4. P. E. Hyden, *Symmetries and Differential Equations*, 1st edition, Cambridge University Press, 2000.

Course Code: MAT-7024 **Title:** Computer Applications in Mathematics **Credit Hrs:** 03

Course Outline: Introduction and motivation. Examples of simulations for random walk, Poisson process, Brownian motion Review of probability, Inverse transform method, Acceptance - rejection method, Normal random variable and Brownian motion, Brownian motion and Geometric Brownian motion, Simulating Brownian motion and Geometric Brownian motion, Practicing with Matlab, Poisson Process, Homogeneous and non-homogeneous, Simulating Poisson process, Statistical analysis of the output, Discrete event simulation, G/G/1 networks, Simulation of the queueing networks, Variance reduction, Markov Chain Monte Carlo, Optimization, Applications: Trading in financial markets.

Text and Reference Books:

1. J. M. Hill, *Differential Equations and Group Methods*, CRC Press, Inc. New York, 1992.
2. L. P. Eisnhart, *Continuous Group of Transformation*, Dover Publication, Inc. New York, 1961.
3. P. E. Luther, *Continuous Group of Transformation*, Andesite Press, 2017.
4. P. E. Hyden, *Symmetries and Differential Equations*, 1st edition, Cambridge University Press, 2000.

Course Code: MAT-7025

Title: Fundamentals of Finite Element Methods

Credit Hrs: 03

Course Outline: Finite Element Methods: General Approach, The Galarkin Method in One and More Dimensions and Application, Error Bound on the Galarkin Method and Application, The Method of Collocation, Error Bounds on the Collocation Method and Application, Comparison of Efficiency of the Finite Difference and Finite Element Method, Application to Solution of Linear and Non-Linear Partial Differential Equations Appearing in Physical Problems

Text and Reference Books

1. S. D. Burnett, *Finite Element Analysis from Concept to Applications*, Addison Wesley, 1987.
2. G. S. Desai, *Elementary Finite Element Method*, Prentice Hall, 1988.
3. G. Strang and G. Fix, *Analysis of Finite Element Method*, Prentice Hall, New Jersey, 1973.
4. J. N. Reddy, *Introduction to the Finite Element Method*, 3rd Edition, MHI, 2006.

Course Code: MAT-7026

Title: Advanced Integral Equations

Credit Hrs: 03

Course Outline: Existence Theorem, Integral Equations with L_2 Kernal, Applications to Partial differential equations, Integral Transforms, Wiener-Hopt Techniques.

Text and Reference Books

1. H. H. Stadl, *Integral Equations*, John Wiley and Sons, 1973.
2. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Macmillan, New York, 1968.
3. F. G. Tricomi, *Integral Equations*, Inter science, 1957.
4. J. J. Abdul, *Introduction to Integral Equations with Applications*, Marcel Dekker Inc. New York, 1985.

Course Code: MAT-7027

Title: Approximation Theory

Credit Hrs: 03

Course Outline: Best Approximation in Metric and Normed Spaces, Least Square Approximation, Rational Approximation, Haar Condition and Best Approximation in Function Spaces, Interpolation, Stone-Weierstrass Theorem for Scalar and Vector-Valued Functions, Spline Approximation, Best Approximations in Normal Spaces, Existence Theorem, Approximation by Algebraic Polynomials, Uniqueness, Strict Convexity, Lemma Convexity, Uniqueness Theorem, Hilbert Space, Uniform Approximation, External Point, Haar Condition, Extreme Points, Best Approximation, Characterization of Best Approximation, A Brief Introduction to Interpolation, Chebyshev Polynomials, Chebyshev Theorem, Least Squares Approximation, Gram-Schmidt Orthonormalization Process, Orthogonal Function, Pade Approximation, Remex Algorithm

Text and Reference Books

1. N. I. Achieser, *Theory of approximation*, Dover Publications, Inc., New York, 2004.
2. T. J. Rivlin, *An Introduction to the Approximation of Functions*, Dover Publications, Inc., New York, 1981.
3. M. J. D. Powell, *Approximation Theory and Methods*, Cambridge University Press, 1988.
4. E. W. Cheney, *Introduction to Approximation Theory*, AMS, 2000.

Course Code: MAT-7028 **Title:** Complex Analysis of Several Variables **Credit Hrs:** 03

Course Outline: Holomorphic Functions: Review of One Variable Theory, Real and Complex Differentiability, Power Series, Complex Differentiable Functions, Cauchy Inequalities, The Maximum Principles.

Extension of Analytical Functions: Hartogs Figures, Hartogs Theorems, Domains of Holomorphy, Holomorphic Convexity, Theorem of Cartan Thullen.

Levi-Convexity: The Levi Forms, Geometric Interpretation of its Signature, E. E. Levi's Theorem, Connections with Kählerian Geometry, Elementary Properties of Plurisubharmonic Functions.

Introduction to Cohomology: Definition and Example of Complex Manifolds, The $\bar{\partial}$ Operators, The Poincaré Lemma and the Dolbeault Lemma, The Cousin Problems, Introduction to Sheaf Theory.

Text and Reference Books

1. J. Morrow and K. Kodaria, *Complex Manifolds*, Holt, Rinehart and Winston, New York, 1971.
2. L. Hormander, *An Introduction to Complex Analysis in Several Variables*, D. V. Nostand, New York, 1966.
3. H. Grauert and K. Fritsch *Several, Complex Variables*, Springer Verlag, 1976.
4. M. Field, *Several Variables and Complex Manifolds*, Cambridge University Press, 1982.

Course Code: MAT-7029 **Title:** Advanced Analytical Dynamics **Credit Hrs:** 03

Course Outline: Equations of Dynamic and its Various Forms, Equations of Lagrange and Euler, Jacobi's Elliptic Functions and the Quantitative and Qualitative Solutions of the Problem of the Euler and Poisson, the Problems of Lagrange and Poisson, Dynamical System, Equations of Hamilton and Appell, Hamilton–Jacobi Theorem, Separable System, Holder's Variational Principle and its Consequences. Group of Continuous Transformations and Poincaré's Equations, System with one Degree of Freedom, Singular Points, Cyclic Characteristics of System With N-Degree of Freedom, Ergodic Theorem, Metric Indecomposability, Stability of Motion, Periodic Orbits.

Text and Reference Books

1. H. Baruh, *Analytical Dynamics*, Heinmann, 1st Edition, WCB/McGraw-Hill, 1998.
2. E. T. Whittaker, *A treatise on Dynamic of Rigid Bodies and Particles*, At the University Press, 1927.
3. V. D. Sapio, *Advanced Analytical Dynamics: Theory and Applications*, 1st Edition, Cambridge University Press, 2017.
4. L. Meirovitch, *Methods of analytical dynamics*, McGraw-Hill, 1970.

Course Code: MAT-7030 **Title:** Introduction to Robotics **Credit Hrs:** 03

Course Outline: Fundamental Concepts: Introduction to Robot (Fundamental notions and Definitions), **Jacobians:** Transformations and Jacobians, Manipulator. **Kinematics:** Kinematics (Forward and Inverse) of manipulator, Manipulator Dynamics, Trajectory Generation, Manipulator Mechanism, Manipulator Design. **Linear Control:** Linear Control of Manipulator, Non-linear Control of Manipulator, Forced Control of Manipulator, **Multivariable Control:** Multivariable control, Feedback linearization, Variable structure and Adaptive Control.

Text and Reference Books

1. J. J. Craig, *Introduction to Robotics*, Addison-Wesley Publishing Company, 1999.
2. Mark, W. Sponge, and M. Vidyasagar, *Robot Dynamics Control*, John Wiley and Sons, 2004.
3. G. Franklin, and J. D. Powell, *Feed-back Control of Dynamic Systems*, Addison-Wesley Publishing Company, 1989.
4. S. M. Shimmers, *Modern Control System Theory and Applications*, Addison-Wesley Publishing Company, 1987.

Course Code: MAT-7031 **Title:** Stochastics Processes **Credit Hrs:** 03

Course Outline: Definition of a Stochastic Process, Characterization of a Stochastic Process, Discrete-Time and Continuous-Time Stochastic Process and Their First and Second Order Statistics, Continuity, Derivative and Integral of a Stochastic Process, Time-Averages and Ergodic Theorems, Stationarity, Power Spectral Density, Time- Series Analysis, Discrete-Time Markov Chains, Continuous-Time Markov Chains and Introduction To Queuing Theory

Text and Reference Books

1. W. Whitt, *Stochastic-Process Limits: An Introduction to Stochastic-Process Limits and Their Applications to Queues*, Springer, New York, USA, 2002.
2. Z. Brzeźniak and T. Zastawniak, *Basic Stochastic Processes: A Course Through Exercises*, Springer, NY, 2005.
3. S. M. Ross, *Stochastic-Process*, 2nd Edition, Wiley, 1995.
4. R. G. Gallager, *Stochastic-Process*, 1st Edition, Cambridge University Press, 2014.

Course Code: MAT-7032 **Title:** Estimation Theory **Credit Hrs:** 03

Course Outline: Properties of Estimator, Unbiaseness, Efficiency, Sufficiency and the minimal sufficient statistic, complete classes, Exponential families, Cramer-Rao lower bound and its extension, bias reduction by Jackknifing, ancilliary and Basu theorem, methods of estimation and their optimal properties, Bayes and minimax estimators, shrinkage estimation, sequential estimation. Non Linear Models, Parameters and estimation using ML method, Transformations of parameters, inference and stable transformations. Computing Methods for Non-linear Modelling, Confidence intervals for parameters and functions. Applications of non-linear modelling.

Text and Reference Books

1. Levy, P. S., and Lemeshow, S., *Sampling of Populations Methods and Applications*, 3rd Ed. John Wiley, New York (1999)
2. Lindgren, B. W., *Statistical Theory*, Chapman and Hall (1998).
3. Lehman, E. L., *Theory of Point Estimation*, John Wiley and sons (1987).
4. Ross, G. J. S., *Non-linear Estimation*, Springer-Verlag, New York Inc., (1990).

Course Code: MAT-7033

Title: Time Series

Credit Hrs: 03

Course Outline: Methods of decomposing time-series into its component parts and measuring their effects. Stationary stochastic processes and their properties in the time domain. Frequency domain- Cyclical trend, spectral representation of a stochastic process. Properties of ARMA process and linear filters. Multivariate spectral analysis. Estimation of ARMA models. Model building and forecasting. Practicals based on the above topics

Text and Reference Books

1. A. C. Harvey, *Time Series Models*, Philip Allan Publishers, 1981.
2. I. G. Zurbenko, *The Spectral Analysis of Time Series*, Elsevier Science Publishers B.V., Amsterdam, 1986.
3. E. J. Hannan, *Time Series Analysis*, Methuen, London, 1960.
4. M. G. Kendall, *Time-Series*, Griffin, London, 1973.

Course Code: MAT-7034

Mathematical Ecology

Credit Hrs: 3

Course Outlines: Key models in Behavioral Ecology, Diet-choice and foraging, Evolutionarily Stable Strategies, Search and Predation, Stochastic models and statistics, Probability background and important distributions, Some applications to search and foraging, Bayesian methods, Host-parasitoid models, Nicholson-Bailey and extensions, Evolutionary models and stochastic dynamic programming, Disease models and Fishery models (may be included based on participant interest and available time), Basic SIR and extensions, Evolution of virulence, Vectors and disease, Fisheries bio-economic models, Stochastic population models, Sample paths and stochastic differential equations, General stochastic diffusion processes, Extinction time in density independent case, Extinction time in density-dependent case, Designing a model Cellular automata and IBMs, Formulating and implementing a model

Text and Reference Books:

1. Allen, L. J. S., *An Introduction to Stochastic Processes with Applications to Biology*. Pearson. Upper Saddle River, NJ, USA, 2003.
2. Allen, L. J. S., *An Introduction to Mathematical Biology*. Pearson. Upper Saddle River, NJ, USA, 2007.
3. Allman, E. S. and J. Rhodes., *Mathematical Models in Biology: An Introduction*. Cambridge University Press, 2004.
4. Brauer, F. and C. Castillo-Chavez., *Mathematical Models in Population Biology and Epidemiology*, Springer, NY, 2001.

Course Code: MAT- 7035

Biomathematics

Credit Hrs: 3

Course Outlines: Biological applications of difference and differential equations, Biological applications of nonlinear differential equations, Biological applications of graph theory.

Text and Reference Books:

1. Linda J. S. Allen, *An introduction to Mathematical Biology*, Pearson, 2007.
2. J. Smith, *Mathematical ideas in biology*, Cambridge Press, Cambridge, 1968.
3. S. I. Rubinow, *An introduction to Mathematical Biology*, 1st edition, Dover Publications, 2003.
4. B. P. Ingalls, *Mathematical Modeling in Systems Biology*, 1st edition, The MIT Press, 2013.

Course Code: MAT-7036 **Advances in Discrete Mathematics and Applications** **Credit Hrs: 3**

Course Outlines: Introduction, Definitions of stability and linearized stability, Semi-cycle analysis, Full limiting sequences and Convergence theorems, Lyness equation, Todd equation, the generalized Lozi equation, the Gingerbreadman equation and the Riccati difference equation, analysis of semi-cycle of some special type of equations, Period-2 solutions, Global asymptotic stability of period-2 solutions, Existence of unbounded solutions and Boundedness of solutions, on the systems of rational difference equations

Text and Reference Books:

1. M. R. S. Kulenovic, *Dynamics of Second Order Rational Difference Equations: With Open Problems and Conjectures*, Chapman and Hall/CRC, 2005.
2. E. Camouzis, G. Ladas, *Dynamics of Third-Order Rational Difference Equations with Open Problems and Conjectures*, Chapman and Hall/CRC, 2007.
3. M. H. Education, *Advanced Mathematical Concepts*, 6th Edition, McGraw-Hill Education, 2003.
4. K. Abidi and J. X. Xu, *Advanced Discrete-Time Control: Designs and Applications*, 5th Edition, Springer, 2015.

Course Code: MAT-7037

Title: Graph Theory

Credit Hrs: 03

Course Outline: Undirected Graphs, Geometric Graphs, Abstract Graphs, Isomorphism, Edge Progressions Chains and Circuits, Rank and Nullity, Degrees, Trees, Bipartite Graphs, Unicursal Graphs, Hamiltonian Graphs. Directed Graphs, Arc Progressions, Paths Progression and Cycle Progression

Partition and Distances in Graphs, Edge Partitions, Arc Partitions, Hamiltonian Chains and Circuits, Vertex Partitions, Radius and Diameter, Minimal Length Problem, Foundation of Electrical Network Theory, Matrix Representation, The Incidence Matrix, The Circuit Matrix, The Cut-Set Matrix, The Vertex or Adjacency Matrix, The Path Matrix, Network Flows, Network Flow Problems.

Text and Reference Books

1. J. A. Bondy and U. S. R. Murty, *Graph Theory*, Springer Verlag, York, 2008.
2. B. W. Douglas, *Introduction to Graph Theory*, Prentice Hall, 2001.
3. G. Jonathan and Y. Jay, *Graph Theory and its Applications*, CRC Press, London 1999.
4. R. J. Wilson, *Introduction to Graph Theory*, Prentice Hall Wesley, 1996.

Course Code: MAT-7038

Title: Lie Algebra

Credit Hrs: 03

Course Outline: Definitions and Example of Lie Algebras, Ideals and Quotients, Simple, Solvable and Nilpotent Lie Algebras, Radical of a Lie Algebra, Semi-simple Lie Algebra, Engel's Nil Potency Criterion, Lie's and Cartan Theorems, Jordan-Chevalley Decomposition, Killing Forms, Criterion for Semisimplicity, Product of Lie Algebra, Classification of Lie Algebra up to Four Dimension, Application of Lie Algebras.

Text and Reference Books

1. J. E. Humphreya, *Introduction to the Algebra and Representation Theory*, S. Verlag, 1972.
2. N. Jacobson, *Lie Algebra*, Interscience, New York, 1983.
3. J. Lapowsky and G.W. Macculum, *Elementary Lie Algebra Theory*, Yale University, 1974.
4. O. Neill, *Semi-Riemannian Geometry*, Academic Press, 1983.

4. Scheme of Studies for PhD in Mathematics: General Breakup

Content		Description	Remarks
4.1	Awarding Institute/Body	Mirpur University of Science and Technology (MUST)	
4.2	Teaching Institute	Department of Mathematics, Mirpur University of Science and Technology (MUST)	
4.3	Final Award	Doctor of Philosophy	
4.4	Program Title	Ph.D. in Mathematics	
4.5	Starting Time for Program	Fall/Spring Semester of Every Academic Year	
4.6	Duration of the Program	3 to 8 years (6-16 Semesters)	
4.7	Entrance Requirement	M.Phil or MS or Equivalent Degree in Mathematics with CGPA 3.0 or above (for semester system degree) or 1st division (for annual system)	
		No D-grade in academic career	
		The GRE subject test with a minimum of 60% (for admissions thereafter) percentile score is required.	
4.8	Merit Formula	Merit formulas are the following: For M.Sc: 15% of Intermediate, 20% of B.Sc, 20% of M.Sc, 25% of M.Phil marks, 5% Publications, and 15% of interview conducted by the department. For BS: 15% of Intermediate, 40% of BS, 25% of M.Phil marks, 5% Publications, and 15% of interview conducted by the department.	
4.9	Total Credit Hours	Course Work: 18 Credit Hrs	
		Thesis (MAT-8000): 50 Credit Hrs	
		Seminar I & II (MAT-7998, 7999): 1 Credit Hrs each	
		Comprehensive Examination (Written and Oral): P/F	

4.10 Program Educational Objectives:

Our students will be equipped not only with advanced mathematical tools but will also acquire skill set needed to apply mathematics towards real life problems in different fields of engineering, sciences, economics, business and finance, etc. Moreover, our graduates will be able to:

- i. Collaborate with Engineers and scientists from industry and academia in their research/projects to promote the industry-academia linkages;
- ii. Promote the culture of interdisciplinary novel research and produce fundamental & applied quality research in Pakistan;
- iii. Contribute through active research in the emerging areas of science and engineering, for instance, systems and control, computational and theoretical fluid dynamics, advanced complex analysis, mathematical modelling of biological systems, and statistics etc.

4.11 Program Learning Outcomes (PLOs):

The curriculum for Ph.D program is so designed that the students undertaking research in this department will have a chance to learn not only the fundamental courses of mathematics but also advanced courses related to their area of specialization and interest. Fundamental and emerging specializations in the domain of mathematics, like systems and control, computational and theoretical fluid dynamics, advanced complex analysis, mathematical modelling of biological systems, and applied and theoretical statistics etc., will be offered as area of research for graduate students at this department. The mathematics department is also providing support to other engineering and sciences departments of MUST, so upon successful completion of the courses taught by mathematics faculty, students will be able to:

PLO-01: Apply knowledge of mathematics, science, and engineering fundamentals to the solution of complex problems involved in different areas of engineering and sciences.

PLO-02: Identify, formulate, search literature, and analyze mathematical models governing laws of physics and other engineering sciences.

PLO-03: Design solution strategy for mathematical models arising in aerospace engineering, electrical engineering, mechanical engineering, and other science and engineering disciplines.

PLO-04: Create, select, and apply appropriate techniques, resources, and modern engineering and IT tools, including prediction and modeling the physical phenomena with an understanding of the limitations.

PLO-05: Communicate effectively on mathematical activities with the engineering community and with society at large, such as being able to comprehend and write effective reports and design documentation, make effective presentations, and give and receive instructions effectively.

PLO-06: Apply ethical principles and exhibit commitment to professional ethics, responsibilities and norms of the profession.

4.12 Scope of the Program: The mathematical experts are in demand across all kind of industries, the world over. The curriculum of MPhil mathematics is so designed that students in this department will have a chance to learn not only the fundamental courses of mathematics but also advanced courses and tools related to the emerging areas of applied mathematics like systems and control, mathematical modelling, computational fluid dynamics, complex analysis, statistics, etc. Some of the career opportunities for our graduates are listed in the following

- a). Teaching at school, college, or higher level
- b). R&D and strategic organizations like PAEC, NESCOM, SUPARCO, KRL, etc.
- c). Banking sector, trading, and stock exchange businesses
- d). Higher studies in national and international universities and institutes
- e). Armed forces, civil services, oil and gas sector, etc.

4.12 Program Structure and Features, Curriculum Units, Credit and Award Requirements

Sr. No.	Category	No. of Courses	Credit Hrs	Remarks
01	Core Courses	02	06	
02	Elective Courses	04	12	
03	Seminar	02	02	
04	Thesis	01	50	
Total			70	

4.13 Semester-Wise Breakdown

Semester-I

Following advanced courses of Mathematics will be offered in this semester.

1. Core I
2. Elective I
3. Elective II

Semester-II

Following foundation courses of the specialized areas will be offered in this semester.

1. Core II
2. Elective III
3. Elective IV

Semester-III and IV:

Students will complete his/her course work (if it is not finished in the first two semesters) and clear the Comprehensive Examination (Written and Oral) by the end of the 4th semester.

Semester-V and VI:

Students will submit synopsis in the 5th semester to the relevant body and after approval of the synopsis, research work will start formally. The two Seminars will be evaluated after the submission of synopsis and before the public defense of the thesis. After completing the research work and the degree award requirements, the process for the public defense will be started. The students who can't finish their thesis by the end of the 6th semester, will seek approval from the relevant authority (AS&RB) for an extension to complete their degree.

4.14 List of Courses for Ph.D Program

A. Compulsory Requirements

Code	Title	Credit Hours
MAT-7998	Seminar I	01
MAT-7999	Seminar II	01
MAT-8000	Thesis	50
----	Comprehensive Examination (Written & Oral)	P/F

B. Elective Courses* (18 credit hrs)

In the following, a list of elective courses is given. A student will have to complete 18 credit hours of his/her course work from these courses on the recommendation of his/her supervisor.

Code	Course Title	Credit Hours
MAT-8001	Advanced Functional Analysis	03
MAT-8002	Advanced Partial Differential Equations	03
MAT-8003	Variational Inequalities	03
MAT-8004	Convex Analysis	03
MAT-8005	Parameter Estimation and Sensitivity Analysis	03
MAT-8006	Semigroups in Geometric Functions Theory	03
MAT-8007	Differential Subordination Theory and Applications	03
MAT-8008	Conformal Mappings	03
MAT-8009	Perturbation Methods	03
MAT-8010	Electro-dynamics	03
MAT-8011	Magneto-hydro-dynamics	03
MAT-8012	Fundamentals of Turbulence	03
MAT-8013	LIE Group Analysis of Differential Equations	03
MAT-8014	Selected Topics in Applied Mathematics	03
MAT-8015	Selected Topics in Pure Mathematics	03
MAT-8016	Numerical Solutions of PDEs	03
MAT-8017	Design Methods for Control Systems	03
MAT-8018	Optimal State Estimation	03
MAT-8019	Linear Matrix Inequalities	03
MAT-8020	Advanced Probability Theory	03
MAT-8021	Advanced Sampling Techniques	03
MAT-8022	Advanced Finite Mixture Distributions	03
MAT-8023	Advanced Mathematical Statistics	03
MAT-8024	Stochastic Differential Equations	03
MAT-8025	Fixed Point Theory and Applications	03

MAT-8026	Integral Inequalities	03
MAT-8027	Banach Algebras	03
MAT-8028	Harmonic Functions Theory	03
MAT-8029	Cosmology	03
MAT-8030	Bifurcation and Chaos	03

*Apart from this list, a student may also register in a course with M.Phil. class with the consent of his/her supervisor provided the student did not take this course already while doing M.Phil.

4.15: Details of the Courses/Contents

Course Code: MAT-8001

Title: Advanced Functional Analysis

Credit Hrs: 03

Course Outline: Normed Linear Spaces, Bounded Linear Transformation, Finite Dimensional Normed Linear Spaces, Some Dual Spaces, The Hahn Banach Theorem, The Algebra of Bounded Linear Operators, Baire's Theorem, The Principle of Uniform Boundedness, The Open Mapping Theorem, The Closed Graph Theorem, Hilbert Spaces, Spectral Theory in Hilbert Spaces, Hermitian Symmetric Forms, Orthogonality Self Adjoint Bounded Linear Operator, Spectrum of Bounded Linear Operators, Self Adjoint Bounded Linear Operators, Positive Operators, The Spectral Theorem

Text and Reference Books

1. L. Brown, *Elements of Functional Analysis*, Von Nostrand and Renihold Company, 1970.
2. E. Kreyszig, *Introduction to Functional Analysis with Applications*, John Wiley and Sons, New York, 1989.
3. A. Majeed, *Elements of Topological and Functional Analysis*, Ilmi Kitab Khana, 1994.
4. J. T. Oden, *Applied Functional Analysis*, Prentice Hall Inc, 1979.

Course Code: MAT-8002

Title: Advanced PDEs

Credit Hrs: 03

Course Outline: Cauchy's Problems for Linear Second Order Equation in N- Independent Variables, Cauchy Kowalewski Theorem, Characteristic Surface, Adjoint Operations, Bicharacteristics, Spherical and Cylindrical Waves, Heat Equations, Wave, Laplace and Diffusion Equations in Spherical and Cylindrical Polar Coordinates, Maximum-Minimum Principle, Non-Homogeneous Partial Differential Equations.

Text and Reference Books

1. C. B. Chester, *Techniques in Partial Differential Equations*, McGraw Hill Book Company, 1971.
2. R. Dennemyer, *Introduction to Partial Differential Equations and Boundary Value Problems*, McGraw Hill Book Company, 1968.
3. H. F. Weinberger, *A First Course in Partial Differential Equations: with Complex Variables and Transform Methods*, Dover Publications, 1995.
4. E. C. Zachmanoglou and D. W. Thoe, *Introduction to Partial Differential Equations with applications*, Dover Publications, 1987.

Course Code: MAT-8003

Title: Variational Inequalities

Credit Hrs: 03

Course Outline: Variational Inequalities in Fixed Points, The Characterization of the Projection onto a Convex Set, A First Theorem about Variational Inequalities, Some Problems about Variational Inequalities, Variational Inequalities in Hilbert Space, The Obstacle Problem, Variational Inequalities for Monotone Operators, A Variational Inequality with Mixed Boundary Conditions, Penalization

Text and Reference Books

1. C. Baiocchi and A. Capelo, *Variational and Quasivariational Inequalities*, Applications to Free Boundary Problems, John Wiley and Sons, New York, 1984.
2. G. Isac, *Complementarity Problems and Variational Inequalities*, Springer-Verlag, 2006.
3. D. Kinderlehrer and G. Stampacchia, *An Introduction to Variational Inequalities and Their Applications*, Academic Press, New York, 1980.
4. M. A. Noor, *Principles of Variational Inequalities*, Lambert Academic Publishing, Saarbrücken, Germany, 2009.

Course Code: MAT-8004

Title: Convex Analysis

Credit Hrs: 03

Course Outline: Affine Sets, Convex Sets and Cones, The Algebra of Convex Sets, Convex Functions, Functional Operations, Relative Interiors of Convex Sets, Closures of Convex Functions, Recession Cones and Unboundedness, Some Closedness Criteria, Continuity of Convex Functions, Separation Theorems, Conjugates of Convex Functions, Support Functions, Polars of Convex Sets, Polars of Convex Functions, Linear Inequalities, Directional Derivatives and Subgradients, Differential Continuity and Monotonicity, Differentiability of Convex Functions, The Legendre Transformation, The Minimum of a Convex Function, Ordinary Convex Programs and Lagrange

Text and Reference Books

1. G. G. M. IlyaeV and V. M. Tikhomirov, *Convex Analysis: Theory and Applications*, AMS, 2003.
2. R. T. Rockafellar, *Convex Analysis*, Princeton University Press, 1997.
3. J. V. Tiel, *Convex Analysis: An Introductory Text*, Wiley, 1984.
4. J. B. H. Urruty and C. Lemarechal, *Fundamentals of Convex Analysis*, Springer Verlag, 2001.

Code: MAT-7005

Title: Parameter Estimation and Sensitivity Analysis

Credit Hrs: 03

Course Outline:

Some Basic Notions from Probability Theory, Probability spaces, random variables and distribution functions, Expected value and variance, Normally distributed random variables, Some simple examples, Parameter Estimation, Problem formulation, First order necessary condition, Second order conditions, The expected value for the least squares estimator, The variance-covariance matrix for the least squares estimator Sensitivity Analysis, definition, classical sensitivity, Sensitivity equations, fisher information matrix.

Text and Reference Books

1. J. N. Kapur, *Mathematical Modelling*, New Age International, 01-jan-1988.
2. Sandip Banerjee, *Mathematical Modelling*, CRC press, 07-Feb-2014.
3. J. Berry and J. Stephen, *Mathematical Modelling*, PLC Great Britian 1995.
4. E. A. Bender, *Mathematical Modelling*, 1st Edition, Dover Publications, 2000.

Course Code: MAT-7006

Title: Semigroups in Geometric Functions Theory

Credit Hrs: 03

Course Outline: Holomorphic Functions and their Convergence, Metric Spaces and Fixed Point Principles, Schwarz-Pick Lemma and Automorphisms, Boundary Behavior of Holomorphic Self-Mappings and Fixed Points and Fixed Point Free Holomorphic Self-Mappings, The Denjoy-Wolff Theorem, Commuting Family of Holomorphic Mappings, Hyperbolic Geometry and Fixed Points, The Poincare Metric and its Compatibility with Convexity, Infinitesimal Poincare Metric and Geodesics, Fixed Points of Non-expansive Mappings

One-Parameter Continuous Semigroup of Holomorphic and Nonexpansive Self-Mappings, Infinitesimal Generator, Nonlinear Resolvent and the Exponential Formula, Monotonicity w.r.t the Hyperbolic Metric, Flow Invariance Conditions, The Berkson-Porta Parametric Representation of Semi-Complete Vector Fields, Asymptotic Behavior of Continuous Flows, Stationary Points of a Flow, Null Points of Complete Vector Fields, Embedding of Discrete Time Group and Rates of Convergence of a Flow with an Interior Stationary Point, A Rate of Convergence in Poincare Metric, Continuous Version of the Julia-Wolff-Caratheodory Theorem, Lower Bounds for Monotone Functions, Asymptotic behavior of Continuous Flows, Dynamical Approach to Starlike and Spirallike Functions

Text and Reference Books

1. Shoket, *Semigroups in Geometric Function Theory*, Kluwer Academic Publishers, 2001.
2. S. G. Krantz, *Geometric Function Theory: Explorations in Complex Analysis*, 2006th Edition, Birkhäuser, 2005.
3. G. Kohr, G. Graham and I. Graham, *Geometric Function Theory in One and Higher Dimensions*, 1st Edition, CRC Press, 2003.
4. L. V. Ahlfors, *Conformal Invariants: Topics in Geometric Function Theory*, McGraw-Hill Inc., US, 1973.

Course Code: MAT-8007 **Title:** Differential Subordination Theory and Applications **Credit Hrs:** 03

Course Outline: History, Definitions and Some Results, Integral Operators, Introduction to the Theory of Second-Order Differential Subordinations, Applications of First-Order Differential Subordinations, First- Order Linear Differential Subordinations, Briot-Bouquet Differential Subordinations and its Applications in Univalent Functions, Generalized Briot-Bouquet Differential Subordinations, Analytic Integral Operators between Classes of Functions, Subordination-Preserving Integral Operators, Applications of Second-Order Differential Subordinations, Second-Order Linear Differential Subordinations, Operators Preserving Functions with Positive Real Part and Bounded Functions, Averaging Integral Operators, The Schwarzian and Starlikeness, Special Differential Subordinations, Higher Order Differential Subordinations, Introduction to Differential Subordinations of Several Complex Variables

Text and Reference Books

1. P. L. Duren, *Univalent Functions*, Grundlehren der Math. Wissenschaften, Springer-Verlag, New York-Berlin, 1983.
2. S.S. Miller and P.T. Mocanu, *Differential Subordination Theory and Applications*, Marcel Dekker, Inc., New York, Basel, 2000.
3. E. D. Rainville, *Special Functions*, Brett Macmillan Compnay, 1960.
4. 5. C. Viola, *Special Functions*, 1st Edition, Springer, 2016.

Course Code: MAT-8008

Title: Conformal Mappings

Credit Hrs: 03

Course Outline: Conformal Mappings on Simply-connected Domains: Mapping Properties of Analytic Functions, The Linear Transformations, The Schwarz Lemma, The Symmetry Principle, The Schwarz-Christoffel Formula, Domains Bounded by Circular Arcs, The Kernel Functions, Conformal Mappings of Nearly Circular Domains

Mapping Properties of Special Functions: Rational Functions of Second Degree, Exponential and Trigonometric Functions, Elliptic Functions, Domains Bounded by Arcs of Confocal Conics, The Schwarzian δ -Functions, the Elliptic Modular Functions

Conformal Mappings on Multiply-Connected Domains: Cononical Domains and their Characterizations by Extremal Problems, Green's Function and the Dirichlet Problems, Area Problems, The Kernel Functions and the Orthonormal Sets

Text and Reference Books

1. L. Bieberbach, *Conformal Mappings*, Chelsea Publishing Company, 1964.
2. Z. Nehri, *Conformal Mappings*, Dover Publications, 1975.
3. I. I. Gikhman and A.V. Skorokhod, *Theory of Random Processes*, N. Moskow, 1973.
4. R. Schinzinger and P. A. A. Laura, *Conformal Mappings*, Dover Publications, 2003.

Course Code: MAT-8009

Title: Perturbation Methods

Credit Hrs: 03

Course Outline: Approximate Solution of Linear Differential Equations, Approximate Solution of Nonlinear Differential Equations, Singular Perturbation Theory Perturbation Methods for Linear Eigen Value Problems, Asymptotic Matching Boundary Layer Theory, Mathematical Structure of Boundary Layers, Inner, Outer, And Intermediate Limits Higher-Order Boundary, Layer Theory Distinguished Limits and Boundary Layers Validity of the WKB Approximation Patched Asymptotic Approximations, WKB Solution of Inhomogeneous Linear Quations, Matched Asymptotic Approximation, Solution of the One-Turning-Point Problem.

Text and Reference Books

1. A. H. Nayfeh, *Perturbation Methods*, 1st Edition, Wiley-VCH, 2000.
2. E. J. Hinch, *Perturbation Methods*, Cambridge University Press, 1991.
3. A. H. Nayfeh and D. T. Mook, *Nonlinear Oscillations*, Wiley-VCH, 1995,
4. A. H. Nayfeh, *Introduction to Perturbation Techniques*, 1st Edition, Wiley-VCH, 1993.

Course Code: MAT-8010

Title: Electro-dynamics

Credit Hrs: 03

Course Outline: Maxwell's Equations, Electrodynamics Wave Equations, Boundary Conditions, Wave in Conducting and Non-Conducting Media, Reflection and Polarization, Energy Density and Energy Flux, Lorntz Formula, Wave Guides and Cavity Resonators, Spherical and Cylindrical Waves, Inhomogeneous Wave Equations, Retarded Potentials, Lenard-Wiechart Potentials, Fields of Uniformly Moving Point Charge, Radiation From a Group of Moving Charges, Field of Oscillating Dipole, Field of an Accelerated Point Charge.

Text and Reference Books

1. D. Corson and P. Lorrain, *Introduction to Electromagnetic Fields and Waves*, Freeman, 1962.
2. J. D. Jacson, *Classical Electromagnetic*, 3rd Edition, Wiley, 1998.
3. K. Panofsky and M. Philips, *Classical Electricity and Magnetism*, Addison Wesley, 1962.
4. I. R. Retiz and F. J. Malford, *Foundation of Electromagnetic Theory*, Addison Wesley, 1969.

Course Code: MAT-8011

Title: Magneto-hydro-dynamics

Credit Hrs: 03

Course Outline: Basic Equations: Equations of Electrodynamics, Equations of Fluid Dynamics, Ohm's Law Equations of Magneto Hydrodynamics.

Motion of an Incompressible Fluid: Motion of a Viscous Electrically Conducting Fluid with Linear Current Flow, Steady State Motion along a Magnetic Field, Wave Motion of an Ideal Fluid

Small Amplitude MHD Waves: Magneto-Sonic Waves, Alfven's Waves, Damping and Excitations of MHD Waves, Characteristic Lines and Surfaces.

Simple Wave and Shock Wave in Magneto Hydrodynamics, Stability and Structure of Shock Waves in Relativistic Magneto Hydrodynamics, Stability and Structure of Shock Waves, Discontinuities in Various Quantities, Piston Problem, Oblique Shock Waves.

Text and Reference Books

1. A. Etal, *Plasma Electrodynamics*, Pergamon Press, 1975.
2. H. Alfven, *Cosmical Electrodynamics*, Create Space Independent Publishing Platform, 1950.
3. J. E. Anderson, *Magneto hydrodynamics*, Shock Waves, M. I. T. Press, Cambridge, 1963.
4. T. G. Cowling, *Magnetohydrodynamics*, Interscience Publishers, 1963.

Course Code: MAT-8012

Title: Fundamentals of Turbulence

Credit Hrs: 03

Course Outline: Introduction to turbulence, various types of turbulent flows, transition to turbulence from laminar flow. Navier-Stokes equations and turbulence. Statistical Tools: Statistical moments and correlations, probabilities and averaging, space and time scales of turbulence. Kolmogorov's Theory of turbulence, Intermittency.

Text and Reference Books:

1. Marcel Lesieur, *Turbulence in Fluids*, 4th edition, Springer, 2008.
2. J. Mathieu and J. Scott, *An Introduction to Turbulent Flow*, 1st edition, Cambridge University Press, 2000.
3. A. Tsinober, *An Informal Conceptual Introduction to Turbulent Flows*, 2nd edition, Springer, 2009.
4. P. A. Durbin and B. A. P. Reif, *Statistical Theory and Modeling for Turbulent Flows*, 2nd edition, John Wiley and Sons, Ltd., 2011.

Course Code: MAT-8013 **Title:** LIE Group Analysis of Differential Equations **Credit Hrs:** 03

Course Outline: Brief introduction to Lie group analysis of differential equations, preliminaries: heuristic approach in examples, finite differences and transformation groups in space of discrete variables, invariance of finite difference models, invariance difference models of ordinary differential equations, invariance difference models of partial differential equations, combined mathematical models and some generalizations, Lagrangian formalism for difference equations, Hamiltonian formalism for difference equations, symmetries and first integrals, discrete representation of ordinary differential equations with symmetries.

Text and Reference Books:

1. P.J Olver, *Application of Lie groups to Differential Equations*, Springer, New York, 1986.
2. S. Goldberge, *Introduction to Difference Equations*, John Wiley & Sons, New York, 1965.
3. V. Dorodnitsyn, *Applications of Lie Groups to Difference Equations*, CRC press, America, 2011.
4. A. Cohen, *An introduction to the Lie theory of one-parameter groups*, Ulan Press, 2012.
5. S. Elaydi, , *Introduction to Difference Equations*, 3rd edition, Springer, 2005.

Course Code: MAT-8014 **Title:** Selected Topics in Applied Mathematics **Credits:** 3

Course Outline: Course out lines of this course will be determined by the concerned teacher as per requirement of a student in connection with his/her research.

Course Code: MAT-8015 **Title:** Selected Topics in Pure Mathematics **Credit Hrs:** 03

Course Outline: Course out lines of this course will be determined by the concerned teacher as per requirement of a student in connection with his/her research.

Course Code: MAT-8016

Title: Numerical Solutions of PDEs

Credit Hrs: 03

Course Outline: Preliminaries, Classification of PDEs, Canonical Forms and Well-Posed Problems, Behavior of Solutions, Characteristics, Introduction to Finite Difference Methods
Basics of Finite Difference Approximations: Derivation of Finite Difference Approximations, Consistency, Stability, and Convergence for Difference Approximations, Lax Theorem, Matrix and Fourier Stability Analysis, Parabolic Equations: Explicit and Implicit Methods for the Heat Equation, Direction Splitting and ADI Schemes, Convection-Diffusion Equations
Hyperbolic Equations: Finite Difference Methods for the Wave Equation and High-Order Methods, First-Order Non-Linear Equations, Quasi-Linear and Conservation Forms, Characteristics, Shock Waves and Contact Discontinuities, Elliptic Equations: Dirichlet and Neumann Problems, Solvability, Direct vs. Iterative Methods of Solution

Text and Reference Books

1. R. J. LeVeque, *Finite Difference Methods for ODEs and PDEs*, SIAM, Philadelphia, 2007.
2. K. Morton and D. Mayers, *Numerical Solution of PDEs*, Cambridge University Press, 1994.
3. J. W. Thomas, *Numerical PDEs, Finite Difference Methods*, Springer-Verlag, 1995.
4. J. W. Thomas, *Numerical PDEs: Conservation Laws and Elliptic Equations*, Springer-Verlag, 1999.

Course Code: MAT-8017

Title: Design Methods for Control Systems

Credit Hrs: 03

Course Outline:

Introduction to Feedback Control Theory: Basic feedback theory, closed loop stability, stability robustness, frequency response design goals, loop shaping, limits of performance,
Classical Control System Design: Steady state error behavior, integral control, frequency response plots, classical control system design, lead, lag, and lag-lead compensation, the root locus approach to parameter selection, quantitative feedback theory,
Multivariable Control System Design: Poles and zeros of multivariable systems, MIMO structural requirements and design methods,
LQ, LQG, and H_2 Control System Design: LQ theory, LQG theory, H_2 optimization, feedback system design by H_2 optimization, examples and applications
Uncertainty Models and Robustness: parameter robustness analysis, the basic perturbation model, the small gain theorem, stability robustness of feedback systems, structured singular value robustness analysis, combined performance and stability robustness,
 H_∞ – optimization and μ -synthesis: The mixed sensitivity problem, the standard H_∞ problem, suboptimal solutions and examples, state space solutions of standard H_∞ problem, optimal solutions to the H_∞ problem, integral control and high frequency roll-off, μ -synthesis with applications,

Text and Reference Books:

1. O. H. Bosgra, H. Kwakernaak, and G. Meinsma, *Lecture Notes on Design Methods for Systems and Control*, Dutch Institute of Systems and Control, 2006 .
2. B. Friedland, *Control System Design: An Introduction to State-Space Methods*, Dover Publications, 2005.
3. J. Distifano, A. R. Stubberud and L. J. Williams, *Schaum's Outline of Feedback and Control Systems*, 2nd Edition, McGraw-Hill Education, 2013.
4. R. F. Stengel, *Optimal Control*, Dover Publications, 1994.

Course Code: MAT-8018

Title: Optimal State Estimation

Credit Hrs: 03

Course Outline: Least squares estimation, Wiener filtering, propagation of states and covariances for discrete and continuous time systems, the discrete and continuous time Kalman filters, the H-infinity filters, the extended and unscented Kalman filters.

Text and Reference Books

1. D. Simon, *Optimal State Estimation*, John Wiley & Sons, Inc, 2006.
2. J. L. Crassidis and J. L. Junkins, *Optimal Estimation of Dynamic Systems*, 2nd Edition, Chapman and Hall, 2011.
3. B. M. Mohan and S. K. Kar, *Continuous Time Dynamical Systems: State Estimation and Optimal Control with Orthogonal Functions*, CRC Press, 2012.
4. R. F. Stengel, *Optimal State Estimation*, Dover Publications, 1994.

Code: MAT-8019

Title: Linear Matrix Inequalities

Credit Hrs: 03

Course Outline: Basic Concepts: Convex Optimization and LMIs, Dissipative Dynamical Systems: Storage functions and quadratic supply rates, Kalman-Yakubovich-Popov Lemma, The Positive Real Lemma, and Bounded Real Lemma, interconnected dissipative systems, Stability and Nominal Performance: Review of Lyapunov stability, Generalized stability regions for LTI systems, the generalized plane concept, Quadratic, H-infinity, and H2 nominal performances, Control Synthesis: Analysis to synthesis – a general procedure, Performance Specifications: H-infinity design, positive real design, H2 problem, State feedback problems, Discrete Time Systems, Systems with Parametric Uncertainty: Affine parameter dependent systems, polytopic parameter dependent systems, Robust stability for autonomous systems: quadratic stability, quadratic stability of affine and polytopic models, parameter dependent Lyapunov functions,

Text and Reference Books

1. C. Scherer and S. Weiland, *Linear Matrix Inequalities in Control*, Dutch Institute of Systems and Control, 2006.
2. S. Boyd, L. E. Ghaoui, E. Feron and E. Balakrishnan, *Linear Matrix Inequalities in System & Control Theory*, SIAM, 1994.
3. R. Bhatia, *Matrix Analysis*, 1997 Edition, Springer, 1996.
4. F. Zhang, *Matrix Theory*, 2nd Edition, Springer, 2011.

Course Code: MAT-8020

Title: Advanced Probability Theory

Credit Hrs: 03

Course Outline: Probability review, convergence of sequences, characteristic function, transformation of random variables, discrete and continuous probability models, Sets, Indicator functions and classes of sets, measure space and probability space, measurable functions, integration theory and Lebasque measure

Text and Reference Books

1. Stirzaker, *Probability and Random Variables*, Cambridge University Press, 1999.
2. Stuart and O. K. Kendall's, *Advanced Theory of Statistics*, Vol. I, Charles Griffin, 1998.
3. Rohatgi, *Introduction to Probability Theory*, M. Graw Hill, 1976.
4. V. S. Borkar, *Probability Theory*, 1st Edition, Springer, 1995.

Course Code: MAT-8021 **Title:** Advanced Finite Mixture Distributions **Credit Hrs:** 03

Course Outline: Components of a Mixture: Various Informal and Formal Techniques of Determining the Number of Components of a Mixture, The Structure of Modality, Assessment of Modality. Discriminate Analysis. Sequential Problems and Procedure: Introduction to Unsupervised Learning Problems, Approximate Solutions to Unknown Mixing Parameters, Unknown Component Distribution Parameters, Unknown Mixing and Component Parameters and Dynamic Linear Models.

Texts and Reference Books

1. B. S. Everitt and D. J. Hand, *Finite Mixture Distribution*, Chapman and Hall London, 1981.
2. D. M. Titterington, A. F. M. Smith and U. E. Makov, *Statistical Analysis of Finite Mixture Distributions*, John Wiley and Sons, New York, 1985.
3. B. Everitt, *Finite Mixture Distributions (Monographs on Statistics and Applied Probability)*, Springer, 2011.
4. G. McLachlan and D. Peel, *Finite Mixture Models*, Wiley-Interscience, 2000.

Course Code: MAT-8022 **Title:** Advanced Sampling Techniques **Credit Hrs:** 03

Course Outline: Ratio and Regression Estimators with Application in Equal and Unequal Probabilities, Best Linear Unbiased Estimator (BLUE), Model Based Versus Design Based Estimator, Condition Under which Ratio Estimator Is BLUE, Derivation of Variance and Variance Estimator Under a Model for Ratio and Regression Estimator, Multistage Sampling, Derivation of Variance and Estimator for Equal and Unequal Probability Sampling for Two-Stage Sampling, Multistage Rules- Durbin's Rule, Raj's Rule, Raj's Modified Rule, Brewer-Hanif Rule.

Texts and Reference Books

1. W. G. Cochran, *Sampling Techniques*, John Wiley and Sons, New York, 3rd Edition, 1977.
2. I. Kish, *Survey Sampling*, John Wiley and Sons, New York, 1965.
3. D. Raj, *Design of Survey*, McGraw-Hill Book Company Ltd, New York, 1970.
4. D. Raj, *Sampling Theory*, Mc-Graw Hill, New York, 1968.

Course Code: MAT-8023

Title: Advanced Mathematical Statistics

Credit Hrs: 03

Course Outline: Probability Distributions, Weighted Probability Distributions, Transmuted probability Distributions, Convergence in Probability, Weak and Strong Law of Large number, Estimation theory, Constructing estimators ,Evaluating estimators , Hypothesis testing , Constructing decision rules , Evaluating testing procedures , Interval estimation , Constructing interval estimators , Evaluating interval estimators , Maximum likelihood large sample theory , Decision theory and Bayesian Statistics, Robust methods.

Text and Reference Books

1. G. Casella, and R. L. Berger, *Statistical Inference*, 2nd Edition, Duxbury, California, 2002.
2. W. Feller, *An introduction to Probability Theory and Its Applications*, 3rd Edition, (Volume I & II), John and Wiley Sons, New York, 2008.
3. J. O. Berger, *Statistical Decision Theory and Bayesian Analysis*, 2nd Edition, Springer, 2010.
4. M. Peterson, *An introduction to Statistical Decision Theory*, 1st edition, Cambridge University Press, 2009.

Course Code: MAT-8024

Title: Stochastic Differential Equations

Credit Hrs: 03

Course Outline: Brief Introduction to Diffusion Processes and How They Arise as Natural Approximations to Certain Discrete Processes, Review of Some Basic Facts about Brownian Motion and Martingales, ITO Stochastic Integrals Construction and Martingale Properties, ITO's Formula, Integration by Parts, Comparison with Stieltjes Integrals and Ordinary Calculus, Stochastic Differential Equations, Existence and Uniqueness of Solutions, Markov Property, Generators, Martingale Problem Characterization of Weak Solutions, Diffusion Processes, Dynkin's Formula, Calculations of Expectations and Probabilities, Converting to the Natural Scale, Stationary Distributions, Examples from Biology: Wright-Fisher Diffusions, Branching Diffusions

Text and Reference Books

1. K.L. Chung and R. J. Williams, *Introduction to stochastic integration*, Second Ed., Probability and its Applications, Birkhauser Boston Inc., MA, 1990.
2. S. Karlin and H. Taylor, *A Second Course in Stochastic Processes*, 1st Edition, Academic Press, 1981.
3. F. C. Klebaner, *Introduction to Stochastic Calculus with Applications*, 3rd Edition, Imperial College Press, 2012.
4. D. Richard, *Stochastic calculus: A practical introduction*, 1st Edition, CRC Press, 1992.

Course Code: MAT-8025

Title: Fixed Point Theory and Applications

Credit Hrs: 03

Course Outline: Lipschitzian, Contraction, Contractive and Non-Expansive Mappings, Banach's Contraction Principle with Application to Differential and Integral Equations, Brouwer's Fixed Point Theorem with Applications, Schauder's Fixed Point Theorem with Applications, Uniformly Convex and Strictly Convex Spaces, Properties of Non-Expansive Mappings, Extension's of Banach's Contraction Principle

Text and Reference Books

1. A. Granas and J. Dugundji, *Fixed Point Theory*, 2003 Edition, Springer, 2003.
2. R. P. Agarwal, D. O. Regan and D. R. Sahu, *Fixed Point Theory for Lipschitzian-type mappings with applications*, Springer-Verlag, USA.
3. R. P. Agarwal, *Fixed Point Theory and Applications*, Cambridge University Press, 2006.
4. V. I. Istratescu, *Fixed Point Theory: (Mathematics and Its Applications)*, 1st edition, 2001.

Course Code: MAT-8026

Title: Integral Inequalities

Credit Hrs: 03

Course Outline: Some Quadrature Rules and Their Applications Ostrowski Inequality in L_1 And L_p - and L_∞ Spaces and Applications Gruss Inequality, Its Variant and Applications Ostrowski – Gruss Inequalities, Their Consequences and Applications Perturbed Results for Ostrowski and Ostrowski-Gruss Type Inequalities for Convex Functions, Hadmard, Sinequality, Hadmard,S Inequality for Convex Functions and Applications.

Text and Reference Books

1. S. Dragomir and T. M. Rassias, *Ostrowski Type Inequalities and Applications in Numerical Integration*, 2002 Edition, Springer, 2002.
2. G. A. Anastassiou, *Advanced Inequalities*, World Scientific Publishing Company, Singapore. 2011.
3. D. D. Bainov and P.S. Simeonov, *Integral Inequalities and Applications*, 1st Edition, Springer, 1992.
4. D. S. Mitrinovic, J. Picarcic and A.M Fink, *Inequalities Involving Functions and Their Integrals and Derivatives*, 1991 Edition, Springer, 1991.

Course Code: MAT-8027

Title: Banach Algebras

Credit Hrs: 03

Course Outline: Banach Algebra: Ideals, Homeomorphisms, Quotient Algebra, Wiener's Lemma, Gelfand's Theory of Commutative Banach Algebras: The Notions of Gelfand's Topology, Radicals Gelfand's Transforms.

Basic Properties of Spectra, Gelfand-Mazur Theorem and Symbolic Calculus of A-Valued Functions, Normed Rings, Gelfand-Naimark Theorem.

Text and Reference Books

1. M.A. Naimark, *Normed Algebras*, Wolters Noordhoff Publishing Groningen, Netherlands, 1972.
2. C. E. Rickart, *Banach Algebras*, D Van Nostrand Company Inc. NewYork , 1960.
3. W. Rudin, *Functional Analysis*, McGraw Hill, Inc, New York, 1989.
4. W. Zelazko, *Banach Algebras*, American Elsevier Publishing Company Inc, New York, 1973.

Code: MAT-8028

Title: Harmonic Functions Theory

Credit Hrs: 03

Course Outline: Definition and Examples, Invariance Properties, The Mean-Value Property, The Maximum Principle, The Poisson Kernel, The Dirichlet Problem, Converse of the Mean-Value Property, Real Analyticity and Homogeneous Expansions, Bounded Harmonic Functions Related Properties, Positive Harmonic Functions Related Properties, The Kelvin Transforms, Harmonic Polynomials, Harmonic Hardy Spaces, Harmonic Functions on Half-Spaces, Harmonic Bergman Spaces, The Decomposition Theorem, Annular Regions, The Dirichlet Problem and Boundary Behavior

Text and Reference Books

1. S. Axler, P. Bourdon, W. Ramey, *Harmonic Function Theory*, 2nd Edition, Springer, 2001.
2. S. Bergman, *The Kernel Function and Conformal Mapping*, American Mathematical Society, 1950
3. L. L. Helms, *Introduction to Potential Theory*, Wiley-Inter science, 1969.
4. O. D. Kellogg, *Foundations of Potential Theory*, Springer, 1929.

Course Code: MAT-8029

Title: Cosmology

Credit Hrs: 03

Course Outline: Review of Relativity, Historical Background, Astronomy, Astrophysics, Cosmology, The Cosmological Principle and its Strong Form, The Einstein and Desitter Universe Models, Measurement of Comic Distance, The Hubble Law and the Friedmann Models, Steady State Models, The Hot Big Bang Models, The Inicrowave Background, Discussion of Significance of a Start of Time, Fundamentals of High Energy Physic, The Chronology and Composition of the Universe, Non-Brayonic Dark Matter, Problems of the Standard Model of Cosmology, Bianch Space-Times, Mixmaster Models, Inflationary Cosmology, Further Development of Inflationary Models, Kaluza-Klein Cosmologies, Review of Material.

Text and Reference Books

1. L. F. Abbott and S. Y. Pi, *Inflationary Cosmology*, World Scientific, 1986.
2. E.W. Kolb and M. S. Turner *The Early Universe*, Addison Wesley, 1990.
3. P. J. E. Peebles, *Principles of Physical*, Princeton University Press, 1993.
4. Ryan M. P. Jr. and Shepley, *Homogeneous Relativistic Cosmologies*, Princeton University Press, 1975.

Course Code: MAT- 8030

Bifurcation and Chaos

Credit Hrs: 3

Course Outlines: Modeling with Nonlinear Systems of ODEs, Stability and Bifurcation Theory, The Hopf bifurcation and limit cycles, .Homoclinic & Heteroclinic Orbits and Mel'nikov Theory, Stability, Bifurcation and Chaos in I-dimensional Maps. Period doubling, Feigenbaum's Approach to Chaos, Properties of Chaos. The Lorenz Equations

Text and Reference Books:

1. S. Strogatz, *Nonlinear Dynamics, and Chaos: With Applications to Physics, Biology, Chemistry and Engineering*, 2nd Edition, Westview Press, 2014.
2. P. Glendinning, *Stability, Instability and Chaos*, 1st edition, Cambridge University Press, 1994.
3. R. Hillborn, *Nonlinear Dynamics and Chaos*, 2nd edition, Oxford University Press, 2001.
4. J. Ohtsubu, *Stability, Instability and Chaos*, 3rd edition, Springer, 2012.

5. Approval for the Updated Lists of External Examiners for Comprehensive Oral Exams of BS and MSc students, Thesis/Project Evaluation of BS, M.Sc, M.Phil and PhD Programs

5.1 List of External Examiners for Comprehensive Oral Examinations and Projects/Thesis Evaluation of BS / M.Sc

1. Prof. Dr. Muhammad Shafique Baig
Department of Mathematics, University of South Asia, Lahore
E-mail:
Cell: 0300 4846438
2. Prof. Dr. Muhammad Mushtaq
Chairman, Department of Mathematics, UET, Lahore
E-mail: mmushtaq@uet.edu.pk
Cell: 0300 9611187
3. Prof. Dr. Muhammad Ozair Ahmad
Chairman, Department of Mathematics, UoL, Lahore
E-mail:
Cell: 0336 4162538
4. Dr. Muhammad Arif
Assistant Professor, Department of Mathematics,
Abdul Wali Khan University, Mardan
E-mail:
Cell: 0313 5176926
5. Dr. Wasim-ul-Haq
Assistant Professor, Department of Mathematics,
Abdul Wali Khan University, Mardan
E-mail:
Cell: 0322 5227802
6. Dr. Ibrar Hussain
Assistant Professor, Department of Mathematics, NUST, Islamabad
E-mail:
Cell: 0334 5039452
7. Dr. Asif Malik
Assistant Professor, Department of Mathematics,
HITEC University, Taxila
E-mail:
Cell: 0334 5256266

8. Dr. Saira Zanib Butt
Assistant Professor, Department of Mathematics,
HITEC University, Taxila
E-mail:
Cell: 0332 5193283
9. Dr. Farooq Ahmed Shah
Assistant Professor, Department of Mathematics, CIIT, Attock
E-mail:
Cell: 0334 5490567
10. Dr. Asim Naseem
Assistant Professor, Department of Mathematics, GCU Lahore
E-mail:
Cell: 0321 4539597
11. Dr. Kashif Shafique
Department of Mathematics, GCU Faisalabad
E-mail:
Cell: 0321 4866779
12. Dr. Mohsin Raza Chaudary
Assistant Professor, Department of Mathematics, GCU Faisalabad
E-mail:
Cell: 0333 6523141
13. Dr. Bushara Malik
Assistant Professor, Department of Mathematics, CIIT, Islamabad
E-mail:
Cell: 0333 5067889
14. Dr. SaleemUllah
Assistant Professor, Federal Education Department, Islamabad
E-mail:
Cell: 0333 5452314
15. Dr. Sarfraz Nawaz
Assistant Professor, Department of Mathematics, GCU Faisalabad
E-mail:
Cell: 0300 7226094

16. Dr. Muhammad Wasim
Assistant Professor, Department of Mathematics, CIIT, Sahiwal
E-mail:
Cell: 0333 6346907
17. Dr. Hani Shaker
Assistant Professor, Department of Mathematics, CIIT, Lahore Campus
E-mail:
Cell: 0321 4120429
18. Dr. Qammar ud Din
Assistant Professor, Department of Mathematics, UAJK Muzaffarabad
E-mail:
Cell: 0300 3964842
19. Prof. Dr. Siraj ul Islam
Department of Basic Sciences, UET Peshawar,
Email: siraj.islam@gmail.com
Cell: 0345-9669495
20. Dr Saifullah Khalid
Associate Professor, Department of Mathematics, GCU, Lahore
Email: dr.saifullah@gcu.edu.pk
Cell: 0300-5858233
21. Dr. Ahmer Mehmood
Assistant Professor, Department of Maths & Stats,
International Islamic University, Islamabad
Email: ahmerqau@yahoo.co.uk, ahmer.mehmood@iiu.edu.pk
Cell # 0333 5171013
22. Dr. Nasir Ali
Assistant Professor, Department of Maths & Stats,
International Islamic University, Islamabad
Email: nasirali_qau@yahoo.com, nasir.ali@iiu.edu.pk
Cell # 0333 5252565
23. Dr. Tariq Javed
Assistant Professor, Department of Maths & Stats,
International Islamic University, Islamabad
Email: tariq_17pk@yahoo.com, tariq.javed@iiu.edu.pk
Cell # 0300 5283773

24. Dr. Sajid Ali
Assistant Professor, Dept. of Basic Sciences, SEECS,
National University of Science and Technology Islamabad
Email: sajid_ali@mail.com, sajid.ali@seecs.nust.edu.pk
Phone: +92 51 90852358
25. Dr. Muhammad Ayub
Assistant Professor, Department of Mathematics, CIIT, Abbottabad.
Email: muhhammad_ayub5@hotmail.com, ayub@ciit.net.pk
Cell No: 0302 8920677
26. Dr. Fayyaz Ahmad
Assistant Professor, University of Gujrat,
Email: dr.fayyaz@uog.edu.pk
Phone: +92 53 3643112 (Ext. 217)
27. Mr. Mirza Naveed Shahzad
Lecturer, University of Gujrat,
Phone: +92 (53) 3643112 (Ext. 217)
Email: nvd.shzd@uog.edu.pk
28. Prof. Dr. Muhammad Aslam
Ripha International University, Islamabad
E-mail:
Cell #: 0300 5191826
29. Dr. Zahid Asghar
Assistant Professor, QAU, Islamabad,
Email: g.zahid@gmail.com
Phone: +92-51-90642184
30. Prof. Dr. Javid Shabbir
QAU, Islamabad,
Email: javidshabbir@gmail.com
Phone: +92-51-90642184,
31. Dr. Ishfaq Ahmad
Assistant Professor, IIU, Islamabad,
Email: ishfaq.ahmad@iiu.edu.pk
Phone: +92-51-9019733

32. Dr. Muhammad Azam
Associate Professor, University of VAS, Lahore,
Email: mazam@uvas.edu.pk
Cell #: 0322-5508700,
33. Dr. Kamran Abbas
Assistant Professor, UAJ&K Muzaffarabad,
Email: kamiuajk@yahoo.com
Cell #: 0312-9217669
34. Dr. Azhar Saleem
Associate Professor, UAJ&K Muzaffarabad,
Cell #: 0306-7120441,
Email: drazharsaleem@yahoo.com
35. Dr Malik Muhammad Yousaf
Associate Professor, Department of Mathematics,
Quaid-e-Azam University, Islamabad
Cell #: 0300-9696401
36. Dr. Masood Khan
Associate Professor, Department of Mathematics,
Quaid-e-Azam University, Islamabad
Cell #: 0300-9705550
37. Dr. Saghir Ahmad
Associate Professor, Department of Mathematics,
Muhammad Ali Jinnah University, Islamabad
Cell #: 0332-5150889
38. Dr. Shafqat Hussain
Assistant Professor, Department of Mathematics,
Muhammad Ali Jinnah University, Islamabad
Cell #: 0300-5080308
39. Dr. Siraj ul Haq
Associate Professor, Faculty of Engineering Sciences,
GIK Institute of Engineering Sciences and Technology, Topi
Cell #: 0334-9334599
40. Dr. Amer Qureshi
Assistant Professor, Faculty of Engineering Sciences,
GIK Institute of Engineering Sciences and Technology, Topi
Email: amergikian@yahoo.com
Cell:

41. Dr Matloob Anwar
Assistant Professor, School of Natural Sciences,
NUST, Rawalpindi
Cell #: 0333-5185778
- 41- Dr. Muhammad Asad Meraj
Associate Professor, Department of Mathematics,
CIIT, Sahiwal Campus
asad@ciitsahiwal.edu.pk
Cell: 03334301971
1. Dr. Najma Abdul Rehman
Assistant Professor, Department of Mathematics, CIIT, Sahiwal Campus
E-mail: Najma.ar@hotmail.com
Cell: 00923016924302
2. Dr. Mustafa Habib
Assistant Professor, Department of Mathematics, UET Lahore
E-mail:
Cell: 03467221027
3. Dr. Shabieh Farwa
Assistant Professor, Department of Mathematics, CIIT, Wah Cantt
E-mail: drsfarwa@gmail.com
Cell: +92 336 0994078
4. Dr. Muhammad Munir
Associate Professor, Department of Mathematics,
Govt post Graduate College Abbottabad.
E-mail: Dr.muhammadmunir@gmail.com
Cell: +92 347 9556209
5. Dr. Muhammad Muddassar
Assistant Professor, Department of Basic Sciences and Humanities, UET Taxila.
E-mail: Malik.muddassar@gmail.com
Cell: +92 333 4365878
6. Dr. Muhammad Umer Saleem
Assistant Professor, Department of Mathematics, Education University Lahore
E-mail: umerlinks@hotmail.com
Cell: +92 300 4251923

7. Dr. Muhammad Munir Butt
Assistant Professor, Department of Mathematics, UoL, Lahore
E-mail: Buttlahore@yahoo.com
Cell:
8. Dr. Azeem Shahzad
Lecturer, Department of Basic Sciences and Humanities, UET Taxila
E-mail:
Cell: +92 300 8540963
50. Dr. Nasir Siddiqui
Assistant Professor, Department of Basic Sciences and Humanities, UET Taxila
E-mail:
Cell: +92 300 5323393
51. Prof. Dr. Malik Muhammad Yousaf
Professor (Tenured) and Chairman, Department of Mathematics, QAU Islamabad
E-mail: drmymalik@hotmail.com
52. Prof. Dr. Tasawar Hayat
Professor (Tenured), Department of Mathematics, QAU Islamabad
E-mail: fmgpak@gmail.com
Cell: 05190642172
53. Prof. Dr. Sohail Nadeem
Professor (Tenured), Department of Mathematics, QAU Islamabad
E-mail: snqau@hotmail.com
Cell: 03005117317
54. Dr. Azad Hussain
Assistant Professor, Department of Mathematics, University of Gujrat
E-mail: azad.hussain@uog.edu.pk
55. Dr. Rizwan Ul Haq
Assistant Professor, Department of Mathematics, Bahria University Islamabad
E-mail: rulhaq@uwo.ca
Cell: 03005432771
56. Dr. Umer Farooq
Assistant Professor, Department of Mathematics, COMSATS, Islamabad
E-mail: umer_farooq@comsats.edu.pk
Cell: 0334 5511778

57. Dr. Muhammad Ayub
Assistant Professor, Department of Mathematics, COMSATS, Abbotabad,
E-mail: Muhammad_ayub5@hotmail.com
Cell: 0302 8920677
58. Dr. Abdul Qadeer Khan
Assistant Professor, Department of Mathematics, UAJ&K Muzaffarabad,
E-mail: abdulqadeerkhan1@gmail.com
Cell: 0344 5102758
59. Prof. Dr. Muhammad Naeem Qureshi
Professor (Rtd), Department of Mathematics, UAJ&K, Registrar AIOU Islamabad,
E-mail: nqureshi58@gmail.com
Cell: 0300 4746083

5.2 External Examiners for M.Phil Thesis Evaluation

1. Prof. Dr. Muhammad Shafique Baig
Department of Mathematics, University of South Asia, Lahore
E-mail:
Cell:
2. Prof. Dr. Muhammad Aslam Noor
Department of Mathematics, CIIT, Islamabad
E-mail:
Cell:
3. Prof. Dr. Khalida Inayat Noor
Department of Mathematics, CIIT, Islamabad
E-mail:
Cell:
4. Prof. Dr. Muhammad Ayub,
Department of Mathematics, Quaid-i-Azam University, Islamabad.
E-mail:
Cell:
5. Prof. Dr. Muhammad Ozair Ahmad
Chairman, Department of Mathematics, UoL, Lahore
E-mail:
Cell:
6. Prof. Dr. Shahid Siddiqi,
Director General, SMS, GCU, Lahore
E-mail:
Cell:
7. Prof. Dr. Tousif Mohi-Ud-Din
Department of Mathematics, HITEC University, Taxila
E-mail:
Cell:
8. Prof. Dr. Tasawar Hayat,
Chairman, Department of Mathematics, Quaid-i-Azam University, Islamabad
E-mail:
Cell:

9. Prof. Dr. Muhammad Mushtaq
Chairman, Department of Mathematics, UET, Lahore
E-mail:
Cell: 0300-9611187
10. Dr. Malik Muhamamd Yousaf
Associate Professor, Department of Mathematics, Quaid-i-Azam University, Islamabad
E-mail:
Cell:
11. Dr. Tariq Shah
Associate Professor, Department of Mathematics, Quaid-i-Azam University Islamabad
E-mail:
Cell:
12. Prof. Dr. Iftikhar Mughal
Department of Mathematics, UAJK, Muzaffarabad
E-mail:
Cell:
13. Prof. Dr. Siraj ul Islam
Department of Basic Sciences, UET Peshawar,
Email: siraj.islam@gmail.com
Cell: 0345-9669495
14. Dr. Salman Ahmad
Assistant Professor
Department of Applied Mathematics & Statistics, IST, Islamabad
Email: salman.ahmad@ist.edu.pk
Cell: 0300-6335482
15. Dr. Saifullah Khalid
Associate Professor, Department of Mathematics, GCU, Lahore
Email: dr.saifullah@gcu.edu.pk
Cell: 0300-5858233
16. Dr. Muhammad Arif
Assistant Professor, Department of Mathematics, Abdul Wali Khan University, Mardan
E-mail:
Cell: 0313 5176926
17. Dr. Wasim ul Haq
Assistant Professor, Department of Mathematics, Abdul Wali Khan University, Mardan
E-mail:
Cell: 0322 5227802

18. Dr. Ibrar Hussain
Assistant Professor, Department of Mathematics, NUST, Islamabad
E-mail:
Cell: 0334 5039452
19. Dr. Asif Malik
Assistant Professor, Department of Mathematics, HITEC, University Taxila
E-mail:
Cell: 0334 5256266
20. Dr. Saira Zanib Butt
Assistant Professor, Department of Mathematics, HITEC University Taxila
E-mail:
Cell: 0332 5193283
21. Dr. Farooq Ahmed Shah
Assistant Professor, Department of Mathematics, CIIT, Attock
E-mail:
Cell: 0334 5490567
22. Dr. Asim Naseem
Assistant Professor, Department of Mathematics, GCU Lahore
E-mail:
Cell: 0321 4539597
23. Dr. Kashif Shafique
Department of Mathematics, GCU, Faisalabad
E-mail:
Cell: 0321 4866779
24. Dr. Mohsin Raza Chaudary
Assistant Professor, Department of Mathematics, GCU, Faisalabad
E-mail:
Cell: 0333 6523141
25. Dr. Bushara Malik
Assistant Professor, Department of Mathematics, CIIT, Islamabad
E-mail:
Cell: 0333 5067889
26. Dr. SaleemUllah
Assistant Professor, Federal Education Department, Islamabad
E-mail:
Cell: 0333 5452314

27. Dr. Sarfraz Nawaz
Assistant Professor, Department of Mathematics, GCU, Faisalabad
E-mail:
Cell: 0300 7226094
28. Dr. Muhammad Wasim
Assistant Professor, Department of Mathematics, CIIT, Sahiwal
E-mail:
Cell: 0333 6346907
29. Dr. Hani Shaker
Assistant Professor, Department of Mathematics, CIIT, Lahore
E-mail:
Cell: 0321 4120429
30. Dr. Qammar ud Din
Assistant Professor, Department of Mathematics, UAJK, Muzaffarabad
E-mail:
Cell: 0300 3964842
31. Dr. Ahmer Mehmood
Assistant Professor, Department of Maths & Stats, International Islamic University, Islamabad

Email: ahmerqau@yahoo.co.uk, ahmer.mehmood@iiu.edu.pk
Cell # 03335171013
32. Dr. Nasir Ali
Assistant Professor, Department of Maths & Stats, International Islamic University, Islamabad
Email: nasirali_qau@yahoo.com, nasir.ali@iiu.edu.pk
Cell # 0333 5252565
33. Dr. Tariq Javed
Assistant Professor, Department of Maths & Stats, International Islamic University Islamabad
Email: tariq_17pk@yahoo.com, tariq.javed@iiu.edu.pk
Cell # 0300 5283773
34. Dr. Sajid Ali
Assistant Professor, Dept. of Basic Sciences, SEECS, NUST, Islamabad
Email: sajid_ali@mail.com, sajid.ali@seecs.nust.edu.pk
Phone: +92 51 90852358
35. Dr. Muhammad Ayub
Assistant Professor, Department of Mathematics, CIIT, Abbottabad.
Email: muhammad_ayub5@hotmail.com, ayub@ciit.net.pk
Cell No: 0302 8920677

36. Dr. Fayyaz Ahmad
Assistant Professor, University of Gujrat,
Email: dr.fayyaz@uog.edu.pk
Phone: +92 53 3643112 (Ext. 217)
37. Mr. Mirza Naveed Shahzad
Lecturer, University of Gujrat,
Email: nvd.shzd@uog.edu.pk
Phone: +92 53 3643112 (Ext. 217)
38. Prof. Dr. Muhammad Aslam
Ripha International University, Islamabad,
E-mail:
Cell #: 03005191826
39. Dr. Zahid Asghar
Assistant Professor, Quaid-i-Azam University, Islamabad,
Email: g.zahid@gmail.com
Phone: +92-51-90642184,
40. Prof. Dr. Javid Shabbir
Quaid-i-Azam University, Islamabad,
Email: javidshabbir@gmail.com
Phone: +92-51-90642184,
41. Dr. Ishfaq Ahmad
Assistant Professor, International Islamic University, Islamabad,
Email: ishfaq.ahmad@iiu.edu.pk
Phone: +92-51-9019733
42. Dr. Muhammad Azam
Associate Professor, University of VAS, Lahore,
Email: mazam@uvas.edu.pk
Cell #: 0322-5508700,
43. Dr. Kamran Abbas
Assistant Professor, UAJ&K, Muzaffarabad,
Email: kamiujk@yahoo.com
Cell #: 0312-9217669,
44. Dr. Azhar Saleem
Associate Professor, UAJ&K, Muzaffarabad,
Email: drazharsaleem@yahoo.com
Cell #: 0306-7120441,

45. Dr Malik Muhammad Yousaf
Associate Professor, Department of Mathematics, Quaid-e-Azam University, Islamabad
E-mail:
Cell #: 0300-9696401
46. Dr Masood Khan
Associate Professor, Department of Mathematics, Quaid-e-Azam University, Islamabad
E-mail:
Cell #: 0300-9705550
47. Dr Saghir Ahmad
Associate Professor, Department of Mathematics, Capital University, Islamabad
E-mail:
Cell #: 0332-5150889
48. Dr Shafqat Hussain
Assistant Professor, Department of Mathematics, Capital University, Islamabad
E-mail:
Cell #: 0300-5080308
49. Dr. Siraj ul Haq
Associate Professor, Faculty of Engineering Sciences, GIK Institute of Engineering Sciences
and Technology, Topi
E-mail:
Cell #: 0334-9334599
50. Dr. Amer Qureshi
Assistant Professor, Faculty of Engineering Sciences, GIK Institute of Engineering Sciences
and Technology, Topi
Email: amergikian@yahoo.com
Cell:
51. Dr Matloob Anwar
Assistant Professor, School of Natural Sciences, NUST, Rawalpindi
E-mail:
Cell #: 0333-5185778
52. Dr. Muhammad Asad Meraj
Associate Professor, Department of Mathematics, CIIT, Sahiwal
E-mail: asad@ciitsahiwal.edu.pk
Cell: 0324 9825404

53. Dr. Najma Abdul Rehman
Assistant Professor, Department of Mathematics, CIIT, Sahiwal
E-mail: Najma.ar@hotmail.com
Cell: +92 301 6924302
54. Dr. Shabieh Farwa
Assistant Professor, Department of Mathematics, CIIT, Wah Cantt
E-mail: drsfarwa@gmail.com
Cell: +92 336 0994078
55. Dr. Muhammad Munir
Associate Professor, Department of Mathematics, Govt post Graduate College Abbottabad.
E-mail: drmuhammadmunir@gmail.com
Cell: +92 347 9556209
56. Dr. Mustafa Habib
Assistant Professor, Department of Mathematics, UET Lahore
E-mail:
Cell: 0346 7221027
57. Dr. Muhammad Muddassar
Assistant Professor, Department of Basic Sciences and Humanities UET, Taxila.
E-mail: Malik.muddassar@gmail.com
Cell: + 92 333 4365878
58. Dr. Muhammad Umer Saleem
Assistant Professor, Department of Mathematics, Education University, Lahore
E-mail: umerlinks@hotmail.com
Cell: +92 300 4251923
59. Dr. Muhammad Munir Butt
Assistant Professor, Department of Mathematics, University of Lahore
E-mail: Buttlahore@yahoo.com
Cell:
60. Dr. Azeem Shahzad
Lecturer, Department of Basic Sciences and Humanities, UET, Taxila
E-mail:
Cell: + 92 300 8540963
61. Dr. Nasir Siddiqui
Assistant Professor, Department of Basic Sciences and Humanities, UET Taxil
E-mail:
Cell: + 92 300 5323393

62. Dr Muhammad Riaz
Assitant Professor, Department of Mathematics, University of the Punjab, Lahore
Email: mriazpu@gmail.com
Cell: 0300 4012299
60. Prof. Dr. Tahir Mahmood
Department of Mathematics, Islamia University Bahawalpur, Bahawalpur
E-mail:
Cell: 0307 6321017
61. Prof. Dr. Ghulam Muhammad
Department of Mathematics, Govt College Civil Lines, Lahore
E-mail: chgm2004@yahoo.com
Cell: 0312 4602628
58. Prof. Dr. Malik Muhammad Yousaf
Professor (Tenured) and Chairman, Department of Mathematics, QAU Islamabad
E-mail: drmymalik@hotmail.com
51. Prof. Dr. Tasawar Hayat
Professor (Tenured), Department of Mathematics, QAU Islamabad
E-mail: fmgpak@gmail.com
Cell: 051-90642172
52. Prof. Dr. Sohail Nadeem
Professor (Tenured), Department of Mathematics, QAU Islamabad
E-mail: snqau@hotmail.com
Cell: 0300-5117317
53. Dr. Azad Hussain
Assistant Professor, Department of Mathematics, University of Gujrat
E-mail: azad.hussain@uog.edu.pk
54. Dr. Rizwan Ul Haq
Assistant Professor, Department of Mathematics, Bahria University Islamabad
E-mail: rulhaq@uwo.ca
Cell: 03005-432771
55. Dr. Umer Farooq
Assistant Professor, Department of Mathematics, COMSATS, Islamabad
E-mail: umer_farooq@comsats.edu.pk
Cell: 0334 5511778

56. Dr. Muhammad Ayub
Assistant Professor, Department of Mathematics, COMSATS, Abbotabad,
E-mail: Muhammad_ayub5@hotmail.com
Cell: 0302 8920677
57. Dr. Abdul Qadeer Khan
Assistant Professor, Department of Mathematics, UAJ&K Muzaffarabad,
E-mail: abdulqadeerkhan1@gmail.com
Cell: 0344 5102758
58. Prof. Dr. Muhammad Naeem Qureshi
Professor (Rtd), Department of Mathematics, UAK&K, Registrar AIOU Islamabad,
E-mail: nqureshi58@gmail.com
Cell: 0300 4746083

5.3 Adjunct Faculty:

1. Prof. Dr. Muhammad Naeem Qureshi Retd from Department of Mathematics, UAJ&K, Registrar AIOU, Islamabad.
2. Dr. Abdul Qadeer Khan, Assistant Prof. Department of Mathematics, UAJ&K, Muzaffarabad.

5.4 External Examiners for PhD Thesis Evaluation

(a) International

1. Prof. Dr. G. J. Olsder
Professor Emeritus, Delft Institute of Applied Mathematics,
Area of Instest: Dynamic Games, Mathematical Systems Theory
Delft University of Technology, Delft, The Netherlands
Email: G.J.Olsder@tudelft.nl
2. Prof. Dr. J. W. van der Woude
Associate Professor, Delft Institute of Applied Mathematics,
Delft University of Technology, Delft, The Netherlands
Area of Instest: Max-Plus Algebra, Mathematical Systems Theory
Email: J.W.vanderWoude@tudelft.nl
3. Dr. A. Doria Cerezo
Assistant Professor,
Department of Electrical Engineering and Institute of Industrial and Control Engineering,
Universitat Politècnica de Catalunya, Barcelona, Spain
Area of Instest:
Email: arnau.doria@upc.edu
4. Dr. P. Gunther,
Department of Mathematics and Scientific Computing,
Uni Graz, Heinrichstraße 36, 8010 Graz, Austria
Area of Instest: Shape Otimization Problem, Free Boundar Value Problems, Control Partial
Differential Equations, Ficitius Domain method for Partial Differentail Equations.
E-mail: gunther.peichl@uni-graz.at
Phone: 43 380316-5619
5. Prof. Dr. G. Propst,
Department of Mathematics and Scientific Computing
Uni Graz, Heinrichstraße 36, 8010 Graz, Austria
Area of Instest: Valveless Pumping: nonlinear dynamics with ODEs, Functional Analytic Method
for linear Hyperbolic problem with Memory, Nonlinear hyperbolic System of Conservation Laws
Email: georg.propst@uni-graz.at
Phone: +43 316 380 - 5168
6. Prof. Dr. D. W. Ring,
Department of Mathematics and Scientific Computing
Uni Graz, Heinrichstraße 36, 8010 Graz, Austria
Area of Instest: Optimal Control and Inverse Problems
Email: wolfgang.ring@uni-graz.at

Phone: +43 316 380 – 5161

7. Prof. Dr. J. Batzel,
Department of Mathematics and Scientific Computing
Uni Graz, Heinrichstraße 36, 8010 Graz, Austria
Area of Interest: Functional Differential Equations: stability analysis for differential equations with delay, delay differential equation applications, Medical Applications: modeling of the respiratory and cardiovascular systems in humans, modeling apnea in infants, modeling sleep physiology in humans, hemorrhage and transfusion design, Parameter Estimation Problems parameter identification of the infant human cardiovascularrespiratory systems, Optimal Control optimal control analysis applied to physiological systems, Optimization Methods numerical methods for optimal control systems with and without delay.
Email: jerry.batzel@uni-graz.at
Phone:
8. Prof. Dr. F. Kappel
Department of Mathematics and Scientific Computing
Uni Graz, Heinrichstraße 36, 8010 Graz, Austria
Area of Interest:
Email: franz.kappel@uni-graz.at
Phone: +43 316 380 – 5174
9. Dr. N. Goswami
Assistant Professor,
Department Of Physiology Universitätsstraße 15, 8010 Graz, Austria
Area of Interest:
Email: nandu.goswami@medunigraz.at
Phone: +43 316 380 – 5174
10. Dr. D. H. Fuertinger
Senior Research Fellow at Renal Research Institute, New York, USA
Area of Interest: Inequalities.
Email: doa@gmx.at
Phone: +2348033965848
11. Prof. Dr. S. Keeling
Department of Mathematics and Scientific Computing
Uni Graz, Heinrichstraße 36, 8010 Graz, Austria
Area of Interest: Optimization, Optimal Control and Mathematical Imaging, Optimal Control and inverse Problem.
Email: stephen.keeling@uni-graz.at
Phone: +43 316 380 – 5165
12. Dr. P. Kotanko
Adjunct Professor, The Mount Sinai Hospital New York, USA

Area of Interest:

Email:

Phone:

13. Prof. Dr. S. Owa

Department of Mathematics, Kinki University, Osaka, Japan

Area of Interest:

Email: owa@math.kindai.ac.jp

Phone:

14. Prof. Dr. J. Jahangiri

Department of Mathematical Sciences, Kent State University, Burton, Ohio, USA

Area of Interest:

Email:

Phone:

15. Prof. Dr. H. Irmak

Department of Mathematics, Faculty of Science and Letters, Kirikkale University, Turkey

Area of Interest:

Email: irmak@kku.edu.tr

Phone:

16. Prof. Dr. J. Sokól

Department of Mathematics, Rzeszow University of Technology, Poland

Area of Interest:

Email: jsokol@prz.edu.pl

Phone:

17. Professor S. S. Dragomir

School of Engineering and Science,

Victoria University, PO Box 14428, Melbourne VIC 8001, Australia

Area of Interest:

Email: sever.dragomir@vu.edu.au

Phone: +613 9919 4437.

18. Dr Imdat Iscan, Associate Professor,

28100, Giresun University, Turkey,

Area of Interest:

Email: imdati@yahoo.com, imdat.iscan@giresun.edu.tr

19. Prof Dr Cemil Tunc

Department of Mathematics, Faculty of Sciences, Yuzuncu Yil University, Turkey

Area of Interest:

e-mail: cemtunc@yahoo.com

Phone: +432 2251024

(b) Local

1. Prof. Dr. Malik Zawwar Hussain
Department of Mathematics, University of the Punjab, Lahore
Email: malikzawwar@hotmail.co.uk
Phone: +923009422346
2. Prof. Dr. Siraj ul Islam
Department of Basic Sciences, UET Peshawar,
Email: siraj.islam@gmail.com
Cell: 0345-9669495
3. Dr. Azhar Saleem
Associate Professor, UAJ&K Muzaffarabad,
Cell #: 0306-7120441,
Email: drazharsaleem@yahoo.com
4. Prof. Dr. Muhammad Shafique Baig
Department of Mathematics, University of South Asia, Lahore
E-mail:
Cell:
5. Prof. Dr. Muhammad Aslam Noor
Department of Mathematics, CIIT, Islamabad
E-mail:
Cell:
6. Prof. Dr. Khalida Inayat Noor
Department of Mathematics, CIIT, Islamabad
E-mail:
Cell:
7. Prof. Dr. Muhammad Ayub,
Department of Mathematics, Quaid-i-Azam University, Islamabad.
E-mail:
Cell:
8. Prof. Dr. Muhammad Ozair Ahmad
Department of Mathematics, UET Lahore
E-mail:
Cell:

9. Prof. Dr. Shahid Siddiqi,
Department of Mathematics, University of the Punjab, Lahore
E-mail:
Cell:
10. Prof. Dr. Tousif Mohi-Ud-Din
Department of Mathematics, HITEC University, Taxila
E-mail:
Cell:
11. Prof. Dr. Tasawar Hayat,
Professor (Tenured), Department of Mathematics, QAU Islamabad
E-mail: fmgpak@gmail.com
Cell: 051-90642172
12. Dr. Malik Muhamamd Yousaf
Professor (Tenured) and Chairman, Department of Mathematics, QAU Islamabad
E-mail: drmymalik@hotmail.com
Cell:
13. Dr. Tariq Shah
Associate Professor, Department of Mathematics,
Quaid-i-Azam University Islamabad
Email:
Cell:
14. Prof. Dr. Iftikhar Mughal
Department of Mathematics, UAJK, Muzaffarabad
Email:
Cell:
15. Prof. Dr. Muhammad Mushtaq
Chairman, Department of Mathematics, UET Lahore
E-mail: mushtaqmalik2004@yahoo.co.uk
Cell: 0300 9611187
16. Dr. Muhammad Asad Meraj
Associate Professor, Department of Mathematics, CIIT, Sahiwal
E-mail: asad@ciitsahiwal.edu.pk
Cell: 0324-9825404
17. Dr. Ali Muhammad
Associate Professor, Department of Basic Sciences, UET Peshawar,
E-mail: ali7887@gmail.com
Cell:

18. Dr. Saqib Hussain
Associate Professor, Department of Mathematics, CIIT Abbotabad,
E-mail: saqibhussain@ciit.net.pk
Cell:
19. Prof. Dr. Tahir Mahmood
Department of Mathematics, Islamia University Bahawalpur, Bahawalpur
E-mail:
Cell: 0307 6321017
20. Prof. Dr. Ghulam Muhammad
Department of Mathematics, Govt College Civil Lines, Lahore
E-mail: chgm2004@yahoo.com
Cell: 0312 4602628
21. Dr. Shahid Mubeen
Associate Professor, Department of Mathematics, University of Sargodha, Sargodha
E-mail: smjhanda@gmail.com
Cell: 0300-4251732
22. Dr. Abdus Saboor
Assistant Professor, Department of Mathematics, Kohat University of Science and Technology,
Kohat
E-mail: dr.abdussaboor@kust.edu.pk
Cell: 0321-9023914
23. Dr. Umer Farooq
Assistant Professor, Department of Mathematics, COMSATS, Islamabad
Area of Interest: Fluid Mechanics
E-mail: umer_farooq@comsats.edu.pk
Cell: 0334 5511778
24. Dr. Muhammad Ayub
Assistant Professor, Department of Mathematics, COMSATS, Abbotabad,
Area of Interest: Symmetries,
E-mail: Muhammad_ayub5@hotmail.com
Cell: 0302 8920677
25. Dr. Abdul Qadeer Khan
Assistant Professor, Department of Mathematics, UAJ&K Muzaffarabad,
Area of Interest: Discrete Dynamical Systems
E-mail: abdulqadeerkhan1@gmail.com
Cell: 0344 5102758

26. Prof. Dr. Muhammad Naeem Qureshi
Professor (Rtd), Department of Mathematics, UAK&K, Registrar AIOU Islamabad,
Area of Interest: Symmetries, Discrete Dynamical Systems
E-mail: nqureshi58@gmail.com
Cell: 0300 4746083

6. Scheme of Studies for BSc (Two Years Program) for affiliated colleges

There are three different courses of studies in Mathematics and each course has status of the subject

- i) A-course of Mathematics (200 Marks)
- ii) B-course of Mathematics (200 Marks)
- iii) General Mathematics (200 Marks)

The following division is recommended:

6.1 A-Course of Mathematics

- i) Differential and Integral Calculus (50 Marks)
- ii) Complex Number and Analytic Geometry (50 Marks)
- iii) Infinite Series, Differential Equation and Laplace Transform (50 Marks)
- iv) Linear Programming and Application of Calculus (50 Marks)

6.2 B-Course of Mathematics

- i) Group Theory and Linear Algebra (50 Marks)
- ii) Number Theory, Topology and inner product space (50 Marks)
- iii) Vector Analysis and Statics (50 Marks)
- iv) Numerical Method and Dynamics (50 Marks)

6.3 General Mathematics

- i) Complex Number and linear Algebra and Analytic Geometry (50 Marks)
- ii) Differential and integral calculus (50 Marks)
- iii) Application of calculus and Analytical Geometry of Three Dimension (50 Marks)
- iv) Numerical Method, Infinite Series, Linear Programming and Differential Equation (50 Marks)

6.4 Course Contents of A-Course of Mathematics

6.4.1 Paper-I : DIFFERENTIAL AND INTEGRAL CALCULUS (3rd Year)

Students have to attempt five **question** out of eight: three from Section-I and two question from Section-II

Section-I Differential Calculus (5 out of 8)

A review of real number system, upper and lower bounds, Function and their Graphs, limits, continuity and related theorems, Tangents and the Derivative at a point, Differential rules and their Application, Derivative as a rate of change, Derivatives of trigonometry, exponential, logarithmic, hyperbolic function and differentiation of their inverse, Implicit differentiation, Related rates, Linearization and differentials, Higher derivatives, Leibnitz's theorem, Rolle's theorem, Lagrange mean value theorem, increasing and decreasing function, Cauchy's mean-value theorem, indeterminate forms and L'Hospital's rule.

Section-II Integral calculus (3 out of 8)

Area and estimating with finite sums, sigma notations and limit of finite sums, definite integral as the limit of a sum, properties of definite integral, fundamental theorem of calculus, indefinite integrals and techniques of integration, reduction formulae, application of definite integral to area, arc length and other problems

Recommended Books

1. G.B.Thomas Jr.M.D.Weir and J.R.Hass, Thomas Calculus , 12th edition ,Pearson Edu.Inc.,2010.
2. H.Anton, Calculus.(Latest edition) . John Wiley and sons , New York .
3. S.M.Yousaf ,Calculus
4. Zia-ul-Haq , Calculus and analytical Geometry , Carvan Book , 2001.
5. C.H.Edwards and D.E.Penny, Calculus and analytical Geometry, (Latest Edition).
6. Prentice Hall, Inc.

6.4.2 Paper-II Complex Number and Analytical Geometry (3rd year)

Student have to attempt five question out of eight: two from section-I and three question from section-II

Section-I: Complex Numbers (3 out of 8)

Complex Numbers and algebra of complex number, polar representation, Euler's Formula, De-Moivres' theorem and its applications, Trigonometric and Hyperbolic function, Exponential and logarithmic function, Separation of complex valued functions and imaginary parts, Summation of series.

Section-II: Analytical Geometry (5 out of 8)

Two-dimensional Analytical Geometry (2 out of 8)

Translation and rotation of axes, General equation of the second degree and the classification of conic sections, Conic sections in polar coordinates, Tangents and normals, Pedal equation of curves, Tracing of polar curves.

Three- dimensional Analytical Geometry (3 out of 8)

Direction cosines and ratios, angle between two lines, Standard forms of equations of lines and planes, Distances between points, Lines and planes, Spherical polar and cylindrical coordinate systems, Standard form of the equation of sphere, Cylinder, Cone, ellipsoid, paraboloid and hyperboloid, symmetry, intercepts and sections of a surface, tangent planes and normals.

Recommended Books:

1. G.B.Thomas Jr.M.D.Weir and J.R.Hass, Thomas Calculus, 12th Edition, Pearson Edu. Inc. 2010.
2. H.Anton, Calculus.(Latest edition) . John Wiley and Sons, New York.
3. S. M. Yousaf, Muhammad Amin, Calculus with Analytical Geometry.
4. Zia-ul-Haq , Calculus and analytical Geometry , Carvan Book , 2001.
5. C.H.Edwards and D.E. Penny ,calculus and analytical Geometry,(Latest edition).
 - a. Prentice Hall,Inc.
6. E.H. Swokowski, Calculus with Analytical Geometry ,(Latest Editor). PWS publishers, Boston, Massachusetts.

6.4.3 PAPER.III: INFINITE SERIES, DIFFERENTIAL EQUATIONS AND LAPLACE TRANSFORMS (4th Year)

Students have to attempt five questions out of eight:two from section-I and three question from section-II

Section –I: Infinite series (3 out of 8)

Sequence of numbers and their convergence, Algebra of convergent sequences, Infinite series and their convergences, Convergences tests for infinite series: Comparison, quotient, ratio, root and integral tests, Absolute and conditional convergences, Interval and radius of convergences, Taylors and Maclaurin's theorems in finite and infinite form and their use' in expansion of function.

Section-II: Differential Equations (5 out of 8)

Definition and types of differential equations and their formations, Different methods of solving first order ordinary differential equations, The Bernoulli, Riccati and Clairaut equations, Families of curves, Orthogonal trajectories, Initial and boundary value problem, Application of first order differential equations in problems of decay and growth of populations of dynamics and logistics, second and higher order linear differential equations with constant coefficients and methods of their solutions, Cauchy-Euler equations, system of second order linear differential Equations, Method of undetermined coefficient, Method of variation of parameters, Reduction of order, Laplace transforms and applications.

Recommended Books

1. G.B.Thomas Jr.M.D weir and J.R Hass, Thomas Calculus, 12th Edition, pearson Edu. Inc., 2010.
2. D.G Zill and M.R. Cullen, Differential Equations with boundary –Value problems, 3rd Edition, PWS publishing Company, 1997.
3. H.Anton, Calculus.(Latest Edition).Jhon Wiley and Sons, New York.
4. S.M. Yosaf, Mathematical Methods
6. Zia ul Haq, Calculus and Analytical Geometry, The Carvan Book House, 2001.
8. E.H Swokowski, Calculus with Analytical Geometry (Latest Edition).PWS publishers, boston, Massachusetts

6.4.4 PAPER-IV: LINEAR PROGRAMMING AND APPLICATIONS OF CALCULUS (4th Year)

Students have to attempt five questions out of eight :three from section-I and two from section-II.

Section-I: (5 out of 8)

(a) Applications of Differential Calculus 4/5

Curves and their Cartesian ,polar and parametric representations, Asymptotes ,Maxima and Minima, points of inflexion and their applications, singular points, curve tracing, Curvature ,centre and radius of curvature, Functions of several variables, limits continuity and partial derivatives, Maxima and minima of functions of two variables with applications ,Approximations ,Equations of tangent plane and normal line to a surface.

(b) Linear programming 1/5

Introduction to Operations Research in general and in particular to linear programming simplex method ,Assignment Models

Section-II: Applications of Integral Calculus (3/8)

Rectifications and Quadrature, Simple cases of double and triple integrals, Volumes and area of surfaces of revolutions.

Books Recommended

1. G.B Thomas Jr. M.D weir and J.R. Hass, Thomas Calculus, 12th Edition, pearson Edu. Inc., 2010.
2. A.Sultan, Linear programming, Academic press.
3. W.A Spivey Linear programming ,McMillan Co.
4. Hamday A. Taha, Operations Research
5. Hiller, Introduction to Operations Research
6. Dar, K.H. Mathematical Techniques, Carvan Book House, 2001.

6.5 B-COURSE OF MATHEMATICS

6.5.1 PAPER-I: GROUP THEORY AND LINEAR ALGEBRA (3rd Year)

Students have to attempt five questions out of eight :three from section-I and two from section-II.

Section-I Group Theory (3 out of 8)

Definitions and examples of groups, Groups of residue classes, Cyclic group, Order of a group and order of an element of a group ,subgroup, cosets, Lagrange's theorem and its applications
Permutations ,even and odd permutations ,Cycles and length, transpositions

Section-II: Linear Algebra (5 out of 8)

Fields, Vector spaces,subspaces and examples ,Linear dependence and independence,Bases and dimensions ,Linear transformation,Motivations of ,matrices through a system of linear homogenous and non -homogenous equations , Elementary row and column operations on matrices ,Algebra of matrices Determinants of matrices ,their properties and evaluation of various kinds of matrices ,Matrix of a linear transformation , Rank of a matrix , Evaluation of ranks and inverses of matrices ,solution of system of homogenous and non- homogenous linear equations (Elimination and Gauss Method)

Books Recommended

1. H.Anton, Elementary Linear Algebra .(Latest Edition).J. Wiley
2. S.M. Yosaf, Mathematical Methods
3. A.Majeed .Group Theory.
4. K.L. Mir, Linear Algebra, ilmi kutab khana.
5. C.H Edwards, Jr. and D.E. Penney, Elementary Linear Algebra,(Latest Edition).prentice Hall, International edition
6. S.J.Axler, Linear Algebra, Done Right, Springer-Verlag,1996

6.5.2 Paper-II: NUMBER THEORY, TOPOLOGY AND INNER PRODUCT SPACE(3rd Year)

Student have to attempt five question out of eight: two from section-I and three question from section-II

Section-I: Number Theory (3 out of 8)

Divisibility Euclid's theorem (Division Algorithm) ,Greatest common divisor and latest common multiple, theory of primes, Linear Equations, Diophantine Equation.

Section-II: Topology & Inner Product Space (5 out of 8)

Definition and examples of metric space, open balls, open sets in a metric space, interior, exterior, boundary and closure of a set in a metric space, definition and example of topology and topological spaces, open and closed sets in topological spaces, Neighborhood, Limit Point, Interior, exterior, boundary and closure of sets in a topological spaces, Definition and example of inner product spaces, Orthogonality, orthogonal and orthogonal system, orthogonal matrices.

Books Recommended

1. A. Majeed, Element of topology and functional Analysis, Ilmi kitab Khana, Lahore 1997.
2. S. M. Fahfa, Introduction to point set topology.
3. B. Ahmad, General Topology, 1998.
4. S.Manzur Hussain, Introduction to theory of Number . G. A Jones and J.M.Jones,
5. Elementary Number Theory, Springer-Varlog, London Limited, 1998.
6. M. B. Nathanson, Methods in Number Theory, Springer-Verlog, New York,2000.
7. Introductory set topology by S. M. Yhaya.

6.5.3 PAPER-III: VECTOR ANALYSIS AND STATICS (4th YEAR)

Students have to attempt five questions out of eight: two from section-I and three from section-II

Section-I: Vector Analysis (3 out of 8)

Vectors and their algebra, coordinate systems and bases, Scalar and vector triple products, Differentiation and integration of vectors, Scalar and vector point functions, Concepts of gradient, divergence and curl along with their applications.

Section-II: Statics (5 out of 8)

Composition and resolution of forces, Particles in equilibrium, Parallel forces, moments, Couples, General conditions of equilibrium of coplanar forces, Principle of virtual work, Friction, Centre of gravity.

Books Recommended

1. G.B. Thomas Jr. M.D. Weir and J.R. Hass, Thomas Calculus, 12th Edition, Pearson Edu. Inc., 2010
2. Q. K. Gori, Introduction to Mechanics (West Pakistan Co., Ltd., Lahore)
3. G.D. Smith, Vector Analysis, (Latest Edition), Oxford University Press.
4. K.L.Mir, Vector Analysis, (Latest Edition), Ilmi Kitab Khana.
5. M.N. Talpur, Calculus with Analytical Geometry.
6. L.Syngé and B.A Griffith, (Latest Edition), Principles of Mechanics. Mc-Graw Hill.
7. R. Whitworth and Dyke, Guide to Mechanics, (Latest Edition), MacMillan

6.5.4 PAPER-IV NUMERICAL METHODS AND DYNAMICS (4th Year)

Students have to attempt five questions out of eight : three from section-I and two questions from section-II.

Section-I: Numerical Methods (3 out of 8)

Introduction to Numerical Analysis, Numerical solution of algebraic and transcendental equations: graphical method, bisection method, iteration method, Newton-Raphson method, secant method and method of false position, System of Linear equations: Gauss-Jordan and Jacobi methods, Numerical integration: Trapezoidal and Simpson's rules. (If possible computer programming may be used for problem solving).

Section-II: Dynamics of a Particle (5 out of 8)

Motion in a straight line, Uniformly accelerated and resisted motion. Velocity, acceleration and their components in cartesian and polar coordinates, tangential and normal components, Conservative forces, Projectiles, Central forces and orbits, Simple harmonic motion, Damped and forced vibrations.

Books Recommended

1. Robert-W.Hornbeck, Numerical Methods, Quantum Publishers.
2. Alestair Wood, Introduction to Numerical Analysis, Addison Wesley.
3. M. Iqbal, Numerical Analysis, National Book Foundation.
4. S.A. Bhatti, N.A. Bhatti, Numerical Methods
5. Q. L. Gori, Introduction to Mechanics (West Pakistan Publishing Co., Ltd., Lahore).

6.6 GENERAL MATHEMATICS

6.6.1 PAPER-I: COMPLEX NUMBER, LINEAR ALGEBRA AND ANALYTICAL GEOMETRY (3rd Year)

Students have to attempt five questions out of eight: two from section-I and three questions from section-II.

Section-I: Complex Number System (3 out of 8)

Real number system and properties of real numbers, Real-valued functions and their graphs, Complex numbers their algebra and Polar form, De-Moivres' theorem, n n^{th} roots of complex numbers, Complex functions, Sum of trigonometric series.

Section-II: Linear Algebra and Analytical Geometry (5 out of 8)

Matrices: rank and inverse of a matrix. Linear transformation and their matrices, Determinants, System of linear equations, Analytic Geometry of two Dimension, Translation and rotation of axis, Properties of tangents and normal, Polar equation of conics Pedal equation, Tracing of polar curves.

5.6.2 PAPER-II: DIFFERENTIAL AND INTEGRAL CALCULAS (3rd Year)

Students have to attempt five questions out of eight: three from section-I and two questions from section-II

Section-I: Differential Calculus (5 out of 8)

Techniques of finding limits, Continuity of a function, Differentiability, Indeterminate forms, Use of Rolle's theorem, Mean value theorems (Lagrange and Cauchy), Taylor and Maclaurins series, Derivatives, Higher Derivatives and Partial Derivatives, Related rates.

Section-II: Integral Calculus (3 out of 8)

Techniques of integration, Definite integral as limit of a sum, Evaluation of a definite integral by definition, Improper integrals, reduction formulae.

6.6.3 PAPER-III: APPLICATION OF CALCULUS AND ANALYTICAL GEOMETRY OF THREE DIMENSIONS (4th Year)

Students have to attempt five questions out of eight: two from section-I and three questions from section-II.

Section-I: Application of differential and Integral Calculus (5 out of 8)

Asymptotes, maxima and minima of a function of one and two variables, Curvatures and centre of curvature, rectification, quadrate, Eulers theorem, Chain Rule, Total derivative, Equation of tangent, Plane and normal lines to surfaces volumes and surface area of revolution, Simple cases of double and triple integrals.

Section-II:: Analysis Geometry (3 out of 8)

Direction cosines and ratios, Angle between two lines, Standard form of equations of planes and lines, Intersection of planes and lines, Distance between points, lines and planes, Spherical, polar and cylindrical coordinate systems, Standard form of the equations of a sphere, cylinder, cone, ellipsoid, paraboloid and hyperboloid, Symmetry and intercepts of a surface, Tangent planes and normal.

6.6.4 PAPER-IV: NUMERICAL METHODS, INFINITE SERIES, LINEAR PROGRAMMING AND DIFFERENTIAL EQUATIONS (4th Year)

Students have to attempt five questions out of eight: two from section-I and three questions from section-II.

Section-I: Numerical Methods and Infinite Series (3 out of 8)

Introduction to infinite series and tests for their convergence, Absolute and conditional convergence. Introduction to Numerical Analysis, Numerical Solution of algebraic and transcendental equations: bisection method, Newton-Raphson method.

Section-II: Linear Programming and Differential Equations (5 out of 8)

Introduction to linear programming, Simplex methods and their examples from real life, Differential equations of first order, Separable, Homogenous equation, Exact equation, Linear differential equation, Bernoulli's equation, orthogonal trajectories, Differential equations 2nd and higher order Cauchy Euler equation, Method of variation of parameters, Method of undetermined Coefficient.

Books Recommended for General Mathematics (Papers I to IV)

1. G.B. Thomas Jr. M.D. Weir and J.R. Hass, Thomas Calculus, 12th Edition, Pearson. Edu. Inc., 2010.
2. S.T. Tan, Applied Mathematics. For the Managerial, life, and social sciences.
3. H. Anton, Elementry Linear Algebra. (7th edition, 1997). Wiley.
4. H. Anton, Calculus, (Latest Edition)m John Wiley and Sons, New York.
5. E. Kreyosing, Advanced Engineering Mathematics, (Latest Edition), J. Wiley.
6. M. Iqbal Numerical Analysis. (Latest Edition), National Book Foundation.
7. Fiaz Ahmad and M.A. Rana, Elements of Numerical Analysis, (Latest Edition), NBF.
8. S.M. Yousaf, Mathematical Methods.
9. Hmaday A. Taha, Operations Research.
10. A. Sultan, Linear Programmingm, Academic Press.

Other Books

1. Calculus S.M. Yousaf
2. Introduction to Mechanics, S.M. Yousaf
3. Topology Ch. M. Amin
4. Introductions Set Topology S.M. Yousaf.
5. Metric Spaces by Z.R Bhatti
6. Elementary Theory of Numbers by Sayyed Manzoor Hussain
7. Elementary Numerical Analysis by Dr. M. Iqbal
8. Vector Analysis by Dr. Munawwar Hussain.

Any Other Item