

**DEPARTMENT OF MATHEMATICS**



**5<sup>TH</sup> MEETING OF THE BOARD OF STUDIES  
SEPTEMBER, 2017**

**MINUTES OF MEETING AND APPROVED SCHEME OF STUDIES**

**MIRPUR UNIVERSITY OF SCIENCE AND TECHNOLOGY (MUST)**

**ALLAMA IQBAL ROAD, MIRPUR-10250**

**MIRPUR, AZAD JAMMU & KASHMIR**

**Members of the Board of Studies**

The following members were present in the meeting:

| Sr. # | Name  | Designation      | Signature |
|-------|---|------------------|-----------|
| 1     | Dr. Rashida Hussain<br>Coordinator, Department of Mathematics, MUST, Mirpur AJ&K                                | Convener/Member  |           |
| 2     | Prof. Dr. Rehana Asghar<br>Dean, Faculty of Sciences, MUST, Mirpur, AJK   | Observer         |           |
| 3     | Prof. Dr. Muhammad Mushtaq<br>Dept. of Mathematics, UET Lahore  | Member           |           |
| 4     | Dr. Muhammad Munir<br>Associate Professor, Department of Mathematics,<br>Post Graduate College, Abbottabad, KPK | Member           |           |
| 5     | Mr. Suleman Khan<br>Assistant Prof., Dept. of Mathematics, MUST, Mirpur AJK                                     | Member           |           |
| 6     | Dr. Shah Muhammad<br>Assistant Prof. Dept. of Mathematics, MUST, Mirpur AJK                                     | Member/Secretary |           |
| 7     | Director AS & RB, MUST, Mirpur AJK  | Observer         |           |
| 8     | The Registrar, MUST, Mirpur AJK   | Observer         |           |
| 9     | The Controller of Examinations, MUST, Mirpur AJK  | Observer         |           |
| 10    | Director QEC, MUST, Mirpur AJK  | Observer         |           |

### 1. Scheme of Studies for BS Mathematics: General Breakup

| Content |                         | Description  | Remarks |
|---------|-------------------------|--|---------|
| 1.1     | Entrance Requirement    | Intermediate with Mathematics  |         |
|         |                         | No D-grade in academic career  |         |
|         |                         | Entry Test conducted by the University with the following breakup:<br>Mathematics: 80 %, English: 20%<br>Merit shall be determined on 10% of SSC, 50% of Intermediate and 40% of Entry Test marks. |         |
| 1.2     | Duration of the Program | 8-12 Semesters   |         |
| 1.3     | Total Credit Hours      | Course Work: 133 Credit Hrs  |         |
|         |                         | Final Year Project (Optional): 3 Credit Hrs  |         |
|         |                         | Comprehensive Oral Examination: 2 Credit Hour  |         |

### 1.4 Structure

| Sr. No. | Category                  | No. of Courses | Credit Hrs | Remarks |
|---------|---------------------------|----------------|------------|---------|
| 01      | General Education Cluster | 12             | 30         |         |
| 02      | Allied Courses            | 07             | 18         |         |
| 03      | Major Courses             | 34             | 85         |         |
| 04      | Field Experience          | 01             | 03         |         |
| 05      | Capstone Project          | 01             | 03         |         |
| Total   |                           | --             | --         |         |

### 1.5 Layout/Framework

| Category                  | Course Title   | Credit Hrs | Remarks |
|---------------------------|--|------------|---------|
| General Education Cluster | Arabic   | 02         |         |
|                           | Physics-I  | 03         |         |
|                           | Introduction to Sociology/HR Management  | 02/03      |         |
|                           | English-I (Functional English)   | 03         |         |
|                           | English-III (Technical Writing and Presentation Skills)                                | 03         |         |
|                           | <b>Quantitative Reasoning:</b>   | <b>03</b>  |         |
|                           | <b>Quantitative Reasoning:</b>   | <b>03</b>  |         |
|                           | Islamic Studies/Ethics   | 02         |         |
|                           | Pakistan Studies   | 02         |         |
|                           | Introduction to Computers  | 03         |         |
|                           | Educational Psychology/Organizational Behavior/ Business Mathematics/ Entrepreneurship | 02/03      |         |
|                           | <b>Civics and Community Engagement:</b>  | <b>02</b>  |         |
| Allied Courses            | Physics-II   | 03         |         |
|                           | English-II (Communication Skills)  | 03         |         |
|                           | Mathematical Statistics I  | 03         |         |
|                           | Mathematical Statistics II   | 03         |         |
| Major Courses             | Calculus-I   | 04         |         |
|                           | Calculus-II  | 04         |         |
|                           | Calculus-III   | 04         |         |
|                           | Foundation of Mathematics  | 03         |         |
|                           | Linear Algebra-I   | 03         |         |
|                           | Linear Algebra-II  | 02         |         |
|                           | Introduction to Differential Equations   | 02         |         |
|                           | Mechanics I  | 03         |         |
|                           | Mechanics II   | 03         |         |
|                           | Ordinary Differential Equations  | 03         |         |
|                           | Abstract Algebra   | 03         |         |
|                           | Real Analysis-I  | 03         |         |
|                           | Complex Analysis   | 03         |         |
|                           | Metric Spaces  | 02         |         |
|                           | Topology   | 03         |         |
|                           | Scientific Programming   | 2+1        |         |
|                           | Tensor Analysis  | 02         |         |
|                           | Differential Geometry-I  | 03         |         |
|                           | Real Analysis-II   | 03         |         |

|  |                                |    |  |
|--|--------------------------------|----|--|
|  | Partial Differential Equations | 03 |  |
|  | Number Theory                  | 02 |  |
|  | Analytical Mechanics           | 03 |  |
|  | Numerical Methods I            | 03 |  |
|  | Mathematical Physics           | 03 |  |
|  | Functional Analysis            | 03 |  |
|  | Integral Equations             | 03 |  |
|  | Comprehensive Oral Examination | 02 |  |
|  | Elective-I                     | 03 |  |
|  | Elective-II                    | 03 |  |
|  | Elective-III                   | 03 |  |
|  | Elective-IV                    | 03 |  |
|  | Elective-V                     | 03 |  |

### 1.6 Semester-Wise Breakdown

| Course Code                | Course Title  | Lec. Hrs. | Lab. Hrs. | Credit Hrs. |
|----------------------------|---|-----------|-----------|-------------|
| <b>1<sup>st</sup> Year</b> |   |           |           |             |
| <b>Semester-I</b>          |   |           |           |             |
| ISL-1101                   | Islamic Studies   | 2         | 0         | 2           |
| ENG-1102                   | English-I (Functional English)                          | 3         | 0         | 3           |
| COM-1103                   | Introduction to Computers                               | 2         | 1         | 3           |
| PHY-1104                   | Physics-I   | 3         | 0         | 3           |
| MAT-1105                   | Calculus-I  | 4         | 0         | 4           |
| MAT-1106                   | Foundation of Mathematics                               | 3         | 0         | 3           |
| <b>Semester-II</b>         |   |           |           |             |
| HUM-1201                   | Arabic  | 2         | 0         | 2           |
| ENG-1202                   | English-II (Communication Skills)                       | 3         | 0         | 3           |
| HUM-1203                   | Pakistan Studies  | 2         | 0         | 2           |
| PHY-1204                   | Physics-II  | 3         | 0         | 3           |
| MAT-1205                   | Calculus-II   | 4         | 0         | 4           |
| MAT-1206                   | Linear Algebra-I  | 3         | 0         | 3           |
| <b>2<sup>nd</sup> Year</b> |   |           |           |             |
| <b>Semester-III</b>        |   |           |           |             |
| ENG-2302                   | English-III (Technical Writing and Presentation Skills) | 3         | 0         | 3           |
| MAT-2303                   | Mathematical Statistics I                               | 3         | 0         | 3           |
| MAT-2304                   | Mechanics-I   | 3         | 0         | 3           |
| MAT-2305                   | Calculus-III  | 4         | 0         | 4           |
| MAT-2306                   | Linear Algebra-II                                       | 2         | 0         | 2           |
| <b>One Optional</b>        |   |           |           |             |
| HUM-2301                   | Introduction to Sociology                               | 3         | 0         | 3           |
| HUM-2308                   | HR Management   | 3         | 0         | 3           |
| <b>Semester-IV</b>         |   |           |           |             |
| MAT-2402                   | Introduction to Differential Equations                  | 2         | 0         | 2           |
| MAT-2403                   | Mathematical Statistics II                              | 3         | 0         | 3           |
| MAT-2404                   | Mechanics-II  | 3         | 0         | 3           |
| MAT-2405                   | Metric Spaces   | 2         | 0         | 2           |
| MAT-2406                   | Number Theory   | 2         | 0         | 2           |

**One Optional**

|          |                         |   |   |   |
|----------|-------------------------|---|---|---|
| PSY-2401 | Educational Psychology  | 3 | 0 | 3 |
| HUM-2408 | Organizational Behavior | 3 | 0 | 3 |
| MAT-2409 | Business Mathematics    | 3 | 0 | 3 |
| HUM-2410 | Entrepreneurship        | 3 | 0 | 3 |

**3<sup>rd</sup> Year****Semester-V**

|          |                                 |   |   |   |
|----------|---------------------------------|---|---|---|
| MAT-3501 | Real Analysis-I                 | 3 | 0 | 3 |
| MAT-3502 | Ordinary Differential Equations | 3 | 0 | 3 |
| MAT-3503 | Differential Geometry-I         | 3 | 0 | 3 |
| MAT-3504 | Analytical Mechanics            | 3 | 0 | 3 |
| MAT-3505 | Topology                        | 3 | 0 | 3 |
| MAT-3506 | Abstract Algebra                | 3 | 0 | 3 |

**Semester-VI**

|          |                                |   |   |   |
|----------|--------------------------------|---|---|---|
| MAT-3601 | Real Analysis-II               | 3 | 0 | 3 |
| MAT-3602 | Partial Differential Equations | 3 | 0 | 3 |
| MAT-3603 | Numerical Methods-I            | 3 | 0 | 3 |
| MAT-3604 | Complex Analysis               | 3 | 0 | 3 |
| MAT-3605 | Tensor Analysis                | 2 | 0 | 2 |
| MAT-3606 | Scientific Programming         | 2 | 1 | 3 |

**4<sup>th</sup> Year****Semester-VII**

|          |                                |     |   |   |
|----------|--------------------------------|-----|---|---|
| MAT-4702 | Mathematical Physics           | 3   | 0 | 3 |
| MAT-4704 | Functional Analysis            | 3   | 0 | 3 |
| MAT-4705 | Fluid Mechanics-I              | 3   | 0 | 3 |
| MAT-4715 | Conference/Seminar/Readings-II | S/U |   |   |

**Two Optional Courses**

|          |                          |   |   |   |
|----------|--------------------------|---|---|---|
| MAT-4701 | Measure Theory           | 3 | 0 | 3 |
| MAT-4703 | Numerical Methods II     | 3 | 0 | 3 |
| MAT-4706 | Operation Research       | 3 | 0 | 3 |
| MAT-4707 | Discrete Structures      | 3 | 0 | 3 |
| MAT-4708 | Special Functions        | 3 | 0 | 3 |
| MAT-4709 | Quantum Mechanics-I      | 3 | 0 | 3 |
| MAT-4710 | Ring Theory              | 3 | 0 | 3 |
| MAT-4711 | Analytical Dynamics      | 3 | 0 | 3 |
| MAT-4712 | Approximation Theory     | 3 | 0 | 3 |
| MAT-4713 | Differential Geometry-II | 3 | 0 | 3 |
| MAT-4714 | Electromagnetic Theory-I | 3 | 0 | 3 |

**Semester-VIII**

|          |                                |   |     |   |
|----------|--------------------------------|---|-----|---|
| MAT-4803 | Integral Equations             | 3 | 0   | 3 |
| MAT-4805 | Fluid Mechanics-II             | 3 | 0   | 3 |
| MAT-4807 | Comprehensive Oral Examination | 2 | 0   | 2 |
| MAT-4815 | Conference/Seminar/Readings-II |   | S/U |   |

**Three Optional Courses**

|          |   |   |   |   |
|----------|---|---|---|---|
| MAT-4801 | Mathematical Systems Theory             | 3 | 0 | 3 |
| MAT-4802 | Mathematical Modeling                   | 3 | 0 | 3 |
| MAT-4804 | Optimization Theory                     | 3 | 0 | 3 |
| MAT-4806 | Algebraic Topology                      | 3 | 0 | 3 |
| MAT-4808 | Project                                 | 3 | 0 | 3 |
| MAT-4809 | Quantum Mechanics-II                    | 3 | 0 | 3 |
| MAT-4810 | Introduction to Combinatorics           | 3 | 0 | 3 |
| MAT-4811 | Variational Inequalities                | 3 | 0 | 3 |
| MAT-4812 | Theory of Elasticity                    | 3 | 0 | 3 |
| MAT-4813 | Special Theory of Relativity            | 3 | 0 | 3 |
| MAT-4814 | Electromagnetic Theory-II               | 3 | 0 | 3 |
| MAT-4816 | Measure Theory and Lebesgue Integration | 3 | 0 | 3 |



## 1.7 Detail of Courses

### Semester-I

**Course Code:** MAT-1105

**Title:** Calculus-I

**Credit Hrs:** 04

#### Course Outline:

**Review Topics:** Equations and inequalities: Solving linear and quadratic equations, linear inequalities. Division of polynomials, synthetic division. Roots of a polynomial, rational roots; Viète Relations. Descartes rule of signs. Solutions of equations with absolute value sign. Solution of linear and non-linear inequalities with absolute value sign.

Functions and Graphs: Domain and range of a function. Examples: polynomial, rational, piecewise defined functions, absolute value, functions, and evaluation of such functions. Operations with functions: sum, product, quotient and composition. Graphs of functions: linear, quadratic, piecewise defined functions.

Lines and System of Equations: Equation of a straight line, slope and intercept of a line, parallel and perpendicular lines. Systems of linear equations, solution of system of linear equations. Nonlinear systems: at least one quadratic equation.

**Limits and Continuity:** Functions, limit of a function. Graphical approach. Properties of limits. Theorems of limits. Limits of polynomials, rational and transcendental functions. Limits at infinity, infinite limits, one-sided limits. Continuity.

**Derivatives:** Definition, techniques of differentiation. Derivatives of polynomials and rational, exponential, logarithmic and trigonometric functions. The chain rule. Implicit differentiation. Rates of change in natural and social sciences. Related rates. Linear approximations and differentials. Higher derivatives, Leibnitz's theorem.

**Applications of derivatives:** Roll's Theorem, Cauchy's MVT, Increasing and decreasing functions. Relative extrema and optimization. First derivative test for relative extrema. Convexity and point of inflection. The second derivative test for extrema. Curve sketching. Indeterminate forms and L'Hopitals rule. Inverse functions and their derivatives.

**Integration:** Antiderivatives and integrals. Riemann sums and the definite integral. Properties of definite integral. The fundamental theorem of calculus. The substitution rule.

#### Texts and Reference Books

1. H. Anton, *Calculus, A New Horizon*, 6<sup>th</sup> Edition, John Wiley and Sons, New York, 1999
2. J. Stewart, *Calculus*, 3<sup>rd</sup> Edition, Brooks/Cole, 1995.
3. G. B. Thomas and A.R. Finney, *Calculus*, 10<sup>th</sup> Edition, Addison Wesley, USA, 2002.
4. Dr. B. H. Edwards, *Calculus*: 10<sup>th</sup> Edition, Brooks/Cole, 2013.
5. S.M Yousaf, Muhammad Amin, *Calculus*: 7<sup>th</sup> Edition, Ilmi Kitab Khana.

**Course Code:** MAT-1106

**Title:** Foundation of Mathematics

**Credit Hrs:** 03

**Course Outline:** Sets and its Subsets, Operations on Sets, Some Fundamental Results, Cartesian Products of Sets, Binary Relations, Equivalence Relations, Partially Ordered Relations, Functions and Their Graph, Countable and Uncountable Sets, Upper Bounds, Lower Bounds, Supremum and Infimum, Complex Numbers, Algebra of Complex Numbers, Modulus and Argument, Polar Form of a Complex Number, De Moivre's Theorem, Roots, Complex-Valued Functions Binary Operations, Groups, Subgroups, Cyclic Groups, Groups of Permutations, Cycles, Transpositions, Order of a Permutation, Rings

#### Texts and Reference Books

1. G. B. Thomas and A.R. Finney, *Calculus*, 10<sup>th</sup> Edition, Addison Wesley, USA, 2002.
2. J. A. Fraleigh, *A first course in Abstract Algebra*, Addison Wesley publishing Company, 1982.
3. S. Lang, *Algebra*, Addison Wesley, 1975.
4. T. Q. Sibley, *The Foundations of Mathematics*, 1<sup>st</sup> Edition, Wiley, 2008.
5. D. Tall, *The Foundations of Mathematics*, 2<sup>nd</sup> Edition, Oxford University Press, 2015.

## Semester-II

Course Code: MAT-1205

Title: Calculus-II

Credit Hrs: 04

### Course Outline:

**Techniques of integration:** Integrals of elementary, hyperbolic, trigonometric, logarithmic and exponential functions. Integration by parts, substitution and partial fractions. Approximate integration. Improper integrals. Reduction Formulas, Gamma functions.

**Applications of integrals:** Area between curves, average value. Volumes. Arc length. Area of a surface of revolution. Applications to Economics, Physics, Engineering and Biology.

**Infinite series:** Sequences and series. Convergence and absolute convergence. Tests for convergence: divergence test, integral test, p-series test, comparison tests, alternating series test, ratio test, root test. Power series. Convergence of power series. Representation of functions as power series. Differentiation and integration of power series. Taylor and McLaurin series. Approximations by Taylor polynomials.

**Conic section, parameterized curves and polar coordinates:** Curves defined by parametric equations. Calculus with parametric curves: tangents, areas, arc length. Polar coordinates. Polar curves, tangents to polar curves. Area and arc length in polar coordinates.

### Texts and Reference Books

1. H. Anton, *Calculus: A New Horizon*, 6<sup>th</sup> Edition, John Wiley and Sons, New York, 1999
2. J. Stewart, *Calculus*, 3<sup>rd</sup> Edition, Brooks/Cole, 1995.
3. G. B. Thomas and A. R. Finney, *Calculus*, 10<sup>th</sup> Edition, Addison Wesley, Reading, Ma, USA, 2002
4. M. Ryan, *Calculus*, 2<sup>nd</sup> Edition, For Dummies, 2016.
5. M. D. Spivak, *Calculus*, 4<sup>th</sup> Edition, Publish or Perish, 2008.

Course Code: MAT-1206

Title: Linear Algebra-I

Credit Hrs: 03

**Course Outline: System of Linear Equations**, Row Reduction, Echelon and Reduced Forms, Vector Equations and the Matrix Equation, Solution of Linear Systems and Applications, **Matrix Operations**, Inversion and Characterizations of Invertible Matrices, Matrix Factorization, Application of Matrices and Linear Equations, Determinants and Their Properties, Cramer's Rule, Volume and Linear Transformations, Fields, Vector Spaces, Subspaces, Linear Dependence and Independence, Linear Span of a Subset of a Vector Space, Bases and Dimensions, Rank and Nullity

### Texts and Reference Books

1. D. C. Lay, *Linear Algebra and its Applications*, Dorling Kindersley Publishing, 2003.
2. S. J. Leon, *Linear Algebra with Applications*, 6<sup>th</sup> Edition, Prentice Hall, 2002.
3. G. E. Shilov, *Linear Algebra*, Dover Publication, Inc., New York, 1997.
4. D. G. Zill and M. R. Cullen, *Advanced Engineering Mathematics*, PWS, Publishing Company, Boston, 1996.
5. G. Strang, *Linear Algebra*, 5<sup>th</sup> Edition, Wellesley-Cambridge Press, 2016.

**Semester-III****Course Code:** MAT-2303**Title:** Mathematical Statistics I**Credit Hrs:** 03

**Course Outline:** The postulates of probability, Some elementary theorems, Addition and multiplication rules, Baye's rule and future Baye's theorem, Random variables and probability functions, Uniform, Bernoulli and Binomial distribution, Hypergeometric and geometric distribution, Negative binomial and Poisson distribution, Uniform and exponential distribution, Gamma and beta distributions, Normal distribution, Moments and moment generating functions  
Moments of binomial, hypergeometric, Poisson, gamma, beta and normal distributions

**Texts and Reference Books**

1. M. H. De-Groot and M. J. Schervish, *Probability and Statistics*, 3<sup>rd</sup> Edition, Addison Wesley, 2002.
2. A. Papoulis, *Probability, Random Variables, and Stochastic Processes*, 3<sup>rd</sup> Edition, Mc-Graw Hill, 1991.
3. T. Sincich, *Statistics by Examples*, Dellen Publishing Company, 1990.
4. A. S. Hirahi, *A Course in Mathematical Statistics*, 4<sup>th</sup> Edition, Ilmi Kitab Khana, Lahore, Pakistan, 2012.
5. S. M. Chaudhry and S. Kamal, *Introduction to Statistical Theory Part-II*, Ilmi Kitab Khana, Lahore, Pakistan, 2012.

**Course Code:** MAT-2304**Title:** Mechanics-I**Credit Hrs:** 03**Course Outline:**

**Forces:** Fundamental concepts and principles, Newtonian Mechanics, Inertial-non-inertial frames, Resultant of several concurrent forces, The parallelogram law of forces, Resolution of a forces, triangle of forces, Lamy's theorem, polygon of forces, Conditions of equilibrium for a particle, External and internal forces, principle of transmissibility, Resultant of like and unlike parallel forces, Moment of forces about a point, Varignon's theorem, Moment of a couple, equivalent couples, composition of couples, Reduction of coplanar forces to a force or a couple

**Friction:** Dry friction and fluid friction, Laws of dry friction, coefficients of friction, angle of friction, Equilibrium of a particle on a rough inclined plane, Particle on a rough inclined plane acted on by an external force, Conditions for sliding or titling

**Virtual Work:** Principle of virtual work, Problems involving tensions and thrust.

**Texts and Reference Books:**

1. A. Bedford and W. Fowler, *Dynamics Engineering Mechanics*, Addison-Wesley, Reading, USA.
2. T. L. Chow, *Classical Mechanics*, John Wiley and Sons, New York, 1995.
3. H. Goldstein, *Classical Mechanics*, 2<sup>nd</sup> Edition, Addison Wesley, Reading, Ma, USA, 1980.
4. J. B. Marion, *Classical Dynamics of Particles and Fields*, 2<sup>nd</sup> Edition, Academic Press, New York, 1970.
5. J. R. Taylor, *Classical Mechanics*, University Science Books, 2005.

**Course Code:** MAT-2305**Title:** Calculus-III**Credit Hrs:** 04**Course Outline:**

**Multivariable functions and partial derivatives:** Functions of several variables. Limits and Continuity. Partial derivatives, Composition and chain rule. Directional derivatives and the gradient vector. Implicit function theorem for several variables. Maximum and minimum values. Optimization problems. Lagrange Multipliers.

**Vectors and analytic geometry in space:** Coordinate system. Rectangular, cylindrical and spherical coordinates. The dot product, the cross product. Equations of lines and planes. Quadric surfaces.

**Vector-valued functions:** Vector-valued functions and space curves. Derivatives and integrals of vector valued functions. Arc length. Curvature, normal and binormal vectors.

**Multiple integrals:** Double integrals over rectangular domains and iterated integrals. Non-rectangular domains. Double integrals in polar coordinates. Triple integrals in rectangular, cylindrical and spherical coordinates. Applications of double and triple integrals. Change of variables in multiple integrals.

**Vector calculus:** Vector fields. Line integrals. Green's theorem. Curl and divergence. Surface integrals over scalar and vector fields. Divergence theorem. Stokes' theorem.

**Texts and Reference Books**

1. H. Anton, *Calculus: A New Horizon*, 6<sup>th</sup> Edition, John Wiley and Sons, New York, 1999.
2. J. Stewart, *Calculus*, 3<sup>rd</sup> Edition, Brooks/Cole, 1995.
3. G. B. Thomas and A.R. Finney, *Calculus*, 10<sup>th</sup> Edition, Addison Wesley, Reading, Ma, USA, 2002.
4. M. Ryan, *Calculus*, 2<sup>nd</sup> Edition, For Dummies, 2016.
5. Dr. R. Larson, *Calculus*, 9<sup>th</sup> Edition, Brooks/Cole, 2009.

**Course Code:** MAT-2306**Title:** LinearAlgebra-II**Credit Hrs:** 02

**Course Outline:** Linear Transformations and the Matrix of Linear Transformations, Eigenvectors and eigenvalues, Diagonalization, Complex Eigenvalues, Inner Product Spaces, Length and Orthogonality, Orthogonal Sets and Orthogonal Projections, Gram-Schmidt Process, Symmetric Matrices, Diagonalization of Symmetric Matrices, Quadratic Forms

**Texts and Reference Books**

1. D. C. Lay, *Linear Algebra and its Applications*, Dorling Kindersley Publishing, Inc., 2003.
2. S. J. Axler, *Linear Algebra*, Done Right, Springer-Verlag, 1996.
3. W. K. Nicholson, *Elementary linear algebra with applications*, 2<sup>nd</sup> Edition, PWS Publishing Company, 1994.
4. D.G. Zill and M. R. Cullen, *Advanced Engineering Mathematics*, PWS, Publishing Company, Boston, 1996.
5. M. J. Sterling, *Algebra II*, 2<sup>nd</sup> Edition, For Dummies, 2014.

**Semester-IV****Course Code:** MAT-2402**Title:** Introduction to Differential Equations**Credit Hrs:** 02**Course Outline:**

**Preliminaries:** Introduction (Formulation and classifications of differential equations), existence and uniqueness of solutions, introduction of initial value and boundary value problems

**First order ordinary differential equations:** Basic concepts, Separable variables, Exact Equations, Homogeneous Equations, Linear equations, integrating factors. Some nonlinear first order equations with known solution, differential equations of Bernoulli and Riccati type, Clairaut equation, modeling with first-order ODEs,

**Second and higher order Linear differential equations:** Initial value and boundary value problems, Homogeneous and non-homogeneous equations, Superposition principle, homogeneous equations with constant coefficients, Linear independence and Wronskian, Nonhomogeneous equations, undetermined coefficients method, variation of parameters, Cauchy-Euler equation, Modeling.

**Texts and Reference Books**

1. W. E. Boyce and R. de Prima, *Elementary Differential Equations*, 9<sup>th</sup> Edition, Wiley, 2008.
2. E. Kreyszig, *Advanced Engineering Mathematics*, 10<sup>th</sup> Edition, Wiley, 2011.
3. D. G. Zill, *Differential Equations with Boundary-Value Problems*, 8<sup>th</sup> Edition, Brooks Cole, 2012.
4. S. J. Farlow, *An Introduction to Differential Equations and Their Applications*, Dover Publications, 2006.
5. M. E. Taylor, *An Introduction to Differential Equations*, 14<sup>th</sup> Edition, American Mathematical Society, 2011.

**Course Code:** MAT-2403**Title:** Mathematical Statistics II**Credit Hrs:** 03

**Course Outline:** Distribution function technique, Transformation technique: One variable, several variables, Moment-generating function technique, The distribution of the mean, The distribution of the mean: Finite populations, The Chi-Square distribution., The t distribution, The F distribution, Regression and Correlation, Linear regression, The methods of least squares, Normal regression analysis, Normal correlation analysis, Multiple linear regression, Multiple linear regression (matrix notation)

### Texts and Reference Books

1. M. H. De-Groot and M. J. Schervish, *Probability and Statistics*, 3<sup>rd</sup> Edition, Addison Wesley, 2002.
2. A. Papoulis, *Probability, Random Variables, and Stochastic Processes*, 3<sup>rd</sup> Edition, Mc-Graw Hill, 1991.
3. T. Sincich, *Statistics by Examples*, Dellen Publishing Company, 1990.
4. A. S. Hirahi, *A Course in Mathematical Statistics*, 4<sup>th</sup> Edition, Ilmi Kitab Khana, Lahore, Pakistan, 2012.
5. S. M. Chaudhry and S. Kamal, *Introduction to Statistical Theory Part-II*, Ilmi Kitab Khana, Lahore, Pakistan, 2012.

**Course Code:** MAT-2404

**Title:** Mechanics-II

**Credit Hrs:** 03

### Course Outline:

**Kinematics:** Rectilinear motion of particles. Uniform rectilinear motion, uniformly accelerated rectilinear motion. Curvilinear motion of particle, rectangular components of velocity and acceleration. Tangential and normal components. Radial and transverse components. Projectile motion. **Kinetics:** Work, power, kinetic energy, Conservation Laws (conservative force fields. Conservation of energy Conservation of linear and angular momentum), impulse, torque. Non-conservative forces. **Simple Harmonic Motion:** The simple harmonic oscillator, period, frequency. Resonance and energy. The damped harmonic oscillator, over damped, critically damped and under damped. Motion, forces and vibrations. **Central Forces and Planetary Motion:** Central force fields, Properties of Central Force Field, Equations of motion, potential energy, orbits. Kepler's law of planetary motion. Apsides and apsidal angles for nearly circular orbits. Motion in an inverse square field.

**Planer Motion of Rigid Bodies:** Introduction to rigid and elastic bodies, degree of freedom, translations, rotations, instantaneous axis and center of rotation, Rotation of a rigid body about a fixed axis, moments and products of inertia. Parallel and perpendicular axis theorem.

### Texts and Reference Books

1. A. Bedford and W. Fowler, *Dynamics Engineering Mechanics*, Addison-Wesley, Reading, USA.
2. T. L. Chow, *Classical Mechanics*, John Wiley and Sons, New York, 1995.
3. H. Goldstein, *Classical Mechanics*, 2<sup>nd</sup> Edition, Addison Wesley, Reading, Ma, USA, 1980.
4. J. B. Marion, *Classical Dynamics of Particles and Fields*, 2<sup>nd</sup> Edition, Academic Press, New York, 1970.
5. J. R. Taylor, *Classical Mechanics*, Null Edition, University Science Books, 2005.

**Course Code:** MAT-2405

**Title:** Metric Spaces

**Credit Hrs:** 02

**Course Outline:** Preliminary Concepts, Definition and Examples of Metric Spaces, Open and Closed Spheres and Sets, Convergent Sequences, Cauchy Sequences, Cantor's Intersection Theorem, Complete Metric Spaces, Dense and Nowhere Dense Subsets, Continuous and Uniform Continuous Functions and Their Properties,

### Texts and Reference Books

1. C. W. Patty, *Foundation of Topology*, 2<sup>nd</sup> Edition, The Jones and Bartlett Publishers, 2009.
2. J. Dugundji, *Topology*, W.M. C. Brown Publisher, 1990.
3. E. Kreyszig, *Introductory Fundamental Analysis with Applications*, John Wiley and Sons, 1978.
4. M. O. Searcoid, *Metric Spaces*, 2007 Edition, Springer, 2006.
5. P. K. Jain, *Metric Spaces*, 2<sup>nd</sup> Edition, Alpha Science Intl Ltd, 2004.

**Course Code:** MAT-2406

**Title:** Number Theory

**Credit Hrs:** 02

**Course Outline:** Divisibility, Euclidean Algorithm, GCD and LCM of two Integers, Properties of Prime Numbers, Fundamental Theorem of Arithmetic (UFT), Congruence Relation, Residue System, Euler's Phi-Function, Solution of System of Linear Congruence, Congruences of Higher Degree, Chinese Remainder Theorem, Fermat's Little Theorem, Wilson's Theorem and Applications, Primitive Roots and Indices, Integers Belonging to a Given Exponent (mod  $p$ ), Primitive Roots of Prime and Composite Moduli, Indices

**Texts and Reference Books**

1. G. A. Jones and J. M. Jones, *Elementary Number Theory*, Springer-Varlog, London Limited, 1998.
2. M. B. Nathanson, *Methods in Number Theory*, Springer-Verlag, New York, 2000.
3. A.N. Parshin and I.R. Shafarevich, *Number Theory-I, Fundamental Problems, Ideas and Theories*, Springer-Verlag, Berlin Heidelberg, 1995.
4. K. H. E. Rosen, *Elementary Number theory and its Applications*, 4<sup>th</sup> Edition, Addison Wesley, Reading, Ma, USA, 2000.
5. T. Andreescu and D. Andrica, *Number theory*, 2009 Edition, Birkhauser, 2009.

**Semester-V**

**Course Code:** MAT-3501

**Title:** Real Analysis-I

**Credit Hrs:** 03

**Course Outline:** Supremum and Infimum, Completeness Properties of the Real Numbers, Limits and Continuity, Properties of Continuous Functions on Closed Bounded Intervals, Derivatives in One Variable, The Mean Value Theorem, Sequences and Series of Functions, Power Series, Pointwise and Uniform Convergence, Riemann Integrations

**Texts and Reference Books**

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Real Analysis*, Mc-Graw Hill, 1995.
3. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3<sup>rd</sup> Edition, John Wiley and Sons, 1999.
4. R. L. Brabenec, *Introduction to Real Analysis*, PWS Publishing Company, 1994.
5. E. D. Gaughan, *Introduction to Analysis*, 5<sup>th</sup> Edition, Brooks/Cole, 1997.

**Course Code:** MAT-3502

**Title:** Ordinary Differential Equations

**Credit Hrs:** 03

**Course Outline:**

**Review** of first order linear and nonlinear odes and higher order linear odes and their solution techniques. **Basic theory** of systems of first order linear equations, Homogeneous linear system with constant coefficients, Non homogeneous linear system, **Series Solution and its Limitations**, The Frobenius Method, **Sturm-Liouville** (S-L) System and Boundary-Value Problems, Solution of the Bessel, The Hypergeometric, The Legendre and the Hermite Equations, Properties of the Bessel, the Legendre and the Hermite Functions

**Texts and Reference Books**

1. E. A. Coddington and N. Levinson, *Theory of Ordinary Differential Equations*, Mc-Graw Hill, New York, Toronto and London, 1955.
2. W. E. Boyce and R. de Prima, *Elementary Differential Equations*, 9<sup>th</sup> Edition, Wiley, 2008.
3. P. Hartman, *Ordinary Differential Equations*, John Wesley and Sons, New York, 1964.
4. D. G. Zill and M. R. Cullen, *Differential Equations with Boundary-Value Problems*, 3<sup>rd</sup> Edition, PWS Publishing Company, 1997.
5. V. I. Arnold and R. Cooke, *Ordinary Differential Equations*, 2006 Edition, Springer, 2006.

**Course Code:** MAT-3503

**Title:** Differential Geometry-I

**Credit Hrs:** 03

**Course Outline:** Historical Background, Motivation and Applications, Index Notation and Summation Convention, Space Curves, The Tangent Vector Field, Reparametrization; Arc Length, Curvature, Principal Normal, Binormal, Torsion, The Osculating, The Normal and the Rectifying Planes, The Frenet-Serret Theorem, Spherical Images, Sphere Curves, Spherical Contacts, Fundamental Theorem of Space Curves, Line Integrals and Green's Theorem, Local Surface Theory, Coordinate Transformations, The Tangent and the Normal Planes, Parametric Curves, The First Fundamental Form and the Metric Tensor, Normal and Geodesic Curvatures, Gauss's Formulae, Christoffel Symbols of First and Second Kinds, Parallel Vector Fields Along a Curve and Parallelism, The Second Fundamental Form and the Weingarten Map, Principal, Gaussian, Mean and Normal Curvatures, Dupin Indicatrices, Conjugate and Asymptotic Directions, Isometries and the Fundamental Theorem of Surfaces

#### **Texts and Reference Books**

1. M. P. Do Carmo, *Differential Geometry of Curves and Surfaces*, Prentice Hall, 1976.
2. A. Goetz, *Introduction to Differential Geometry*, Addison Wesley, 1970.
3. R. S. Millman and G. D. Parker, *Elements of Differential Geometry*, Prentice Hall, 1977.
4. A. N. Pressley, *Elementary differential geometry*, 2<sup>nd</sup> Edition, Springer-Verlag, 2012.
5. D. J. Struik, *Lectures on Classical Differential Geometry*, Addison Wesley, Massachusetts, 1977.

**Course Code:** MAT-3504

**Title:** Analytical Mechanics

**Credit Hrs:** 03

**Course Outline:** Kinematics of Particles, Motion in Resisting Medium, Variable Mass Problem, Euler's Theorem and Chasles' theorem, **Moving Coordinate System:** Motion Relative to the Rotating Earth, **The Motion of a System of Particles:** Work, Power, Energy, center of mass, Generalized Coordinates, Lagrange's and Hamilton's Equations, Hamiltonian Principle, Simple Applications, Properties of a Rigid Body, Motion under No Forces, **Motion of Rigid Bodies in Three Dimensions:** General motion of rigid bodies in space. The momental ellipsoid and equimomental systems. Angular momentum vector and rotational kinetic energy. Principal axes and principal moments of inertia. Determination of 16 principal axes by diagonalizing the inertia matrix. **Euler Equations of Motion of a Rigid Body:** Force free motion. Free rotation of a rigid body with an axis of symmetry. Free rotation of a rigid body with three different principal moments. The Eulerian angles, angular velocity and kinetic energy in terms of Euler angles. Motion of a spinning top and gyroscopes-steady precession, sleeping top.

#### **Texts and Reference Books**

1. G. R Fowles, G.L. Cassiday, *Analytical Mechanics*, 7<sup>th</sup> Edition, Thomson Brook Cole, 2005.
2. B. Jafferson, T. Beadsdown, *Further Mechanics*, Oxford University Press, 2001.
3. Louis N. Hand, *Analytical Mechanics*, 1<sup>st</sup> Edition, Cambridge University Press, 1998.
4. Dr. C. Helrich, *Analytical Mechanics*, 1<sup>st</sup> Edition, Springer, 2016.
5. J. S. Torook, *Analytical Mechanics*, 1<sup>st</sup> Edition, Wiley-Interscience, 1999.

**Course Code:** MAT-3505

**Title:** Topology

**Credit Hrs:** 03

**Course Outline:** Overview of Metric Spaces, Convergence, and Continuity in Metric Spaces, Topological Spaces, Sub-Spaces, Closed Sets, Closures and Interiors of Sets, Boundary of a Set, Limit Point, Bases and Sub-bases, Neighborhood Base, First and Second Countable Spaces, Continuous Functions and Homeomorphism, Product Topology  $T_0$ ,  $T_1$ ,  $T_2$  Spaces and Their Characterizations and Basic Properties, Regular and Completely Regular Spaces, Normal and Completely Normal Spaces  
Compact / Countable Spaces and Their Properties, Connected Spaces

### Texts and Reference Books

1. C. W. Patty, *Foundation of Topology*, 2<sup>nd</sup> Edition, The Jones and Bartlett Publishers, 2009.
2. J. Dugundji, *Topology*, W.M. C. Brown Publisher, 1990.
3. J. R. Munkres, *Topology: A First Course in Topology*, 2<sup>nd</sup> Edition, Prentice Hall Inc. Englewood Cliffs, New Jersey, 2005.
4. G. F. Simmons, *Introduction to Topology and Modern Analysis*, Tata Mc-Graw Hill, 1963.
5. Munkres, *Topology*, 2<sup>nd</sup> Edition, Pearson India, 2015.

**Course Code:** MAT-3506

**Title:** Abstract Algebra

**Credit Hrs:** 03

**Course Outline:** Sets and Structures, Basic Axioms and Order of a Group, Subgroups, Subgroups Generated by Subset of a Group, System of Generators, Cyclic Group, Cosets, Lagrange's Theorem, Permutations, Even and Odd Permutations, Cycles, Lengths of Cycles, Transpositions, Symmetric and Alternating Group, Normalizers and Centralizers of a Subset of a Group, Centre of a Group, Normal Subgroup, Quotient Groups, Conjugacy Relation between Elements and Subgroups, Homomorphism and Isomorphism between Groups, Homomorphism and Isomorphism Theorems,

### Texts and Reference Books

1. J. B. Fraleigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. N. Jacobson, *Basic Algebra*, Vol. 1, W.H. Freeman and Company, 1985
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. D. S. Dummit and R. M. Foote, *Abstract Algebra*, 3rd Edition, Wiley, 2003.
5. J. A. Gallian, *Contemporary abstract algebra*, D.C. Heath, 1986.

### Semester-VI

**Course Code:** MAT-3601

**Title:** Real Analysis-II

**Credit Hrs:** 03

#### Course Outline:

**The Riemann-Stieltjes Integrals:** Definition and existence of integrals. Properties of integrals. Fundamental theorem of calculus and its applications. Change of variable theorem. Integration by parts. **Functions of Bounded Variation:** Definition and examples. Properties of functions of bounded variation. **Improper Integrals:** Types of improper integrals, tests for convergence of improper integrals. Beta and gamma functions. Absolute and conditional convergence of improper integrals. **Sequences and Series of Functions:** Power series, definition of point-wise and uniform convergence. Uniform convergence and continuity. Uniform convergence and differentiation. Examples of uniform convergence.

### Texts and Reference Books

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Mathematical Analysis*, Mc-Graw Hill, New York, 1987.
3. T. M. Apostol, *Mathematical Analysis*, 6<sup>th</sup> Edition, Addison Wesley, 1982.
4. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3<sup>rd</sup> Edition, John Wiley and Sons, 1999.
5. S. Lang, *Real Analysis*, Springer-Verlag, London, 1987.

**Course Code:** MAT-3602

**Title:** Partial Differential Equations

**Credit Hrs:** 03

#### Course Outline:

**First order PDEs:** Introduction, formation of PDEs, solutions of PDEs of first order, The Cauchy's problem for quasilinear first order PDEs, First order nonlinear equations, Special types of first order equations, **Second order PDEs:** Basic concepts and definitions, Mathematical problems, Linear operators, Superposition, Mathematical models: The classical equations, the vibrating string, the vibrating membrane, conduction of heat solids, canonical forms and variable, PDEs of second order in two independent variables with constant and variable coefficients, Cauchy's problem for second order PDEs in two independent variables

**Methods of separation of variables and Green's Functions:** Solutions of elliptic, parabolic and hyperbolic PDEs in Cartesian and cylindrical coordinates



### Texts and Reference Books

1. P. Duhaure and D. Zachmann, *Partial Differential Equations*, Mc-Graw Hill, 1986.
2. J. Fritz, *Partial Differential Equations*, Spriger-Verlag, New York, 1979.
3. R. Haberman, *Elementary Applied Partial Differential Equations*, Prentice Hall Inc., 1983.
4. M. Humi and W.B. Miller, *Boundary Value Problems and Partial Differential Equations*, PWS-Kent Publishing Company, Boston, 1992.
5. E. Zauderer, *Partial Differential Equations of Applied Mathematics*, John Wiley and Sons, Englewood Cliff, New York, 1983.

**Course Code:** MAT-3603

**Title:** Numerical Methods-I

**Credit Hrs:** 03

**Course Outline:** Computer Arithmetic, Approximations and Errors; Methods for the Solution of Non-Linear Equations and Their Convergence: Bisection Method, Regula-Falsi, Fixed Point Iteration, Newton-Raphson, Secant and Householder's Method, Error Analysis for Iterative Methods Interpolation and Polynomial Approximation: Lagrange Interpolation, Newton's Divided Difference, Forward-Difference and Backward-Difference Formulae, Hermite Interpolation, Numerical Integration and Error Estimates: Rectangular Rule, Trapezoidal Rule, Simpson's One-Three and Three-Eight Rules. Numerical Solution of Systems of Algebraic Linear Equations: Gauss-Elimination Method, Gauss-Jordan Method, Matrix Inversion, LU-Factorization, Doolittle's, Crout's, Cholesky's Methods, Gauss-Seidel and Jacobi Methods, Matrix Norms, Method of Least Squares, Eigenvalues and Eigenvectors: Power Method

### Texts and Reference Books

1. K. E. Atkinson, *An Introduction to Numerical Analysis*, 2<sup>nd</sup> Edition, John Wiley and Sons, New York, 1989.
2. R.L. Burden and J.D. Faires, *Numerical Analysis*, 5<sup>th</sup> Edition, PWS Publishing Company, 1993.
3. S.C. Chapra and R.P. Canale, *Numerical Methods for Engineers*, Mc-Graw Hill, New York, 1988.
4. A. Greenbaum and T. P. Chartier, *Numerical Methods*, 2012 Edition, Princeton University Press, 2012.
5. J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.

**Course Code:** MAT-3604

**Title:** Complex Analysis

**Credit Hrs:** 03

**Course Outline:** The Algebra and the Geometry of Complex Numbers, Complex Functions, Parametric Curves in the Complex Plane, Linear Mappings, Special Power Functions, Reciprocal Functions, Limit and Continuity, Complex Functions as Vector Fields, Derivative, Analytic Functions, Cauchy-Riemann Equations, Complex Exponential, Logarithmic, Trigonometric, Hyperbolic Functions and Their Derivatives, Harmonic Functions, Contour Integrals, the Cauchy-Goursat Theorem, Cauchy Integral Formulas, the Morera Theorem, Maximum Modulus Principle, The Liouville Theorem, Fundamental Theorem of Algebra, Convergence of Sequences and Series, The Taylor and the Laurent Series, Uniqueness of Representation, Zeros of Analytic Functions Residues, Poles and the Residue Theorem, Evaluation of Improper Integrals, Integrals Around a Branch Point, The Argument Principle and the Rouché's Theorem

### Texts and Reference Books

1. R.V. Churchill and J.W. Brown, *Complex Variables and Applications*, 5<sup>th</sup> Edition, Mc-Graw Hill, New York, 1989.
2. E. Hille, *Analytic Function Theory*, Vol. I and II, Chelsea Publishing Company, New York, 1974.
3. J. E. Marsden, *Basic Complex Analysis*, W. H. Freeman and Company, 1982.
4. D. G. Zill, and P. D. Shanahan, *A First Course in Complex Analysis with Applications*, Jones and Bartlet Publishers, Sudbury, Massachusetts, 2008.
5. L. V. Ahlfors, *Complex Analysis*, 3<sup>rd</sup> Edition, McGraw Hill Education (India) Private Limited, 2013.

**Course Code:** MAT-3605

**Title:** Tensor Analysis

**Credit Hrs:** 02

**Course Outline:** Introduction to general tensors, Summation Convention, Kronecker Delta, Levi-Civita Symbol, Vectors as Quantities Transforming Under Rotations with Notation, The Spherical-Polar and the Cylindrical-Coordinate Meshes, Alternating Symbol, Relation between Alternating Symbol and Kronecker Delta, Tensors of First, Second and Higher Orders, Algebra of Tensors, Contraction of Tensor, Quotient Theorem, Symmetric and Skew-Symmetric Tensors, Invariance Property, Isotropic Tensors, Differentiation of Tensors, Application of Tensors in Modeling Anisotropic Systems, Study of Physical Tensors, Diagonalization of Inertia Tensor as Aligning Coordinate Frame with Natural Symmetries of the System

**Texts and Reference Books**

1. D.E. Bourne and P.C. Kendall, *Vector Analysis and Cartesian Tensors*, 2<sup>nd</sup> Edition, Thomas Nelson, 1977.
2. G. E. Hay, *Vector and Tensor Analysis*, Dover Publications, Inc., New York, 1979.
3. N.A. Shah, *Vector and Tensor Analysis*, A-One Publishers, Lahore, 2005.
4. I. S. Sokolnikoff, *Tensor Analysis: Theory and Application*, John Wiley and Sons, New York, 1951.
5. J. L. Synge and A. Schild, *Tensor Calculus*, Courier Dover Publications, 1978.

**Course Code:** MAT-3606

**Title:** Scientific Programming

**Credit Hrs:** 2+1

**Course Outline** (Matlab, Maple, Mathematica): A list of contents is given below. However the instructor may add or remove some of the contents depending on the need of the students.

Curve sketching (only graphs of functions of one variable in Cartesian Coordinates) by using standard procedure, Intro to MATLAB (history, installation, interface, using product help, etc), MATLAB vs Maths syntax, sketching plane curves and surfaces in MATLAB, use of MATLAB in linear algebra, symbolic computations using MATLAB, creating script and function m-files, MATLAB codes for Bisection, Newton-Raphson, secan, Regula-Falsi, Jacobi, GS, Euler, and RK-4 methods. A brief introduction to Maple/Mathematica, comparison between similar features of MATLAB and Maple/Mathematica.

The following points are important for teaching this course:

1. The course should be taught in a computer lab setting
2. At the completion of this course, the students must be able to utilize the software to solve computationally difficult problems
3. The students should have a good command on at least two of the three programs mentioned above

**Texts and Reference Books**

1. D. M. Etter, D. Kuncicky and D. Hull, *Introduction to Matlab-6*, Prentice Hall, 2001.
2. F. Garvan, *The Maple Book*, Chapman and Hall/CRC, 2002.
3. A. Gilat, *MATLAB: An Introduction with Applications*, 5<sup>th</sup> Edition, Wiley, 2014.
4. L. Nichal, *Maple*, 1<sup>st</sup> Edition, Nancy Paulsen Books, 2014.
5. S. Kaufmann, *Mathematica as a Tool: An Introduction with Practical Examples*, Springer-Verlag, 1994.

**Semester-VII**

**Course Code:** MAT-4701

**Title:** Measure Theory

**Credit Hrs:** 03

**Course Outline:** Definition and Examples of Algebra and  $\sigma$ -Algebra, Basic Properties of Measurable Spaces, Definition and Examples of Measure Spaces, Outer Measure, Lebesgue Measure, Measurable Sets, Complete Measure Spaces Measurable Functions: Some Equivalent Formulations of Measurable Functions, Examples of Measurable Functions, Various Characterizations of Measurable Functions, Properties that Hold Almost Everywhere Definition of Lebesgue Integral, Basic Properties of Lebesgue Integrals, Comparison between Riemann Integration and Lebesgue Integration,  $L_2$ -Spaces

### Texts and Reference Books

1. D. L. Cohn, *Measure Theory*, Birkhauser, 1980.
2. P. R. Halmos, *Measure Theory*, D. Van Nostrand, 1950.
3. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
4. T. Tao, *An Introduction to Measure Theory*, American Mathematical Society, 2011.
5. P. R. Halmos, *Measure Theory*, 2<sup>nd</sup> Edition, Springer, 1978.

**Course Code:** MAT-4702

**Title:** Mathematical Physics

**Credit Hrs:** 03

**Course Outline:** Definition and Properties of Laplace and Inverse Laplace Transforms, s-shifting property of LT, existence and uniqueness theorem, LT of derivatives and integrals and solution of ivps, unite step function and t-shifting property of LT, solution of circuit problems by using LT, Dirac Delta Function and its properties, LT of periodic functions, Convolution Theorem, Convolution of discontinuous functions, solution of integral equations by LT, differentiation and integration of LT, Laguerre's equation and polynomials, Applications of Laplace Transforms to systems of ODEs and PDEs, Fourier Series of  $2\pi$  and  $2L$  periodic functions, Convergence and sum of FS, even and odd functions and half-range expansions of FS, solution of odes and pdes by using FS, Fourier Integrals, Fourier Sine and Cosine integrals, Fourier sine and cosine transforms, Fourier sine and cosine transforms of derivatives, existence of FT, FT of derivatives, Convolution theorem, Discrete and Fast Fourier Transforms, solution of odes and pdes by using FT.

### Texts and Reference Books

1. E. Kreyszig, *Advanced Engineering Mathematics*, 10<sup>th</sup> Edition, Wiley, 2011.
2. E. L. Butkov, *Mathematical Physics*, Addison Wesley, 1973.
3. R. P. Kanwal, *Linear Integral Equations*, Academic Press, 1971.
4. T. Myint-U and L. Denbnath, *Partial Differential Equations*, Elsevier Science Publishing, 1987.
5. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Vol. II, Mc-Millan Publishing Company, Inc., New York, 1968.

**Course Code:** MAT-4703

**Title:** Numerical Methods-II

**Credit Hrs:** 03

**Course Outline:** IVP for ODEs: Elementary theory of ivps, Introduction to Single-Step Numerical Methods for solution of ivps, Picard's method, Euler's Method, Second and higher order Taylor's methods, RK-methods (mid-point, modified Euler, Heun's, and RK-4 methods), Multi-Step methods for numerical solutions of odes (2-, 3-, 4-, and 5-step Adam-Bashforth and Adam-Moulton methods), Extension of Euler and RK-4 methods for numerical solutions of higher order odes and system of first order odes, stability, consistency, and convergence of SS and MS methods, stiff odes, region of absolute stability and A-Stability, BVPs for odes: Discussion on Problem Behavior and Stability, Shooting method and finite difference methods for Linear and Non-Linear BVPs, Rayleigh-Ritz method for Linear and Non-Linear BVPs.

### Texts and Reference Books

1. U. Ascher and L. Petzold, *Computer Methods for ODEs and DAEs*, SIAM, 1998.
2. R.L. Burden and J.D. Faires, *Numerical Analysis*, 5<sup>th</sup> Edition, PWS Publishing Company, 1993.
3. U. Ascher, R. Matteij and R. Russell, *Numerical Solution of BVPs for ODEs*, Prentice Hall, 1988.
4. J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.
5. A. Greenbaum and T. P. Chartier, *Numerical Methods*, 2012 Edition, Princeton University Press, 2012.

**Course Code:** MAT-4704

**Title:** Functional Analysis

**Credit Hrs:** 03

**Course Outline:** Definition and Examples of Normed Spaces, Banach Spaces, Characterization of Banach Spaces, Bounded Linear Transformations, Bounded Linear Operators, Functional and Their Examples, Various Characterization of Bounded (Continuous) Linear Operator, The Space of All Bounded Linear Operators, The Open Mapping and Closed Graph Theorems, The Dual (Conjugate) Spaces, Reflexive Spaces, Hahn-Banach Theorem (Without Proof), Some Important Consequences of the Hahn- Banach Theorem. Inner Product Spaces, Hilbert Spaces, Orthonormal Bases, Convexity in Hilbert Spaces, Operators in Hilbert Spaces, Invariant Sub-Spaces, Decomposition of Hilbert Spaces, Finite Dimensional Spectral Theory and Spectral Mapping Theorem.

**Texts and Reference Books**

1. E. Kreyszig, *Introductory Fundamental Analysis with Applications*, John Wiley and Sons, 1978.
2. I. J. Maddox, *Elements of Functional Analysis*, Cambridge University Press, 1970.
3. W. Rudin, *Functional Analysis*, Mc-Graw Hill, 1983.
4. G. F. Simmon, *Introduction to Topology and Modern Analysis*, Mc-Graw Hill, New York, 1983.
5. J. Muscat, *Functional Analysis*, 2014 Edition, Springer, 2014.

**Course Code:** MAT-4705

**Title:** Fluid Mechanics-I

**Credit Hrs:** 03

**Course Outline:** Fields and Continuum Concepts, Lagrangian and Eulerian Specifications, Local, Convective and Total Rates of Change, Conservatoin of Mass, Equation of Continuity, Boundary Conditions, Nature of Force in a Fluid Field and Their Effects: Surface and Body Forces, Stress at a Point, Viscosity and Newton's Viscosity Law, Viscous and Inviscid Flows, Laminar and Turbulent Flows, Compressible and Incompressible Flows  
Irrotational Fluid Motion: Velocity Potential from an Irrotational Velocity Field, Streamlines. Vortex Lines and Vortex Sheets, Kelvins Minimum Energy Theorem, Conservation of Linear Momentum, Bernoullis Theorem and Its Applications, Circulations, Rate of Change of Circulation (Kelvins Theorem), Axially Symmetric Motion, Stokes Stream Function  
Two-Dimensional Motion: Stream Function, Complex Potential and Complex Velocity, Uniform Flows, Sources, Sinks and Vortex Flows, Flow in a Sector, Flow Around a Sharp Edge, Flow Due to a Doublet

**Texts and Reference Books**

1. I. G. Curie, *Fundamentals of Mechanics of Fluids*, 3<sup>rd</sup> Edition, CRC, 2002.
2. I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
3. R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
4. H. Schlichting, K. Gersten, E. Krause and H. Oertel, Jr, *Boundary-Layer Theory*, 8<sup>th</sup> Edition, Springer-Verlag, 2004.
5. Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

**Course Code:** MAT-4706

**Title:** Operation Research

**Credit Hrs:** 03

**Course Outline:** Introduction to Operation Research and Real Life Phases, Introduction to Linear Programming (LP) with Examples, Graphical Solutions to Mathematical Model with Special Cases, Simplex Algorithm and its Different Cases, Big M Method and Two Phase Method, Scheduling and Blending Problems, The Transportation Problems, The Transshipment Problems, The Assignment Problems, Integer Programming, Network Models, Inventory Models

**Texts and Reference Books**

1. Hillier and Lieberman, *Introduction to Operations Research*, 9<sup>th</sup> Edition, Mc-Graw Hill, 2010.
2. P. R. Murthy, *Operations Research*, New Age International (P) Limited Publishers, New Delhi, 2007.
3. Taha and Hamdy, *Operations Research*, 7<sup>th</sup> Edition, Mc-MillanPublishing Company, Inc., New York, 2003.
4. W. L. Winston, *Practical Management Science: Spreadsheet Modeling and Applications*
5. F. S. Hillier and G. J. Liberman, *Operations Research*, 9<sup>th</sup> Edition, McGraw-Hill Science/Engineering/Math, 2009.

**Course Code:** MAT-4707

**Title:** Discrete Structures

**Credits:** 3

**Course Outlines:** Set and Relations: Basic Notions, Set Operations, Venn Diagrams, Extended-Set Operations, Indexed Family of Sets, Countable and Uncountable Sets, Relations, Cardinality, Equivalence Relations, Congruence, Partitions, Partial Order, Representation of Relations, Mathematical Induction

Elementary Logic: Logics of Order Zero and One, Propositions and Connectives, Truth Tables, Conditionals and Bi-Conditionals, Quantifiers, Methods of Proof, Proofs Involving Quantifiers

### Texts and Reference Books

1. K. H. Rosen, *Discrete Mathematics and its Applications*, 12<sup>th</sup> Edition, Mc-Graw Hill, New York, 1999.
2. K. A. Ross and C. R. B. Wright, *Discrete Mathematics*, Prentice Hall, Englewood Cliffs, NJ, USA, 2003.
3. H. Fell and J. A. Aslam, *Discrete Structures*, 5<sup>th</sup> Edition, Cognella Academic Publishing, 2016.
4. S. S. Epp, *Discrete Mathematics with Applications*, 4<sup>th</sup> Edition, Brooks Cole, 2010.
5. B. Kolman and R. C. Busby, *Discrete Mathematical Structures*, 6<sup>th</sup> Edition, Pearson, 2017.

**Course Code:** MAT-4708

**Title:** Special Functions

**Credit Hrs:** 03

**Course Outline:** Infinite Products: introduction, Definition of an infinite product, A necessary condition for convergence, Associated series of logarithms, Convergences types, The Gamma and Beta Functions: The Euler constant, The Gamma function, A series for logarithmic differential of Gamma function, The order symbols o and O, Evaluation of certain infinite products, The Beta Function, Factorial function, Asymptotic Series: Definition of an asymptotic expansion, Algebraic properties, Term by term integration, Uniqueness, The Hypergeometric function : Simple integral form, The function  $F(a,b;c,z)$  and its properties, The Hypergeometric differential equation, Logarithmic solution of the hypergeometric function,  $F(a,b;c,z)$  as a function of parameters, Elementary series manipulation, Kummer Theorem, Generalized Hypergeometric functions, the exponential and binomial functions, A differential equation, Saalschutz theorem, Contour integral integrals of Barnes' type, the Barnes integrals and the generalized hypergeometric function, Bessel Functions and its properties, The Confluent Hypergeometric functions and its properties, Generating Functions.

### Texts and Reference Books

1. E. D. Rainville, *Special Functions*, 1st Edition, The Macmillan Company New York, 1965.
2. L. J. Slater, and D. Lit, *Confluent Hypergeometric Functions*, Cambridge University Press, London, 1960.
3. A. Erdelyi, *Higher Transcendental Functions*, Volume I, II, & III, McGraw Hill Book Company, Inc. 1953.
4. J. E. Andrews, R. Askey and R. Roy, *Special Functions*, 1<sup>st</sup> Edition, Cambridge University Press, 2001.
5. C. Viola, *Special Functions*, 1<sup>st</sup> Edition, Springer, 2016.

**Course Code:** MAT-4709

**Title:** Quantum Mechanics-I

**Credit Hrs:** 03

**Course Outline:** Black Body Radiation, Photoelectric Effect, Compton Effect, Bohr's Theory of Atomic Structure, Wave-Particle Duality, The De Broglie Postulate, Heisenberg Uncertainty Principle, The Postulates of Quantum Mechanics, Operators, Eigen-functions and Eigenvalues: Observables and Operators. Measurement in Quantum Mechanics, The State Function and Expectation Values Time, Development of the Stat Function (Schrodinger Wave Equation), Solution to the Initial-Value Problem in Quantum Mechanics, Parity Operators

Function Spaces and Hermitian Operators: Particle in a Box, Dirac Notation, Hilbert Space. Hermitian Operators, Properties of Hermitian Operators, Additional One-Dimensional Problems: Bound and Unbound States: General Properties of the One Dimensional Schrodinger Equation, Unbound States, One-Dimensional Barrier Problems, The Rectangular Barrier, Tunneling

### Texts and Reference Books

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2004.
2. H. D. Dehmen, *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics: A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Co., 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

**Course Code:** MAT-4710

**Title:** Ring Theory

**Credit Hrs:** 03

**Course Outline:**

**Rings:** Definition, examples. Quadratic integer rings. Examples of non-commutative rings. The Hamilton quaternions. Polynomial rings. Matrix rings. Units, zero-divisors, nilpotents, idempotents. Subrings, Ideals. Maximal and prime Ideals. Left, right and two-sided ideals;

Operations with ideals. The ideal generated by a set. Quotient rings. Ring homomorphism. The isomorphism theorems, applications. Finitely generated ideals. Rings of fractions.

**Integral Domain:** The Chinese remainder theorem. Divisibility in integral domains, greatest common divisor, least common multiple. Euclidean domains. The Euclidean algorithm. Principal ideal domains. Prime and irreducible elements in an integral domain. Gauss lemma, irreducibility criteria for polynomials. Unique factorization domains. Finite fields. Polynomials in several variables. Symmetric polynomials. The fundamental theorem of symmetric polynomials.

**Texts and Reference Books**

1. J. B. Fraieigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. B. Hartley and T. O. Hawkes, *Ring, Modules and Linear Algebra*, Chapman and Hall, 1980.
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. S. J. Leon, *Linear Algebra with Applications*, 6<sup>th</sup> Edition, Prentice Hall, 2002.
5. P. M. Cohn, *Introduction to Ring Theory*, 1<sup>st</sup> Edition, Springer, 2002.

**Course Code:** MAT-4711

**Title:** Analytical Dynamics

**Credit Hrs:** 03

**Course Outline:** Constraints, Generalized Coordinates, Generalized Forces, General Equation of Dynamics, Lagrange's Equations, Conservation Laws, Ignorable Coordinates, Explicit Form of Lagrange's Equation in Terms of Tensors. Hamilton' Principle of Least Action, Hamilton's Equations of Motion, Hamilton-Jacobi Method, Poisson Brackets (P.B's); Poisson's Theorem; Solution of Mechanical Problems by Algebraic Technique Based on (P.B's) Small Oscillations and Normal Modes, Vibrations of Strings, Transverse Vibrations Normal Modes, Forced Vibrations and Damping, Reflection and Transmission at a Discontinuity, Longitudinal Vibrations, Rayleigh's Principle

**Texts and Reference Books**

1. F. Chorlton, *Textbook of Dynamics*, Van Nostrand, 1963.
2. W. Chester, *Mechanics*, George Allen and Unwin Ltd. London, 1979.
3. H. Goldstein, *Classical Mechanics*, Cambridge University Press, 1980.
4. G. Meirovitch, *Methods of Analytical Dynamics*, Mc-Graw Hill, 1970.
5. H. Baruh, *Analytical Dynamics*, 1<sup>st</sup> Edition, WCB/McGraw-Hill, 1998.

**Course Code:** MAT-4712

**Title:** Approximation Theory

**Credit Hrs:** 03

**Course Outline:** Best Approximations in Normal Spaces, Existence Theorem, Approximation by Algebraic Polynomials, Uniqueness, Strict Convexity, Lemma Convexity, Uniqueness Theorem, Hilbert Space, Uniform Approximation, External Point, Haar Condition, Extreme Points, Best Approximation, Characterization of Best Approximation, A Brief Introduction to Interpolation, Chebyshev Polynomials, Chebyshev Theorem, Least Squares Approximation, Gram-Schmidt Orthonormalization Process, Orthogonal Function, Pade Approximation, Remex Algorithm

**Texts and Reference Books**

1. N. I. Achieser, *Theory of approximation*, Dover Publications, Inc., New York, 2004.
2. J. R. Rice, *The Approximation of Functions*, Vol. I, Addison Wesley Publishing Company, 1964.
3. T. J. Rivlin, *An Introduction to the Approximation of Functions*, Dover Publications, Inc., New York, 1981.
4. M. J. D. Powell, *Approximation Theory and Methods*, Cambridge University Press, 1988.
5. E. W. Cheney, *Introduction to Approximation Theory*, AMS, 2000.

**Course Code:** MAT-4713

**Title:** Differential Geometry-II

**Credit Hrs:** 03

**Course Outline:** Definition and Examples of Manifolds, Differential Maps, Sub-Manifolds, Tangents, Coordinate Vector Fields, Tangent Spaces, Dual Spaces, Multi-Linear Functions, Algebra of Tensors, Vector Fields, Tensor Fields, Integral Curves, Flows, Lie Derivatives, Brackets, Differential Forms, Introduction to Integration Theory on Manifolds, Riemannian and Semi-Riemannian Metrics, Flat Spaces, Affine Connections, Parallel Translations, Covariant Differentiation of Tensor Fields, Curvature and Torsion Tensors, Connection of a Semi-Riemannian Tensor, Killing Equations and Killing Vector Fields, Geodesics, Sectional Curvature

**Texts and Reference Books**

1. R. Abraham, J. E. Marsden and T. Ratiu, *Manifolds, Tensor Analysis and Applications*, Addison Wesley, 1983.
2. R. L. Bishop and S. I. Goldberg, *Tensor Analysis on Manifolds*, Dover Publications, Inc., New York, 1980.
3. M. P. Do Carmo, *Riemannian Geometry*, Birkhauser, 1992.
4. D. Langwitz, *Differential and Riemannian Geometry*, Academic Press, 1970.
5. E. Kreyszig, *Differential Geometry*, 1<sup>st</sup> Edition, Dover Publications, 1991.

**Course Code:** MAT-4714

**Title:** Electromagnetic Theory-I

**Credit Hrs:** 03

**Course Outline:** Electromagnetic Fields, Coulomb's Law, The Electric Field Intensity and Potential, Gauss's Law and Deductions, Piosson and Laplace Equations, Conductors and Condensers, Dipoles, The Linear Quadrupole, Potential Energy of a Charge Distribution, Dielectrics, The Polarization and Displacement Vectors, General Solutions of Laplace's Equation. Solutions of Laplace's Equation in Spherical Coordinates, Legendre's Equation, Legendre's Polynomials, Electromagnetic Fields, The Magnetostatic Law of Force, The Magnetic Induction, The Lorentz Force on a Point Charge Moving in a Magnetic Field, The Divergence of the Magnetic Field, The Vector Potential, The Conservation of Charge and Equation of Continuity, The Lorentz Condition, The Curl of The Magnetic Field, Ampere's Law and the scalar Potential, Steady and Slowly Varying Currents, Electric Current, Linear Conductors. Conductivity, Resistance, Kirchhoff's Laws, Current Density Vector, Magnetic Field of Straight and Circular Current, Magnetic Flux, Vector Potential, Forces on a Circuit in Magnetic Field

**Texts and Reference Books**

1. D. Corrisonand P. Lorrison, *Introduction to Electromagnetic Fields and Waves* , W.H. Freeman and company, London, 1962.
2. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
3. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
4. G. E. Owen, *Introduction to ElectromagneticTheory*, Dover, 2003.
5. J. R. Reitz, F. J. Milford and R. W. Christy, *Foundations, of Electromagnetic Theory*, Addison-Wesley Publishing, 1993.

**Course Code:** MAT-4715

**Title:** Conference/Seminar/Reading-I

**Credit Hrs:** S/U

**Course Outline:** The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also trained on preparing papers and presentations for conferences and seminars.

**Texts and Reference Books**

As per requirement of the students taking the course.

## Semester-VIII

**Course Code:** MAT-4801

**Title:** Mathematical Systems Theory

**Credit Hrs:** 03

**Course Outline:** Conservation laws and phenomenological principles, some principles and laws of thermodynamics, mechanics, and electromagnetism and their applications in modelling, Linearization, matrix exponentials and solution of linear differential equations, LTV systems, Impulse and step responses, Stability, controllability, and observability of LTI systems, Realization theory and Hankel matrices, Feedback and stabilizability, observers and state reconstruction, detectability, separation principle and compensation, disturbance rejection, Laplace transforms and LTI systems, transfer functions and transfer matrices, transfer functions and minimal realizations of SISO and MIMO systems, Abstract systems description and behavioral modeling, polynomial representations of systems, brief discussion of nonlinear, descriptor, stochastic, distributed parameter, and discrete event systems, optimal control theory, parameter estimation, filter theory, model reduction, and adaptive and robust control

### Texts and Reference Books

1. G. J. Olsder, J. W. van der Woude, J. G. Mask, and D. Jeltsema, *Mathematical Systems Theory*, 4<sup>th</sup> Edition, VSSD, 2011.
2. I. D. Hinrichsen and A. J. Pritchard, *Mathematical Systems Theory*, Springer
3. J. W. Polderman and J. C. Willems, *Introduction to Mathematical Systems Theory*, 2<sup>nd</sup> Edition, Springer, 2008.
4. J. Zabczyk, *Mathematical Control Theory*, 1<sup>st</sup> Edition, Birkhauser, 2007.
5. E. D. Sontag, *Mathematical Control Theory*, 2<sup>nd</sup> Edition, Springer, 1998.

**Course Code:** MAT-4802

**Title:** Mathematical Modeling

**Credit Hrs:** 03

**Course Outline:** Introduction to modeling. Basic Guide line of mathematical modeling, Collection and interpretation of data, Technique of mathematical modeling, Classification of mathematical modeling, modeling through algebra, modeling through Geometry, modeling through Trigonometry, modeling through Calculus, Limitation of modeling, Development of Models', , Discrete and Continuous models,, Linear Growth and Decay Model, Non-linear Growth and decay models, Mathematical modeling in population dynamic, Traffic flow models.

### Texts and Reference Books

1. D. Edwards and M. Hamson, *Mathematical modeling Skills*, MacMillan Press Ltd., 1996
2. F. R. Giordano, M. D. Weir, and W. P. Fox, *A First Course in Mathematical modeling*, Thomson Brooks/Cole, 2003
3. J. N. Kapur, *Mathematical modeling*, New Age International Limited, 2015.
4. S. Banerjee, *Mathematical modeling (Modell analysis and Application)*
5. J. J. Batzel, M. Bachar, and F. Kappel, *Mathematical Modeling and Validation in Physiology*, 2013

**Course Code:** MAT-4803

**Title:** Integral Equations

**Credit Hrs:** 03

**Course Outline:** Linear integral equations of the first and second kind. Relationship between differential equation and Volterra integral equation. Neumann series. Fredholm Integral equation of the second kind with separable Kernels. Eigenvalues and eigenvectors. Iterated functions. Quadrature methods. Least square methods. Homogeneous integral equations of the second kind. Fredholm integral equations of the first kind. Fredholm integral equations of the second kind. Abel's integral equations. Hilbert Schmidt theory of integral equations with symmetric Kernels. Regularization and filtering techniques, Introduction to Wiener-Hopf Technique.

### Texts and Reference Books

1. J. J. Abdul, *Introduction to Integral Equations with Applications*, Marcel Dekker Inc. New York, 1985.
2. V. Lovitt, *Linear Integral Equations*, Dover Publications, Inc., New York, 1950.
3. B. Noble, *Methods Based on the Wiener-Hopf Technique*, Pergamon Press, 1988
4. F. Smith, *Integral Equations*, Cambridge University Press, 2003
5. F. G. Tricomi, *Integral Equations*, Interscience, 1957.



**Course Code:** MAT-4804

**Title:** Optimization Theory

**Credit Hrs:** 03

**Course Outline:** Linear Programming: Simplex Method, Duality Theory, Dual and Primal-Dual Simplex Methods  
Unconstrained Optimization: Optimality Conditions, One-Dimensional Problems, Multi-Dimensional Problems and the Method of Steepest Descent, Constrained Optimization with Equality Constraints, Optimality Conditions, Lagrange Multipliers, Hessians and Bordered Hessians, Inequality Constraints, the Kuhn-Tucker Theorem and Applications

**Texts and Reference Books**

1. L. Elsgolts, *DEs and the Calculus of Variations*, Mir Publishers Moscow, 1970.
2. B. S. Gotfried and J. Weisman, *Introduction to Optimization Theory*, Prentice Hall, Englewood Cliffs, NJ, USA, 1973.
3. D. G. Luenberger, *Introduction to Linear and Non-Linear Programming*, Addison Wesley, Reading, Ma. USA, 1973.
4. H. T. Jongen and K. Meer, *Optimization Theory*, 2004 Edition, Springer, 2004.
5. A. Beck, *Introduction to Nonlinear Optimization: Theory, Algorithms, and Applications with MATLAB*, SIAM-Society for Industrial and Applied Mathematics, 2014.

**Course Code:** MAT-4805

**Title:** Fluid Mechanics-II

**Credit Hrs:** 03

**Course Outline:** Circular Cylinder without Circulation, Circular Cylinder with Circulation Blasius Theorem, Kutta Condition and the Flat-Plate Airfoil, Joukowski Airfoil, Vortex Motion, Karman's Vortex Street, Method of Images, Velocity Potential, Stoke's Stream Function, Solution of the Potential Equation, Uniform Flow Source and Sink, Flow Due to A Doublet Viscous Flows of Incompressible Fluids: Constitutive Equations, Navier-Stokes's Equations, Exact Solutions of Navier-Stokes's Equations, Steady Unidirectional Flow, Poiseuille Flow, Coquette Flow, Flow between Rotating Cylinders, Stoke's First Problem, Stoke's Second Problem  
Simplified Approach to Fluid Flow Problems: Similarity from Differential Equations, Dimensional Analysis, One Dimensional Steady Compressible Flow

**Texts and Reference Books**

1. I. G. Curie, *Fundamentals of Mechanics of Fluids*, 3<sup>rd</sup> Edition, CRC, 2002.
2. I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
3. R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
4. H. Schlichting, K. Gersten, E. Krause and H. Oertel, Jr, *Boundary-Layer Theory*, 8<sup>th</sup> Edition, Springer-Verlag, 2004.
5. Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

**Course Code:** MAT-4806

**Title:** Algebraic Topology

**Credit Hrs:** 03

**Course Outline:** Path Wise Connectedness with Examples, Notion of Homotopy, Homotopy Classes and its Application, Path Homotopy, Path Homotopy Classes, Fundamental Groups, Covering Mapping with Examples, Covering Spaces, Lifting Properties of Covering Spaces and its Application, Fundamental Group of a Circle (s)

**Texts and Reference Books**

1. M. J. Greeberge, *Algebraic Topology, A first Course*, Benjamin Commings, 1967.
2. C.A. Kosniowski, *First course in Algebraic Topology*, Cambridge University press, 1980.
3. A. H. Wallace, *Algebraic Topology, Homology and Cohomology*, Benjamin, 1968.
4. A. Hatcher, *Algebraic Topology*, 1<sup>st</sup> Edition, Cambridge University Press, 2001.
5. W. Fulton, *Algebraic Topology*, Springer, 1997.

**Course Code:** MAT-4807

**Title:** Comprehensive Oral Exam

**Credit Hrs:** 01

**Course Outline:** This exam will be conducted at the end of the 8<sup>th</sup> semester. One external examiners and two internal examiners will conduct this exam from each student.

**Course Code:** MAT-4808

**Title:** Project

**Credit Hrs:** 03

**Course Outline:**

The objective of this course is to train students to learn and use the tools required for writing their project report and the tools for doing their research work. They will do the literature survey, work on some research problem and write a project report by the end of the course.

**Texts and Reference Books**

As per requirements of the topic of the Project.

**Course Code:** MAT-4809

**Title:** Quantum Mechanics-II

**Credit Hrs:** 03

**Course Outline:** Harmonic Oscillator and Problems in Three-Dimensions: The Harmonic Oscillator, Eigen-Functions of the Harmonic Oscillator, The Harmonic Oscillator in Momentum Space, Motion in Three Dimensions, Spherical Symmetric Potential and the Hydrogen Atom, Angular Momentum: Basic Properties, Eigenvalues of the Angular Momentum Operators, Eigen-Functions of the Orbital Angular Momentum Operators  $L_2$  and  $L_z$ , Commutation Relations between Components of Angular Momentum and Their Representation in Spherical Polar Coordinates  
The Scattering Cross-Section, Scattering Amplitude, Scattering Equation, Born Approximation, Partial Wave Analysis, Time Independent Perturbation of Non-Degenerate and Degenerate Cases, Time-Dependent Perturbations

**Texts and Reference Books**

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2004.
2. H. D. Dehmen, *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics, A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Company, 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

**Course Code:** MAT-4810

**Title:** Introduction to Combinatorics

**Credit Hrs:** 03

**Course Outline:** Two Basic Counting Principle, Permutations, Combinations, The Injective and Bijective Principles, Arrangements and Selections with Repetitions, Graphs in Combinatorics, The Binomial Theorem, Combinatorial Identities, Properties of Binomial Coefficients, Multinomial Coefficients, The Multinomial Theorem, The Pigeonhole Principle, Examples, Ramsay Numbers, The Principle of Inclusion and Exclusion, Generalization, Integer Solutions, Surjective Mapping. Stirling Numbers of the Second Kind, The Sieve - Eratosthenes, Euler  $\Phi$ -Function, The Problem Des-Menages  
Ordinary Generating Functions, Modeling Problems, Partition of Integers, Exponential Generating Functions  
Linear Homogeneous Recurrence Relations, Algebraic Solutions of Linear Recurrence Relations and Constant Functions, The Method of Generating Functions, A Non-Linear Recurrence Relation and Catalaa Numbers

**Texts and Reference Books**

1. V. K. Balakrishnan, *Theory and Problems of Combinatorics*, Schaum's Outline Series, Mc-Graw Hill, Singapore, 1995.
2. C. C. Chen and K. M. Koh, *Principles and Techniques in Combinatorics*, World Scientific Publishing Company, Pvt. Ltd, Singapore, 1992.
3. C. L. Liu, *Introduction to Combinatorial Mathematics*, Mc-Graw Hill, New York, 1968.
4. A. Tucker, *Applied Combinatorics*, John Wiley and Sons, New York, 1985.
5. R. A. Brualdi, *Introductory Combinatorics*, 5<sup>th</sup> Edition, Pearson, 2009.

**Course Code:** MAT-4811

**Title:** Variational Inequalities

**Credit Hrs:** 03

**Course Outline:** Variational Inequalities in Fixed Points, The Characterization of the Projection onto a Convex Set, A First Theorem about Variational Inequalities, Variational Inequalities, Some Problems which Lead to Variational Inequalities, Variational Inequalities in Hilbert Space, The Obstacle Problem, Variational Inequalities for Monotone Operators, Penalization

**Texts and Reference Books**

1. C. Baiocchi and A. Capelo, *Variational and Quasi-Variational Inequalities: Applications to Free Boundary Problems*, John Wiley and Sons, New York, 1984.
2. V. Barbu, *Optimal Control of Variational Inequalities*, Pitman Adv. Pub. Program, Boston, 1984.
3. G. Isac, *Complementarity Problems and Variational Inequalities*, Springer-Verlag, 2006.
4. D. Kinderlehrer and G. Stampacchia, *An Introduction to Variational Inequalities and Their Applications*, Academic Press, New York, 1980.
5. M. A. Noor, *Principles of Variational Inequalities*, Lambert Academic Publishing, Saarbrücken, Germany, 2009.

**Course Code:** MAT-4812

**Title:** Theory of Elasticity

**Credit Hrs:** 03

**Course Outline:** Cartesian Tensors, Analysis of Stress and Strain, Generalized Hooke's Law, Crystalline Structure, Point Groups of Crystals, Reduction in the Number of Elastic Moduli Due to Crystal Symmetry, Equations of Equilibrium, Boundary Conditions, Compatibility Equation, Plane Stress and Plane Strain Problems, Two Dimensional Problem in Rectangular and Polar Coordinates, Torsion of Rods and Beams

**Texts and Reference Books**

1. E. Dieulesaint and D. Royer, *Elastic Waves in Solids*, John Wiley and Sons, New York, 1980.
2. Y. C. Funk, *Foundations of Solid Mechanics*, Prentice-Hall, Englewood Cliffs, 1965.
3. Sokolnikoff, *Mathematical Theory of Elasticity*, Mc-Graw Hill, New York.
4. S. P. Temoshenko and J. N. Goodier, *Theory of Elasticity*, 3<sup>rd</sup> Edition, McGraw Hill Education (India) Private Limited, 2015.
5. A. I. Lurie and A. Belyaev, *Theory of Elasticity*, 2005 Edition, Springer, 2005.

**Course Code:** MAT-4813

**Title:** Special Theory of Relativity

**Credit Hrs:** 03

**Course Outline:** Historical Background and Fundamental Concepts of Special Theory of Relativity, Lorentz Transformations (for Motion Along One Axis), Length Contraction, Time Dilation and Simultaneity, Velocity Addition Formulae, 3-Dimensional Lorentz Transformation, Introduction to 4-Vector Formalism, Lorentz Transformations in the 4-Vector Formalism, The Lorentz and Poincare Groups, Introduction to Classical Mechanics, Minkowski Space-Time and Null Cone, 4-Velocity, 4-Momentum and 4-Force, Application of Special Relativity to Doppler Shift and Compton Effect, Particle Scattering, Binding Energy, Particle Production and Decay, Electromagnetism in Relativity, Electric Current, Maxwell's Equations and Electromagnetic Waves, The 4-Vector Formulation of Maxwell's Equations, Special Relativity with Small Acceleration

**Texts and Reference Books**

1. H. Goldstein, *Classical Mechanics*, Addison Wesley, New York, 1962.
2. D. Inverno, *Introducing Einstein's Relativity*, Oxford University Press, 1992.
3. J. D. Jackson, *Classical Electrodynamics*, John Wiley and Sons, New York, 1962.
4. A. Qadir, *Relativity: An Introduction to the Special Theory*, World Scientific, 1989.
5. W. Rindler, *Essential Relativity*, Springer-Verlag, 1977.

**Course Code:** MAT-4814

**Title:** Electromagnetic Theory-II

**Credit Hrs:** 03

**Course Outline:** The Faraday Induction Law, Induced Electromotance in a Moving System, Inductance and Induced Electromotance, Energy Stored in a Magnetic Field, The Equations of Electromagnetism, Electromagnetic Waves: Plane Electromagnetic Waves in Free Space and Isotropic Media, The Poynting Vector in Free Space, Propagation of Electromagnetic Waves in NON-Conductors, Propagation of Plane Waves in Conducting Media, Reflection and Refraction of Plane Waves, Guided Waves, Coaxial Line, Hollow Rectangular Wave Guide, Radiation of Electromagnetic Waves, Electromagnetic Field of a Moving Charge

#### **Texts and Reference Books**

1. D. Corison and P. Lorrison, *Introduction to Electromagnetic Fields and Waves*, W.H. Freeman and company, London, 1962.
2. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
3. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
4. G. E. Owen, *Introduction to Electromagnetic Theory*, Dover, 2003.
5. J. V. Stewart, *Intermediate Electromagnetic Theory*, World Scientific, 2001.

**Course Code:** MAT-4815

**Title:** Conference/Seminar/Reading-I

**Credit Hrs:** S/U

**Course Outline:** The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also be trained on preparing papers and presentations for conferences and seminars.

#### **Texts and Reference Books**

As per requirement of the students taking the course.

**Course Code:** MAT-4816

**Title:** Measure Theory and Lebesgue Integration

**Credit Hrs:** 03

**Course Outline:** Measure Spaces: Definition and examples of algebras and  $\sigma$ -algebras, Basic properties of measurable spaces, Definition and examples of measure spaces, Outer measure, Lebesgue measure, Measurable sets, Complete measure spaces.

Measurable Functions: Some equivalent formulations of measurable functions, Examples of measurable functions, Various characterization of measurable functions, Property that holds almost everywhere, Egorov's theorem.

Lebesgue Integrations: Definition of Lebesgue integral, Basic properties of Lebesgue integrals, Comparison between Riemann integration and Lebesgue integration,  $L^2$ -space, The Riesz-Fischer theorem.

#### **Texts and Reference Books**

1. H. L. Royden, *Real Analysis*, Macmillan, 1968.
2. D. L. Cohn, *Measure Theory*, Birkhauser, 1980.
3. P. R. Halmos, *Measure Theory*, D. Van Nostrand, 1950.
4. T. Tao, *An Introduction to Measure Theory*, American Mathematical Society, 2011.
5. P. R. Halmos, *Measure Theory*, 2<sup>nd</sup> Edition, Springer, 1978.

## 9- Details of Allied Courses BS-4 Years Program

**Course Code:** HUM-1101

**Title:** Islamic Studies

**Credit Hrs:** 02

**Contents:** Introduction to Quranic Studies: Basic Concepts of Quran, History of Quran, Uloomul –Quran. Study of Selected Text of Holy Quran: Verses of Surah Al-Baqra Related to Faith (Verse No-284-286), Verses of Surah Al-Hujrat Related to Adab Al-Nabi (Verse No-1-18), Verses of Surah Al-Mumanoon Related to Characteristics of faithful (Verse No-1-11), Verses of Surah al-Furqan Related to Social Ethics (Verse No.63-77), Verses of Surah Al-Inam Related to Ihkam (Verse No-152-154). Study of Selected Text of Holy Quran: Verses of Surah Al-Ihzab Related to Adab al-Nabi (Verse No.6,21,40,56,57,58.), Verses of Surah Al-Hashar (18,19,20) Related to thinking, Day of Judgment, Verses of Surah Al-Saf Related to Tafakar, Tadabar (Verse No-1,14)

Seerat of Holy Prophet (S.A.W), Introduction to Sunnah, Introduction to Islamic Law & Jurisprudence, Islamic Culture and Civilization, Islam and Science, Islamic Economic System, Political System of Islam, Islamic History: Period of Khlaft-E-Rashida, Umayyads and Abbasids, Social System of Islam

### Texts and Recommended books:

1. H.U. Muhammad, *Emergence of Islam*, IRI, Islamabad.
2. H. U. Muhammad, *Introduction to Islam*.
3. H. H. Hassan, *An Introduction to the Study of Islamic Law*, Leaf Publication Islamabad, Pakistan.
4. A. Hasan, *Principles of Islamic Jurisprudence*, Islamic Research.

**Course Code:** ENG-1102

**Title:** English-I (Functional English)

**Credit Hrs:** 03

**Contents:** Basics of Grammar, Parts of Speech and Use of Articles, Sentence Structure, Active and Passive Voice, Practice in Unified Sentence, Analysis of Phrase, Clause and Sentence Structure, Transitive and Intransitive Verbs, Punctuation and Spelling, **Comprehension:** Answers to questions on a given text, **Discussion:** General topics and every-day conversation (topics for discussion to be at the discretion of the teacher keeping in view the level of students), **Listening:** To be improved by showing documentaries/films carefully selected by subject teachers, Translation Skills: Urdu to English, **Paragraph Writing:** Topics to be chosen at the discretion of the teacher, **Presentation skills:** Introduction

### Text and Recommended Books:

1. A. J. Thomson and A. V. Martinet, *Practical English Grammar*, Exercise 1, 3<sup>rd</sup> Edition, OUP, 1997.
2. A. J. Thomson and A. V. Martinet, *Practical English Grammar*, Exercises 2, 3<sup>rd</sup> Edition. OUP, 1997.
3. M. C. Boutin, S. Brinand and F. Grellet, *Intermediate Writing*, Oxford Supplementary Skills. 4th Impression 1993, 7 Pages 20-27 and 35-41.
4. B. Tomlinson and R. Ellis, *Reading: Upper Intermediate*, Oxford Supplementary Skills, 1992.

**Course Code:** COM-1103

**Title:** Introduction to Computer

**Credit Hrs:** 03

**Contents:** Content will be determined by the teacher with the following points in view:

At the end of the semester student must be equipped with the following:

1. Basics of the hardware and operating system
2. MS Word, Excel, Power Point
3. Use of Internet
4. Installation of Softwares
5. Handling Emails

### Texts and Recommended books:

1. D. D. W. Hajek, *Introduction to Computer*, Create Space Independent Publishing Platform, 2017.
2. G. B. Shelly, S. M. Freund and M. E. Vermaat, *Introduction to Computer*, 8<sup>th</sup> Edition, Course Technology, 2010.
3. Y. N. Patt and S. J. Patel, *Introduction to Computing Systems*, 2<sup>nd</sup> Edition, McGraw-Hill Education, 2003.
4. J. Zelle, *Python Programming: An Introduction to Computer Science*, 2<sup>nd</sup> Edition, Franklin, Beedle & Associates, 2010.

**Course Code:** PHY-1104

**Title:** Physics-I

**Credit Hrs:** 03

**Contents:** Work and Energy, Impulse and Momentum, Circular Motion, Mass and Energy, Collisions, Center of Mass, Moment, Center of Gravity, Couples, Angular Motion, Kinetic Energy of Rotation, Moment of Inertia, Parallel Axis Theorem, Momentum, Angular Momentum and Energy, Elastic Restoring Forces, Circle of Reference, Harmonic Motion Density, Pressure in a Fluid, Pressure Gauges, Pumps, Archimedes' Principle, Forces against a Dam, Surface Tension, Pressure Difference across a Surface Film, Contact Angle and Capillarity  
Equation of Continuity, Bernoulli's Equation, Applications of Bernoulli's Equation, Viscosity, Poiseuille's Law, Stokes' Law, Reynolds Number

Waves and Mathematical Description, Speed of a Transverse Wave and Longitudinal Wave, Adiabatic Character of a Longitudinal Wave, Water Waves, Superposition and Standing Waves, Longitudinal Standing Waves, Vibrations of Organ Pipes, Vibrations of Rods and Plates, Interference of Longitudinal Waves, Resonance, Sound Waves, Doppler Effect, Radiation from a Piston, Applications of Acoustic Phenomena

**Texts and Recommended books:**

1. F. W. Sears, M. W. Zemansky and H. D. Young, *University Physics*, 3<sup>rd</sup> Edition, 1963.
2. R. A. Serway and J. W. Jewett, *Principles of Physics*, 5<sup>th</sup> Edition, Brooks Cole, 2012.
3. H. C. Ohanian and J. T. Market, *Physics for Engineers and Scientists*, 3<sup>rd</sup> Edition, W. W. Norton & Company, 2006.
4. R. D. Knight, *Physics for Scientists and Engineers*, 2<sup>th</sup> Edition, Addison-Wesley, 2007.

**Course Code:** HUM-1201

**Title:** Arabic

**Credit Hrs:** 02

**Course Contents:** Arabic to Urdu Translation, Urdu to Arabic Translation, Grammar, Comprehension.

**Texts and Reference Books:** Lisaan Ul Arabi, AIOU, Islamabad.

**Course Code:** ENG-1202

**Title:** English-II (Communication Skills)

**Credit Hrs:** 03

**Contents:** Paragraph Reading (Practice in writing a good, unified, and coherent paragraph), Essay Writing, CV and Job Application, Translation Skills, Study Skills (Skimming and Scanning, intensive and extensive, and speed reading, summary and précis writing, and comprehension), Academic Skills, Personality development (emphasis on content, style, and pronunciation)

**Texts and Reference Books:**

1. A. J. Thomson and A. V. Martinet, *Practical English Grammar*, 3<sup>rd</sup> Edition, Oxford University Press, 1986.
2. M. Christine, S. Brinard, and F. Grellet, *Oxford Supplementary Skills*, 4<sup>th</sup> Impression, 1993.
3. R. Nolasco, *Upper Intermediate Writing*, Oxford Supplementary Skills, 4<sup>th</sup> Impression, 1992.
4. B. Tomlinson and R. Ellis, *Advanced Reading*, Oxford Supplementary Skills, 3<sup>rd</sup> Impression, 1991.

**Course Code:** HUM-1203

**Title:** Pak-Studies

**Credit Hrs:** 02

**Contents:** Historical Perspective: Ideological Rationale with Special Reference to Sir Syed Ahmed Khan, Allama Muhammad Iqbal and Quaid-i-Azam Muhammad Ali Jinnah, Factors Leading to Muslim Separatism, Indus Civilization, Muslim Advent, Location and Geo-physical Features.

Political and Constitutional Phases: 1947-58, 1958-71, 1971-77, 1977-88, 1988-99, 1999 and onward

Economic Institutions and Issues, Society and Social Structure, Ethnicity, Foreign Policy of Pakistan and Challenges and Futuristic Outlook of Pakistan

**Texts and Recommended books:**

1. B. S. Javed, *State & Society in Pakistan*, The Macmillan Press Ltd, 1980.
2. A. S. Zaidi, *Issue in Pakistan's Economy*, Karachi: Oxford University Press, 2000.
3. M. Safdar, *Pakistan Political Roots & Development*, Lahore, 1994.
4. W. Wayne, *The Emergence of Banglades.*, Washington, Institute of PPR, 1972.

**Course Code:** PHY-1204

**Title:** Physics-II

**Credit Hrs:** 03

**Contents:** Electric Charges, Coulomb's Law, Gauss's Law and Applications, Electrical Potential and Energy, Equipotential Surfaces, Potential Gradient, Electron Volt, Cathode Ray Oscilloscope, Capacitors, Effect of a Dielectric, Polarization and Displacement, Current, Resistance, Electromotive Force, Resistors in Series and Parallel, Kirchhoff's Rules, Ammeters and Voltmeters, Ohmmeter Magnetic Field and Flux, Motion of Charged Particles in Magnetic Fields, Thomson's Measurement of e/m, The Biot-Sarvart Law, Magnetic Field of a Long Straight Conductor and Circular Loop, Ampere's Law and Applications, Electromotive Force, Faraday's Law, Induced Electric Fields, Lenz's Law. First Law of Thermodynamics, Energy and Work in Thermodynamics, Adiabatic, Isochoric, Isothermal, Isobaric and Throttling Processes, Differential Form of the First Law of Thermodynamics, Internal Energy of an Ideal Gas and Heat capacities, Adiabatic Process of an Ideal Gas, Second Law of Thermodynamics, Heat Engines, Internal-Combustion Engines, Steam Engines, The Refrigerator, The Carnot Cycle, The Kelvin Temperature Scale, Absolute Zero, Entropy and the Second Law of Thermodynamics, Energy Conversion, Kinetic Theory of Gases

**Texts and Recommended books:**

1. H. C. Ohanian and J. T. Market, *Physics for Engineers and Scientists*, 3<sup>rd</sup> Edition, W. W. Norton & Company, 2006.
2. F. W. Sears, M. W. Zemansky and H. D. Young, *University Physics*, 3<sup>th</sup> Edition, 1963.
3. R. A. Serway and J. W. Jewett, *Principles of Physics*, 5<sup>th</sup> Edition, Brooks Cole, 2012.
4. R. D. Knight, *Physics for Scientists and Engineers*, 2<sup>th</sup> Edition, Addison-Wesley, 2007.

**Course Code:** HUM-2301

**Title:** Introduction to Sociology

**Credit Hrs:** 03

**Contents:** Introduction, Scope and Subject Matter, Sociology as a Science, Historical back ground, Basic Concepts, Social Interaction: Levels of Social Interaction, Social Groups, Culture, Norms and Social Sanctions, Socialization & Personality, Deviance and Social Control, Collective Behavior

**Texts and Recommended books:**

1. Anderson, Margaret and Howard F. Taylor, *Sociology the Essentials*, Australia, Wadsworth, 2001.
2. Brown Ken, *Sociology*, UK: Polity Press, 2004.
3. Gidden, Anthony, *Introduction to Sociology*, UK: Polity Press, 2002.
4. J. Macionis John, *Sociology*, 10<sup>th</sup> Edition New Jersey: Prentice-Hall, 2006.
5. L.Tischler Henry, *Introduction to Sociology*, 7th ed. New York: The Harcourt Press, 2002.
6. N. Frank Magill, *International Encyclopedia of Sociology*, U.S.A: Fitzroy Dearborn Publishers, 2003.
7. J.Macionis John, *Sociology*, 10<sup>th</sup> ed. South Asia: Pearson Education, 2005.
8. R.Kerbo Harold, *Sociology: Social Structure and Social Conflict*, Macmillan Pub. Co., 1989.
9. Koenig Samuel, *Sociology: An Introduction to the Science of Society*, Barnes and Nobel, 1957.

**Course Code:** ENG-2302 **Title:** English-III (Technical Writing and Presentation Skills) **Credit Hrs:** 03

**Contents:** Presentation Skills, Essay Writing (Descriptive, narrative, discursive, argumentative), Academic Writing (How to write a proposal for research paper/term paper, how to write a research/term paper with emphasis on style, contents, language, form, clarity, consistency), Technical Report Writing, Progress report Writing.

**Texts and Reference Books:**

1. J. Langan, *Advanced Writing*, Townsend Press, 2014.
2. J. Langan, *College Writing Skills*, Mc Graw Hill, 2004.
3. L. G. Kirsner and S. R. Mandell, *Patterns of College Writing*, 13<sup>th</sup> Edition, Bedford/St. Martin's, 2016.
4. A. J. Thomson and A. V. Martinet, *Practical English Grammar*, 3<sup>rd</sup> Edition, Oxford University Press, 1986.

**Course Code:** HUM-2308

**Title:** Organizational Behavior

**Credit Hrs:** 03

**Course Contents:**

Introduction to HRM, Human Resource Planning, Job Design and Analysis, Recruitment & Selection, Motivation & Reward System, Career Planning & Development, Training & Development, Performance Appraisal, Compensation Management & Employee Relation, Employee Health and Safety.

**Texts and Recommended books:**

1. Garry Dessler, *Human Resource Management*.
2. Garry Dessler, *Human Resource Management*.
3. Dale S. Beach, *Personnel The Management of people at work*.
4. Holdin, *Human Resource Management*.

**Course Code:** PSY-2401

**Title:** Educational Psychology

**Credit Hrs:** 03

**Course Contents:** Introduction, Nature and Application of Psychology with Special Reference to Pakistan, Historical Background (A Brief Survey), Methods of Psychological Study, Biological Basis of Behavior, Vision, Audition, Perception, Attention, Motives, Emotions, Learning, Memory, Tools of Thinking, Individual Differences

**Texts and Recommended books:**

1. R. C. Atkinson and E. E. Smith *Introduction to psychology*, Harcourt Brace College Publishers, 2000.
2. L.D. Fernald and P.S. Fernald, *Introduction to psychology*, USA: W M C Brown Publishers, 2005.
3. W. E. Glassman, *Approaches to psychology*, Open University Press, 2000.
4. N. Hayes *Foundation of psychology*, 3<sup>rd</sup> Edition, Thomson Learning, 2000.
5. B. B. Lahey, *Psychology: An introduction*, 8<sup>th</sup> Edition, Mc Graw Hill Companies, Inc. (2004).

**Course Code:** ENG-2409

**Title:** Business Mathematics

**Credit Hrs:** 03

**Contents:** Basic mathematical concepts and their application in various business real numbers, Linear equations and their applications, System of linear equations, Functions (linear functions, quadratic and polynomial functions, exponential and logarithmic functions), Matrix algebra, Differentiation and Integration, Mathematics of finance, Ratios, Proportions and Percentages, Principle of simple Interest, Principle of compound Interest, Annuities, Loans and Mortgages, Investment decisions, Discrete and continuous variables, Linear equations and inequalities and graphs, Progression of Sequence and Series and their applications in business, Permutations, Combination and their applications in business and finance.

**Texts and Recommended books:**

1. Frank S. Budnick: *Applied Mathematics for Business and Economics and Social sciences*.
2. E. K. Bowen and G. D. Prichett, *Mathematics with applications in Management and Economics*, 6<sup>th</sup> Edition, McGraw-Hill Inc, 1986.



3. G. Clendenen and S. A. Salzman, *Business Mathematics*, 13<sup>th</sup> Edition, Pearson, 2014.
4. C. D. Miller, G. Clendenen and S. A. Salzman, *Business Mathematics*, 12<sup>th</sup> Edition, Pearson, 2011.

**Course Code:** HUM-2410

**Title:** Entrepreneurship

**Credit Hrs:** 03

**Course Contents:**

Introduction: The concept of entrepreneurship, the economist view of entrepreneurship, The sociologist view, Behavioural approach, Entrepreneurship and Management. The Practice of Entrepreneurship: The process of entrepreneurship, Entrepreneurial Management, The entrepreneurial business, Entrepreneurship in service institutions, The new venture Entrepreneurship and Innovation: The innovation concepts, Importance of innovation for entrepreneurship, Sources of innovative opportunities, The innovation process, Risks involved in innovation Developing Entrepreneur: Entrepreneurial profile, Trait approach to understanding entrepreneurship, Factors influencing entrepreneurship, The environment, Socio cultural factors, Support systems Entrepreneurship Organization: Team work, Networking organization, Motivation and compensation, Value system Entrepreneurship and SMES: Defining SMEs, Scope of SMEs, Entrepreneurial managers of SME, Financial and marketing problems of SMEs Entrepreneurial Marketing: Framework for developing entrepreneurial marketing, Devising entrepreneurial marketing plan, Entrepreneurial marketing strategies, Product quality and design Entrepreneurship and Economic Development: Role of entrepreneur in the economic development generation of services, Employment creation and training, Ideas, knowledge and skill development, The Japanese experience Case Studies of Successful Entrepreneurs

**Recommended Books:**

1. S. Mariotti and C. Glackin, *Small Business and Entrepreneurship*, 1<sup>st</sup> Edition, Prentice Hall, 2011.
2. D. B. Audretsch, M. C. Kelibach and E. E. Lehmann, *Entrepreneurship for Economic Growth*, 1<sup>st</sup> Edition, Oxford University Press, 2006.
3. Peter F. Drucker, *Innovation and Entrepreneurship*, Harper Business, 2006.
4. J. Bessant and J. Tidd, *Innovation and Entrepreneurship*, 3<sup>rd</sup> Edition, Wiley, 2015.

## 2. Scheme of Studies for MSc Mathematics: General Breakup

|     | Content                 | Description  | Remarks |
|-----|-------------------------|--|---------|
|     |                         | Intermediate with Mathematics  |         |
| 2.1 |                         | No D-grade in academic career  |         |
|     | Entrance Requirement    | Entry Test conducted by the University with the following breakup:<br>Mathematics: 80 %, English: 20%<br>Merit shall be determined on 10% of SSC, 50% of Intermediate and 40% of Entry Test marks. |         |
| 2.2 | Duration of the Program | 4-8 Semesters  |         |
|     |                         | Course Work: 65 Credit Hrs   |         |
| 2.3 | Total Credit Hours      | Project (Compulsory): 3 Credit Hrs<br>Comprehensive Oral Examination: 2 Credit Hrs<br>Conference/Seminars/Readings I & II: S/U   |         |

### 2.4 Semester-Wise Breakdown

| Course Code                        | Course Title                    | Lec. Hrs. | Lab. Hrs. | Credit Hrs. |
|------------------------------------|---------------------------------|-----------|-----------|-------------|
| <b>Semester-I</b>                  |                                 |           |           |             |
| MAT-5101                           | Real Analysis-I                 | 3         | 0         | 3           |
| MAT-5102                           | Ordinary Differential Equations | 3         | 0         | 3           |
| MAT-5103                           | Differential Geometry-I         | 3         | 0         | 3           |
| MAT-5104                           | Analytical Mechanics            | 3         | 0         | 3           |
| MAT-5105                           | Topology                        | 3         | 0         | 3           |
| MAT-5106                           | Abstract Algebra                | 3         | 0         | 3           |
| <b>Semester-II</b>                 |                                 |           |           |             |
| MAT-5201                           | Real Analysis-II                | 3         | 0         | 3           |
| MAT-5202                           | Partial Differential Equations  | 3         | 0         | 3           |
| MAT-5203                           | Numerical Methods I             | 3         | 0         | 3           |
| MAT-5204                           | Complex Analysis                | 3         | 0         | 3           |
| MAT-5205                           | Tensor Analysis                 | 2         | 0         | 2           |
| MAT-5206                           | Scientific Programming          | 2         | 1         | 3           |
| <b>Semester-III</b>                |                                 |           |           |             |
| MAT-6302                           | Mathematical Physics            | 3         | 0         | 3           |
| MAT-6304                           | Functional Analysis             | 3         | 0         | 3           |
| MAT-6305                           | Fluid Mechanics-I               | 3         | 0         | 3           |
| MAT-6316                           | Thesis                          | 6         | 0         | 6           |
| MAT-6315                           | Conference/Seminar/Readings-I   | S/U       |           |             |
| <b><u>Two Optional Courses</u></b> |                                 |           |           |             |
| MAT-6301                           | Measure Theory                  | 3         | 0         | 3           |

|          |                          |   |   |   |   |
|----------|--------------------------|---|---|---|---|
| MAT-6303 | Numerical Methods II     | 3 | 0 | 3 |   |
| MAT-6306 | Operation Research       | 3 | 0 | 3 |   |
| MAT-6307 | Number Theory            | 3 | 0 | 3 |   |
| MAT-6308 | Mathematical Statistics  | 3 | 0 | 3 |   |
| MAT-6309 | Quantum Mechanics-I      |   | 3 | 0 | 3 |
| MAT-6310 | Ring Theory              | 3 | 0 | 3 |   |
| MAT-6311 | Analytical Dynamics      | 3 | 0 | 3 |   |
| MAT-6312 | Approximation Theory     | 3 | 0 | 3 |   |
| MAT-6313 | Differential Geometry-II | 3 | 0 | 3 |   |
| MAT-6314 | Electromagnetic Theory-I | 3 | 0 | 3 |   |

#### Semester-IV

|          |                                |   |     |   |   |
|----------|--------------------------------|---|-----|---|---|
| MAT-6403 | Integral Equations             |   | 3   | 0 | 3 |
| MAT-6405 | Fluid Mechanics-II             |   | 3   | 0 | 3 |
| MAT-6407 | Comprehensive Oral Examination | 2 |     | 0 | 2 |
| MAT-6415 | Conference/Seminar/Readings-II |   | S/U |   |   |

#### Three Optional Courses

|            |   |   |   |   |   |
|------------|---|---|---|---|---|
| MAT-6401   | Mathematical Systems Theory             | 3 | 0 | 3 |   |
| MAT-6402   | Mathematical Modeling                   | 3 | 0 | 3 |   |
| MAT-6404   | Special Functions                       | 3 | 0 | 3 |   |
| MAT-6406   | Algebraic Topology                      |   | 3 | 0 | 3 |
| MAT-6408** | Measure Theory and Lebesgue Integration |   | 3 | 0 | 3 |
| MAT-6409   | Quantum Mechanics-II                    | 3 | 0 | 3 |   |
| MAT-6410   | Introduction to Combinatorics           | 3 | 0 | 3 |   |
| MAT-6411   | Theory of Elasticity                    | 3 | 0 | 3 |   |
| MAT-6412   | Optimization Theory                     |   | 3 | 0 | 3 |
| MAT-6413   | Special Theory of Relativity            |   | 3 | 0 | 3 |
| MAT-6414   | Electromagnetic Theory-II               |   | 3 | 0 | 3 |
| MAT-6416   |   |   |   |   |   |

**Note:-** Elective course mentioned above without any pre-requisite can be taught in 3<sup>rd</sup> or 4<sup>th</sup> semester. These courses can only be offered on the availability of the relevant teacher

\*In BOS 2017, change this with MAT-6316 code, 4608 will be vacaned. We may also give it 6308 code but then we have to shuffle mathematical statistics and some other courses

## 2.5 Details of the Courses in M.Sc Mathematics

### Semester-I

**Course Code:** MAT-5101

**Title:** Real Analysis-I

**Credit Hrs:** 03

**Course Outline:** Supremum and Infimum, Completeness Properties of the Real Numbers, Limits of Numerical Sequences, Limits and Continuity, Properties of Continuous Functions on Closed Bounded Intervals, Derivatives in One Variable, The Mean Value Theorem, Sequences of Functions, Power Series, Point-Wise and Uniform Convergence, Riemann Integrations

#### Texts and Reference Books

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Real Analysis*, Mc-Graw Hill, 1995.
3. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3<sup>rd</sup> Edition, John Wiley and Sons, 1999.
4. R. L. Brabenec, *Introduction to Real Analysis*, PWS Publishing Company, 1994.
5. S. Lang, *Real Analysis*, Springer-Verlag, London, 1987.

**Course Code:** MAT-5102

**Title:** Ordinary Differential Equations

**Credit Hrs:** 03

**Course Outline:** **Review** of first order linear and nonlinear odes and higher order linear odes and their solution techniques. **Basic theory** of systems of first order linear equations, Homogeneous linear system with constant coefficients, Non homogeneous linear system, **Sturm-Liouville** (S-L) System and Boundary-Value Problems, **Series Solution and its Limitations**, The Frobenius Method, Solution of the Bessel, The Hypergeometric, The Legendre and the Hermite Equations, Properties of the Bessel, the Legendre and the Hermite Functions

#### Texts and Reference Books

1. E. A. Coddington and N. Levinson, *Theory of Ordinary Differential Equations*, Mc-Graw Hill, New York, Toronto and London, 1955.
2. W. E. Boyce and R. de Prima, *Elementary Differential Equations*, 9<sup>th</sup> Edition, Wiley, 2008.
3. P. Hartman, *Ordinary Differential Equations*, John Wesley and Sons, New York, 1964.
4. D. G. Zill and M. R. Cullen, *Differential Equations with Boundary-Value Problems*, 3<sup>rd</sup> Edition, PWS Publishing Company, 1997.
5. V. I. Arnold and R. Cooke, *Ordinary Differential Equations*, 2006 Edition, Springer, 2006.

**Course Code:** MAT-5103

**Title:** Differential Geometry-I

**Credit Hrs:** 03

**Course Outline:** Historical Background, Motivation and Applications, Index Notation and Summation Convention, Space Curves, The Tangent Vector Field, Reparametrization; Arc Length, Curvature, Principal Normal, Binormal, Torsion, The Osculating, The Normal and the Rectifying Planes, The Frenet-Serret Theorem, Spherical Images, Sphere Curves, Spherical Contacts, Fundamental Theorem of Space Curves, Line Integrals and Green's Theorem, Local Surface Theory, Coordinate Transformations, The Tangent and the Normal Planes, Parametric Curves, The First Fundamental Form and the Metric Tensor, Normal and Geodesic Curvatures, Gauss's Formulae, Christoffel Symbols of First and Second Kinds, Parallel Vector Fields Along a Curve and Parallelism, The Second Fundamental Form and the Weingarten Map, Principal, Gaussian, Mean and Normal Curvatures, Dupin Indicatrices, Conjugate and Asymptotic Directions, Isometries and the Fundamental Theorem of Surfaces

#### Texts and Reference Books

1. M. P. Do Carmo, *Differential Geometry of Curves and Surfaces*, Prentice Hall, 1976.
2. A. Goetz, *Introduction to Differential Geometry*, Addison Wesley, 1970.

3. R. S. Millman and G. D. Parker, *Elements of Differential Geometry*, Prentice Hall, 1977.
4. A. N. Pressley, *Elementary differential geometry*, 2<sup>nd</sup> Edition, Springer-Verlag, 2012.
5. D. J. Struik, *Lectures on Classical Differential Geometry*, Addison Wesley, Massachusetts, 1977.

**Course Code:** MAT-5104

**Title:** Analytical Mechanics

**Credit Hrs:** 03

**Course Outline:** Kinematics of Particles, Motion in Resisting Medium, Variable Mass Problem, Euler's Theorem and Chasles' theorem, **Moving Coordinate System:** Motion Relative to the Rotating Earth, **The Motion of a System of Particles:** Work, Power, Energy, center of mass, Generalized Coordinates, Lagrange's and Hamilton's Equations, Hamiltonian Principle, Simple Applications, Properties of a Rigid Body, Motion under No Forces, **Motion of Rigid Bodies in Three Dimensions:** General motion of rigid bodies in space. The momental ellipsoid and equimomental systems. Angular momentum vector and rotational kinetic energy. Principal axes and principal moments of inertia. Determination of 16 principal axes by diagonalizing the inertia matrix. **Euler Equations of Motion of a Rigid Body:** Force free motion. Free rotation of a rigid body with an axis of symmetry. Free rotation of a rigid body with three different principal moments. The Eulerian angles, angular velocity and kinetic energy in terms of Euler angles. Motion of a spinning top and gyroscopes-steady precession, sleeping top.

#### **Texts and Reference Books**

1. G. R Fowles, G.L. Cassiday, *Analytical Mechanics*, 7<sup>th</sup> Edition, Thomson Brook Cole, 2005.
2. B. Jafferson, T. Beadsdown, *Further Mechanics*, Oxford University Press, 2001.
3. Louis N. Hand, *Analytical Mechanics*, 1<sup>st</sup> Edition, Cambridge University Press, 1998.
4. Dr. C. Helrich, *Analytical Mechanics*, 1<sup>st</sup> Edition, Springer, 2016.
5. J. S. Torook, *Analytical Mechanics*, 1<sup>st</sup> Edition, Wiley-Interscience, 1999.

**Course Code:** MAT-5105

**Title:** Topology

**Credit Hrs:** 03

**Course Outline:** Overview of Metric Spaces, Convergence, and Continuity in Metric Spaces, Topological Spaces, Sub-Spaces, Closed Sets, Closures and Interiors of Sets, Boundary of a Set, Limit Point, Bases and Sub-bases, Neighborhood Base, First and Second Countable Spaces, Continuous Functions and Homeomorphism, Product Topology  $T_0$ ,  $T_1$ ,  $T_2$  Spaces and Their Characterizations and Basic Properties, Regular and Completely Regular Spaces, Normal and Completely Normal Spaces  
Compact / Countable Spaces and Their Properties, Connected Spaces

#### **Texts and Reference Books**

1. C. W. Patty, *Foundation of Topology*, 2<sup>nd</sup> Edition, The Jones and Bartlett Publishers, 2009.
2. J. Dugundji, *Topology*, W.M. C. Brown Publisher, 1990.
3. J. R. Munkres, *Topology: A First Course in Topology*, 2<sup>nd</sup> Edition, Prentice Hall Inc., New Jersey, 2005.
4. G. F. Simmons, *Introduction to Topology and Modern Analysis*, Tata Mc-Graw Hill, 1963.
5. Munkres, *Topology*, 2<sup>nd</sup> Edition, Pearson India, 2015.

**Course Code:** MAT-5106

**Title:** Abstract Algebra

**Credit Hrs:** 03

**Course Outline:** Sets and Structures, Basic Axioms and Order of a Group, Subgroups, Subgroups Generated by Subset of a Group, System of Generators, Cyclic Group, Cosets, Lagrange's Theorem, Permutations, Even and Odd Permutations, Cycles, Lengths of Cycles, Transpositions, Symmetric and Alternating Group, Normalizers and Centralizers of a Subset of a Group, Centre of a Group, Normal Subgroup, Quotient Groups, Conjugacy Relation between Elements and Subgroups, Homomorphism and Isomorphism between Groups, Homomorphism and Isomorphism Theorems,

#### **Texts and Reference Books**

1. J. B. Fraleigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. N. Jacobson, *Basic Algebra*, Vol. 1, W.H. Freeman and Company, 1985
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. D.S. Dummit and R. M. Foote, *Abstract Algebra*, 3rd Edition, Wiley, 2003.
5. J. A. Gallian, *Contemporary abstract algebra*, D.C. Heath, 1986.

## Semester-II

**Course Code:** MAT-5201

**Title:** Real Analysis-II

**Credit Hrs:** 03

**Course Outline:** **The Riemann-Stieltjes Integrals:** Definition and existence of integrals. Properties of integrals. Fundamental theorem of calculus and its applications. Change of variable theorem. Integration by parts. **Functions of Bounded Variation:** Definition and examples. Properties of functions of bounded variation. **Improper Integrals:** Types of improper integrals, tests for convergence of improper integrals. Beta and gamma functions. Absolute and conditional convergence of improper integrals. **Sequences and Series of Functions:** Power series, definition of point-wise and uniform convergence. Uniform convergence and continuity. Uniform convergence and differentiation. Examples of uniform convergence.

### Texts and Reference Books

1. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
2. W. Rudin, *Principles of Mathematical Analysis*, Mc-Graw Hill, New York, 1987.
3. T. M. Apostol, *Mathematical Analysis*, 6<sup>th</sup> Edition, Addison Wesley, 1982.
4. R. G. Bartle and D. R. Sherbert, *Introduction to Real Analysis*, 3<sup>rd</sup> Edition, John Wiley and Sons, 1999
5. S. Lang, *Real Analysis*, Springer-Verlag, London, 1987.

**Course Code:** MAT-5202

**Title:** Partial Differential Equations

**Credit Hrs:** 03

**Course Outline:** Review of ODEs in More than One Variable, **First order PDEs:** Introduction, formation of PDEs, solutions of PDEs of first order, The Cauchy's problem for quasilinear first order PDEs, First order nonlinear equations, Special types of first order equations, **Second order PDEs:** Basic concepts and definitions, Mathematical problems, Linear operators, Superposition, Mathematical models: The classical equations, the vibrating string, the vibrating membrane, conduction of heat solids, canonical forms and variable, PDEs of second order in two independent variables with constant and variable coefficients, Cauchy's problem for second order PDEs in two independent variables  
**Methods of separation of variables and Green's Functions:** Solutions of elliptic, parabolic and hyperbolic PDEs in Cartesian and cylindrical coordinates

### Texts and Reference Books

1. P. Duchaure and D. Zachmann, *Partial Differential Equations*, Mc-Graw Hill, 1986.
2. J. Fritz, *Partial Differential Equations*, Spriger-Verlag, New York, 1979.
3. R. Haberman, *Elementary Applied Partial Differential Equations*, Prentice Hall Inc., 1983.
4. M. Humi and W.B. Miller, *Boundary Value Problems and Partial Differential Equations*, PWS-Kent Publishing Company, Bostan, 1992.
5. J. Kevorkean, *Partial Differential Equations: Analytical Solution Techniques* (Texts in Applied Mathematics), 2<sup>nd</sup> Edition, 1839.

**Course Code:** MAT-5203

**Title:** Numerical Methods I

**Credit Hrs:** 03

**Course Outline:** Computer Arithmetic, Approximations and Errors; Methods for the Solution of Non-Linear Equations and Their Convergence: Bisection Method, Regula-Falsi, Fixed Point Iteration, Newton-Raphson, Secant and Householder's Method, Error Analysis for Iterative Methods Interpolation and Polynomial Approximation: Lagrange Interpolation, Newton's Divided Difference, Forward-Difference and Backward-Difference Formulae, Hermite Interpolation, Numerical Integration and Error Estimates: Rectangular Rule, Trapezoidal Rule, Simpson's One-Three and Three-Eight Rules  
Numerical Solution of Systems of Algebraic Linear Equations: Gauss-Elimination Method, Gauss-Jordan Method, Matrix Inversion, LU-Factorization, Doolittle's, Crout's, Cholesky's Methods, Gauss-Seidel and Jacobi Methods, Matrix Norms, Method of Least Squares, Eigenvalues and Eigenvectors: Power Method

### Texts and Reference Books

1. K.E. Atkinson, *An Introduction to Numerical Analysis*, 2<sup>nd</sup> Edition, John Wiley and Sons, New York, 1989.

2. R.L. Burden and J.D. Faires, *Numerical Analysis*, 5<sup>th</sup> Edition, PWS Publishing Company, 1993.
3. S.C. Chapra and R.P. Canale, *Numerical Methods for Engineers*, Mc-Graw Hill, New York, 1988.
4. A. Greenbaum and T. P. Chartier, *Numerical Methods*, 2012 Edition, Princeton University Press, 2012.
5. J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.

**Course Code:** MAT-5204

**Title:** Complex Analysis

**Credit Hrs:** 03

**Course Outline:** The Algebra and the Geometry of Complex Numbers, Complex Functions, Parametric Curves in the Complex Plane, Linear Mappings, Special Power Functions, Reciprocal Functions, Limit and Continuity, Complex Functions as Vector Fields, Derivative, Analytic Functions, Cauchy-Riemann Equations, Complex Exponential, Logarithmic, Trigonometric, Hyperbolic Functions and Their Derivatives, Harmonic Functions, Contour Integrals, the Cauchy-Goursat Theorem, Cauchy Integral Formulas, the Morera Theorem, Maximum Modulus Principle, The Liouville Theorem, Fundamental Theorem of Algebra, Convergence of Sequences and Series, The Taylor and the Laurent Series, Uniqueness of Representation, Zeros of Analytic Functions Residues, Poles and the Residue Theorem, Evaluation of Improper Integrals, Integrals Around a Branch Point, The Argument Principle and the Rouché's Theorem

#### Texts and Reference Books

1. R.V. Churchill and J.W. Brown, *Complex Variables and Applications*, 5<sup>th</sup> Edition, Mc-Graw Hill, New York, 1989.
2. E. Hille, *Analytic Function Theory*, Vol. I and II, Chelsea Publishing Company, New York, 1974.
3. J. E. Marsden, *Basic Complex Analysis*, W. H. Freeman and Company, 1982.
4. D. G. Zill, and P. D. Shanahan, *A First Course in Complex Analysis with Applications*, Jones and Bartlet Publishers, Sudbury, Massachusetts, 2008.
5. L. V. Ahlfors, *Complex Analysis*, 3<sup>rd</sup> Edition, McGraw Hill Education (India) Private Limited, 2013.

**Course Code:** MAT-5205

**Title:** Tensor Analysis

**Credit Hrs:** 02

**Course Outline** Introduction to general tensors, Summation Convention, Kronecker Delta, Levi-Civita Symbol, Vectors as Quantities Transforming Under Rotations with Notation, The Spherical-Polar and the Cylindrical-Coordinate Meshes, Alternating Symbol, Relation between Alternating Symbol and Kronecker Delta, Tensors of First, Second and Higher Orders, Algebra of Tensors, Contraction of Tensor, Quotient Theorem, Symmetric and Skew-Symmetric Tensors, Invariance Property, Isotropic Tensors, Differentiation of Tensors, Application of Tensors in Modeling Anisotropic Systems, Study of Physical Tensors, Diagonalization of Inertia Tensor as Aligning Coordinate Frame with Natural Symmetries of the System

#### Texts and Reference Books

1. D.E. Bourne and P.C. Kendall, *Vector Analysis and Cartesian Tensors*, 2<sup>nd</sup> Edition, T. Nelson, 1977.
2. G. E. Hay, *Vector and Tensor Analysis*, Dover Publications, Inc., New York, 1979.
3. G. D. Smith, *Vector Analysis*, Oxford University Press, Oxford, 1962.
4. I. S. Sokolnikoff, *Tensor Analysis: Theory and Application*, John Wiley and Sons, 1951.
5. M. R. Spiegel, *Vector Analysis*, Mc-Graw Hill, New York, 1974.

**Course Code:** MAT-5206

**Title:** Scientific Programming

**Credit Hrs:** 2+1

**Course Outline (MATLAB, Maple, Mathematica):** A list of contents is given below. However the instructor may add or remove some of the contents depending on the need of the students.

Curve sketching (only graphs of functions of one variable in Cartesian Coordinates) by using standard procedure, Intro to MATLAB (history, installation, interface, using product help, etc), MATLAB vs Maths syntax, sketching plane curves and surfaces in MATLAB, use of MATLAB in linear algebra, symbolic computations using MATLAB, creating script and function m-files, MATLAB codes for Bisection, Newton-Raphson, secant, Regula-Falsi, Jacobi, GS, Euler, and RK-4 methods. A brief introduction to Maple/Mathematica, comparison between similar features of MATLAB and Maple/Mathematica.

The following points are important for teaching this course:

4. The course should be taught in a computer lab setting
5. At the completion of this course, the students must be able to utilize the software to solve computationally difficult problems

6. The students should have a good command on at least two of the three programs mentioned above

**Texts and Reference Books**

1. D. M. Etter, D. Kuncicky and D. Hull, *Introduction to Matlab-6*, Prentice Hall, 2001.
2. F. Garvan, *The Maple Book*, Chapman and Hall/CRC, 2002.
3. S. Kaufmann, *Mathematica as a Tool: An Introduction with Practical Examples*, Springer-Verlag, 1994.
4. A. Gilat, *MATLAB: An Introduction with Applications*, 5<sup>th</sup> Edition, Wiley, 2014.
5. L. Nichal, *Maple*, 1<sup>st</sup> Edition, Nancy Paulsen Books, 2014.

**Semester-III**

**Course Code:** MAT-6301

**Title:** Measure Theory

**Credit Hrs:** 03

**Course Outline:** Definition and Examples of Algebra and  $\sigma$ -Algebra, Basic Properties of Measurable Spaces, Definition and Examples of Measure Spaces, Outer Measure, Lebesgue Measure, Measurable Sets, Complete Measure Spaces  
Measurable Functions: Some Equivalent Formulations of Measurable Functions, Examples of Measurable Functions, Various Characterizations of Measurable Functions, Properties that Hold Almost Everywhere  
Definition of Lebesgue Integral, Basic Properties of Lebesgue Integrals, Comparison between Riemann Integration and Lebesgue Integration,  $L_2$ -Spaces

**Texts and Reference Books**

1. D. L. Cohn, *Measure Theory*, Birkhauser, 1980.
2. P. R. Halmos, *Measure Theory*, D. Van Nostrand, 1950.
3. H. L. Royden, *Real Analysis*, Mc-Millan Publishing Company, Inc., New York, 1968.
4. T. Tao, *An Introduction to Measure Theory*, American Mathematical Society, 2011.
5. P. R. Halmos, *Measure Theory*, 2<sup>nd</sup> Edition, Springer, 1978.

**Course Code:** MAT-6302

**Title:** Mathematical Physics

**Credit Hrs:** 03

**Course Outline:** Definition and Properties of Laplace and Inverse Laplace Transforms, s-shifting property of LT, existence and uniqueness theorem, LT of derivatives and integrals and solution of ivps, unite step function and t-shifting property of LT, solution of circuit problems by using LT, Dirac Delta Function and its properties, LT of periodic functions, Convolution Theorem, Convolution of discontinuous functions, solution of integral equations by LT, differentiation and integration of LT, Laguerre's equation and polynomials, Applications of Laplace Transforms to systems of ODEs and PDEs, Fourier Series of  $2\pi$  and  $2L$  periodic functions, Convergence and sum of FS, even and odd functions and half-range expansions of FS, solution of odes and pdes by using FS, Fourier Integrals, Fourier Sine and Cosine integrals, Fourier sine and cosine transforms, Fourier sine and cosine transforms of derivatives, existence of FT, FT of derivatives, Convolution theorem, Discrete and Fast Fourier Transforms, solution of odes and pdes by using FT.

**Texts and Reference Books**

1. E. Kreyszig, *Advanced Engineering Mathematics*, 10<sup>th</sup> Edition, Wiley, 2011.
2. E. L. Butkov, *Mathematical Physics*, Addison Wesley, 1973.
3. R. P. Kanwal, *Linear Integral Equations*, Academic Press, 1971.
4. T. Myint-U and L. Denbnath, *Partial Differential Equations*, Elsevier Science Publishing, 1987.
5. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Vol. II, Mc-Millan Publishing Company, Inc., New York, 1968.



**Course Code:** MAT-6303

**Title:** Numerical Methods-II

**Credit Hrs:** 03

**Course Outline:** IVP for ODEs: Elementary theory of ivps, Introduction to Single-Step Numerical Methods for solution of ivps, Picard's method, Euler's Method, Second and higher order Taylor's methods, RK-methods (mid-point, modified Euler, Heun's, and RK-4 methods), Multi-Step methods for numerical solutions of odes (2-, 3-, 4-, and 5-step Adam-Bashforth and Adam-Moulton methods), Extension of Euler and RK-4 methods for numerical solutions of higher order odes and system of first order odes, stability, consistency, and convergence of SS and MS methods, stiff odes, region of absolute stability and A-Stability,

BVPs for odes: Discussion on Problem Behavior and Stability, Shooting method and finite difference methods for Linear and Nonlinear BVPs, Rayleigh-Ritz method for Linear and Non-Linear BVPs.

#### Texts and Reference Books

- 1 U. Ascher and L. Petzold, *Computer Methods for ODEs and DAEs*, SIAM, 1998.
- 2 R. L. Burden and J.D. Faires, *Numerical Analysis*, 5<sup>th</sup> Edition, PWS Publishing Company, 1993.
- 3 U. Ascher, R. Matteij and R. Russell, *Numerical Solution of BVPs for ODEs*, Prentice Hall, 1988.
- 4 J. Lambert, *Numerical Methods for Ordinary Differential Systems*, Wiley, 1991.
- 5 A. Greenbaum and T. P. Chartier, *Numerical Methods*, 2012 Edition, Princeton University Press, 2012.

**Course Code:** MAT-6304

**Title:** Functional Analysis

**Credit Hrs:** 03

**Course Outline:** Definition and Examples of Normed Spaces, Banach Spaces, Characterization of Banach Spaces, Bounded Linear Transformations, Bounded Linear Operators, Functional and Their Examples, Various Characterization of Bounded (Continuous) Linear Operator, The Space of All Bounded Linear Operators, The Open Mapping and Closed Graph Theorems, The Dual (Conjugate) Spaces, Reflexive Spaces, Hahn-Banach Theorem (Without Proof), Some Important Consequences of the Hahn- Banach Theorem. Inner Product Spaces, Hilbert Spaces, Orthonormal Bases, Convexity in Hilbert Spaces, Operators in Hilbert Spaces, Invariant Sub-Spaces, Decomposition of Hilbert Spaces, Finite Dimensional Spectral Theory and Spectral Mapping Theorem.

#### Texts and Reference Books

- 1 E. Kreyszig, *Introductory Fundamental Analysis with Applications*, John Wiley and Sons, 1978.
- 2 I. J. Maddox, *Elements of Functional Analysis*, Cambridge University Press, 1970.
- 3 W. Rudin, *Functional Analysis*, Mc-Graw Hill, 1983.
- 4 G. F. Simmon, *Introduction to Topology and Modern Analysis*, Mc-Graw Hill, New York, 1983.
- 5 J. Muscat, *Functional Analysis*, 2014 Edition, Springer, 2014.

**Course Code:** MAT-6305

**Title:** Fluid Mechanics-I

**Credit Hrs:** 03

**Course Outline:** Fields and Continuum Concepts, Lagrangian and Eulerian Specifications, Local, Convective and Total Rates of Change, Conservatoin of Mass, Equation of Continuity, Boundary Conditions, Nature of Force in a Fluid Field and Their Effects: Surface and Body Forces, Stress at a Point, Viscosity and Newton's Viscosity Law, Viscous and Inviscid Flows, Laminar and Turbulent Flows, Compressible and Incompressible Flows

Irrotational Fluid Motion: Velocity Potential from an Irrotational Velocity Field, Streamlines. Vortex Lines and Vortex Sheets, Kelvins Minimum Energy Theorem, Conservation of Linear Momentum, Bernoullis Theorem and Its Applications, Circulations, Rate of Change of Circulation (Kelvins Theorem), Axially Symmetric Motion, Stokes Stream Function

Two-Dimensional Motion: Stream Function, Complex Potential and Complex Velocity, Uniform Flows, Sources, Sinks and Vortex Flows, Flow in a Sector, Flow Around a Sharp Edge, Flow Due to a Doublet

#### Texts and Reference Books

- 1 I. G. Curie, *Fundamentals of Mechanics of Fluids*, 3<sup>rd</sup> Edition, CRC, 2002.
- 2 I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
- 3 R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
- 4 H. Schlichting, K. Gersten, E. Krause and H. Oertel, Jr, *Boundary-Layer Theory*, 8<sup>th</sup> Edition, Springer-Verlag, 2004.
- 5 Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

**Course Code:** MAT-6306

**Title:** Operation Research

**Credit Hrs:** 03

**Course Outline:** Introduction to Operation Research and Real Life Phases, Introduction to Linear Programming (LP) with Examples, Graphical Solutions to Mathematical Model with Special Cases, Simplex Algorithm and its Different Cases, Big M Method and Two Phase Method, Scheduling and Blending Problems, The Transportation Problems, The Transshipment Problems, The Assignment Problems, Integer Programming, Network Models, Inventory Models

**Texts and Reference Books**

1. Hillier and Lieberman, *Introduction to Operations Research*, 9<sup>th</sup> Edition, Mc-Graw Hill, 2010.
2. P. R. Murthy, *Operations Research*, New Age International (P) Limited Publishers, New Delhi, 2007.
3. Taha and Hamdy, *Operations Research*, 7<sup>th</sup> Edition, Mc-Millan Publishing Company, Inc., New York, 2003.
4. W. L. Winston, *Practical Management Science: Spreadsheet Modeling and Applications*.
5. F. S. Hillier and G. J. Liberman, *Operations Research*, 9<sup>th</sup> Edition, McGraw-Hill Science/Engineering/Math, 2009.

**Course Code:** MAT-6307

**Title:** Number Theory

**Credit Hrs:** 03

**Course Outline:** Divisibility, Euclidean Algorithm, GCD and LCM of two Integers, Properties of Prime Numbers, Fundamental Theorem of Arithmetic (UFT), Congruence Relation, Residue System, Euler's Phi-Function, Solution of System of Linear Congruence, Congruences of Higher Degree, Chinese Remainder Theorem, Fermat's Little Theorem, Wilson's Theorem and Applications, Primitive Roots and Indices, Integers Belonging to a Given Exponent (mod p), Primitive Roots of Prime and Composite Moduli, Indices

**Texts and Reference Books**

1. G. A. Jones and J. M. Jones, *Elementary Number Theory*, Springer-Varlog, London Limited, 1998.
2. M. B. Nathanson, *Methods in Number Theory*, Springer-Verlag, New York, 2000.
3. A. N. Parshin and I.R. Shafarevich, *Number Theory-I, Fundamental Problems, Ideas and Theories*, Springer-Verlag, Berlin Heidelberg, 1995.
4. K. H. E. Rosen, *Elementary Number theory and its Applications*, 4<sup>th</sup> Edition, Addison Wesley, Reading, Ma, USA, 2000.
5. T. Andreescu and D. Andrica, *Number theory*, 2009 Edition, Birkhauser, 2009.

**Course Code:** MAT-6308

**Title:** Mathematical Statistics

**Credit Hrs:** 03

**Course Outline:** Set and Algebra of sets, Some elementary theorems of probability, Addition and multiplication rules, Baye's rule and Baye's theorem, Random variables, probability functions, Cumulative distribution Function, Discrete and Continuous probability distribution, Moments and moment generating functions, Moments of binomial, hypergeometric, Poisson, gamma, beta and normal distributions and their characterizations. Joint probability functions and their properties, Bivariate Normal distribution, Transformation; Distribution function technique, Transformation technique: One variable, several variables, Moment-generating function technique, Sampling distributions and their properties, Regression and Correlation, Linear regression, The methods of least squares, Normal regression analysis, Normal correlation analysis, Multiple linear regression, Multiple linear regression (matrix notation)

**Texts and Reference Books**

1. M. H. De-Groot and M. J. Schervish, *Probability and Statistics*, 3<sup>rd</sup> Edition, Addison Wesley, 2002.
2. A. Papoulis, *Probability, Random Variables, and Stochastic Processes*, 3<sup>rd</sup> Edition, Mc-Graw Hill, 1991.
3. T. Sincich, *Statistics by Examples*, Dellen Publishing Company, 1990.
4. A. S. Hirahi, *A Course in Mathematical Statistics*, 4<sup>th</sup> Edition, Ilmi Kitab Khana, Lahore, Pakistan, 2012.
5. I. Miller and M. Miller, *Mathematical Statistics with Applications*, 8<sup>th</sup> Edition, Pearson, 2012.

**Course Code:** MAT-6309

**Title:** Quantum Mechanics-I

**Credit Hrs:** 03

**Course Outline:** Black Body Radiation, Photoelectric Effect, Compton Effect, Bohr's Theory of Atomic Structure, Wave-Particle Duality, The De Broglie Postulate, Heisenberg Uncertainty Principle, The Postulates of Quantum Mechanics, Operators, Eigen-functions and Eigenvalues: Observables and Operators. Measurement in Quantum Mechanics, The State Function and Expectation Values Time, Development of the Stat Function (Schrodinger Wave Equation), Solution to the Initial-Value Problem in Quantum Mechanics, Parity Operators  
Function Spaces and Hermitian Operators: Particle in a Box, Dirac Notation, Hilbert Space. Hermitian Operators, Properties of Hermitian Operators, Additional One-Dimensional Problems: Bound and Unbound States: General Properties of the One Dimensional Schrodinger Equation, Unbound States, One-Dimensional Barrier Problems, The Rectangular Barrier, Tunneling

#### Texts and Reference Books

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2004.
2. H. D. Dehmen, *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics: A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Co., 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

**Course Code:** MAT-6310

**Title:** Ring Theory

**Credit Hrs:** 03

#### Course Outline:

**Rings:** Definition, examples. Quadratic integer rings. Examples of non-commutative rings. The Hamilton quaternions. Polynomial rings. Matrix rings. Units, zero-divisors, nilpotents, idempotents. Subrings, Ideals. Maximal and prime Ideals. Left, right and two-sided ideals;

Operations with ideals. The ideal generated by a set. Quotient rings. Ring homomorphism. The isomorphism theorems, applications. Finitely generated ideals. Rings of fractions.

**Integral Domain:** The Chinese remainder theorem. Divisibility in integral domains, greatest common divisor, least common multiple. Euclidean domains. The Euclidean algorithm. Principal ideal domains. Prime and irreducible elements in an integral domain. Gauss lemma, irreducibility criteria for polynomials. Unique factorization domains. Finite fields. Polynomials in several variables. Symmetric polynomials. The fundamental theorem of symmetric polynomials.

#### Texts and Reference Books

1. J. B. Fraieigh, *A First Course in Abstract Algebra*, Addison Wesley, 2002.
2. B. Hartley and T. O. Hawkes, *Ring, Modules and Linear Algebra*, Chapman and Hall, 1980.
3. S. Lang, *Algebra*, Springer-Verlag, 2002.
4. S. J. Leon, *Linear Algebra with Applications*, 6<sup>th</sup> Edition, Prentice Hall, 2002.
5. P. M. Cohn, *Introduction to Ring Theory*, 1<sup>st</sup> Edition, Springer, 2002.

**Course Code:** MAT-6311

**Title:** Analytical Dynamics

**Credit Hrs:** 03

**Course Outline:** Constraints, Generalized Coordinates, Generalized Forces, General Equation of Dynamics, Lagrange's Equations, Conservation Laws, Ignorable Coordinates, Explicit Form of Lagrange's Equation in Terms of Tensors. Hamilton' Principle of Least Action, Hamilton's Equations of Motion, Hamilton-Jacobi Method, Poisson Brackets (P.B's); Poisson's Theorem; Solution of Mechanical Problems by Algebraic Technique Based on (P.B's) Small Oscillations and Normal Modes, Vibrations of Strings, Transverse Vibrations Normal Modes, Forced Vibrations and Damping, Reflection and Transmission at a Discontinuity, Longitudinal Vibrations, Rayleigh's Principle

#### Texts and Reference Books

1. F. Chorlton, *Textbook of Dynamics*, Van Nostrand, 1963.
2. W. Chester, *Mechanics*, George Allen and Unwin Ltd. London, 1979.
3. H. Goldstein, *Classical Mechanics*, Cambridge University Press, 1980.
4. G. Meirovitch, *Methods of Analytical Dynamics*, Mc-Graw Hill, 1970.
5. H. Baruh, *Analytical Dynamics*, 1<sup>st</sup> Edition, WCB/McGraw-Hill, 1998.

**Course Code:** MAT-6312

**Title:** Approximation Theory

**Credit Hrs:** 03

**Course Outline:** Best Approximations in Normal Spaces, Existence Theorem, Approximation by Algebraic Polynomials, Uniqueness, Strict Convexity, Lemma Convexity, Uniqueness Theorem, Hilbert Space, Uniform Approximation, External Point, Haar Condition, Extreme Points, Best Approximation, Characterization of Best Approximation, A Brief Introduction to Interpolation, Chebyshev Polynomials, Chebyshev Theorem, Least Squares Approximation, Gram-Schmidt Orthonormalization Process, Orthogonal Function, Pade Approximation, Remex Algorithm

**Texts and Reference Books**

1. N. I. Achieser, *Theory of approximation*, Dover Publications, Inc., New York, 2004.
2. J. R. Rice, *The Approximation of Functions*, Vol. I, Addison Wesley Publishing Company, 1964.
3. T. J. Rivlin, *An Introduction to the Approximation of Functions*, Dover Publications, Inc., New York, 1981.
4. M. J. D. Powell, *Approximation Theory and Methods*, Cambridge University Press, 1988.
5. E. W. Cheney, *Introduction to Approximation Theory*, AMS, 2000.

**Course Code:** MAT-6313

**Title:** Differential Geometry-II

**Credit Hrs:** 03

**Course Outline:** Definition and Examples of Manifolds, Differential Maps, Sub-Manifolds, Tangents, Coordinate Vector Fields, Tangent Spaces, Dual Spaces, Multi-Linear Functions, Algebra of Tensors, Vector Fields, Tensor Fields, Integral Curves, Flows, Lie Derivatives, Brackets, Differential Forms, Introduction to Integration Theory on Manifolds, Riemannian and Semi-Riemannian Metrics, Flat Spaces, Affine Connections, Parallel Translations, Covariant Differentiation of Tensor Fields, Curvature and Torsion Tensors, Connection of a Semi-Riemannian Tensor, Killing Equations and Killing Vector Fields, Geodesics, Sectional Curvature

**Texts and Reference Books**

1. R. Abraham, J. E. Marsden and T. Ratiu, *Manifolds, Tensor Analysis and Applications*, Addison Wesley, 1983.
2. R. L. Bishop and S. I. Goldberg, *Tensor Analysis on Manifolds*, Dover Publications, Inc., New York, 1980.
3. M. P. Do Carmo, *Riemannian Geometry*, Birkhauser, 1992.
4. D. Langwitz, *Differential and Riemannian Geometry*, Academic Press, 1970.
5. D. Lovelock and H. Rund, *Differential Forms and Variational Principles*, John Wiley and Sons, 1975.

**Course Code:** MAT-6314

**Title:** Electromagnetic Theory-I

**Credit Hrs:** 03

**Course Outline:** Electromagnetic Fields, Coulomb's Law, The Electric Field Intensity and Potential, Gauss's Law and Deductions, Poisson and Laplace Equations, Conductors and Condensers, Dipoles, The Linear Quadrupole, Potential Energy of a Charge Distribution, Dielectrics, The Polarization and Displacement Vectors, General Solutions of Laplace's Equation. Solutions of Laplace's Equation in Spherical Coordinates, Legendre's Equation, Legendre's Polynomials, Electromagnetic Fields, The Magnetostatic Law of Force, The Magnetic Induction, The Lorentz Force on a Point Charge Moving in a Magnetic Field, The Divergence of the Magnetic Field, The Vector Potential, The Conservation of Charge and Equation of Continuity, The Lorentz Condition, The Curl of The Magnetic Field, Ampere's Law and the scalar Potential, Steady and Slowly Varying Currents, Electric Current, Linear Conductors. Conductivity, Resistance, Kirchhoff's Laws, Current Density Vector, Magnetic Field of Straight and Circular Current, Magnetic Flux, Vector Potential, Forces on a Circuit in Magnetic Field

**Texts and Reference Books**

1. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
2. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
3. G. E. Owen, *Introduction to Electromagnetic Theory*, Dover, 2003.
4. J. R. Reitz, F. J. Milford and R. W. Christy, *Foundations, of Electromagnetic Theory*, Addison-Wesley Publishing Co., 1993.
5. J. V. Stewart, *Intermediate Electromagnetic Theory*, World Scientific, 2001.

**Course Code:** MAT-6315

**Title:** Conference/Seminar/Reading-I

**Credit Hrs:** S/U

**Course Outline:** The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also be trained on preparing papers and presentations for conferences and seminars.

#### **Texts and Reference Books**

As per requirement of the students taking the course

### **Semester-IV**

**Course Code:** MAT-6401

**Title:** Mathematical Systems Theory

**Credit Hrs:** 03

**Course Outline:** Conservation laws and phenomenological principles, some principles and laws of thermodynamics, mechanics, and electromagnetism and their applications in modelling, Linearization, matrix exponentials and solution of linear differential equations, LTV systems, Impulse and step responses, Stability, controllability, and observability of LTI systems, Realization theory and Hankel matrices, Feedback and stabilizability, observers and state reconstruction, detectability, separation principle and compensation, disturbance rejection, Laplace transforms and LTI systems, transfer functions and transfer matrices, transfer functions and minimal realizations of SISO and MIMO systems, Abstract systems description and behavioral modeling, polynomial representations of systems, brief discussion of nonlinear, descriptor, stochastic, distributed parameter, and discrete event systems, optimal control theory, parameter estimation, filter theory, model reduction, and adaptive and robust control

#### **Texts and Reference Books**

1. G. J. Olsder, J. W. van der Woude, J. G. Mask, and D. Jeltsema, *Mathematical Systems Theory*, 4<sup>th</sup> Edition, VSSD, 2011.
2. I. D. Hinrichsen and A. J. Pritchard, *Mathematical Systems Theory*, Springer, 2012.
3. J. W. Polderman and J. C. Willems, *Introduction to Mathematical Systems Theory*, 2<sup>nd</sup> Edition, Springer, 2008.
4. J. Zabczyk, *Mathematical Control Theory*, 1<sup>st</sup> Edition, Birkhauser, 2007.
5. E. D. Sontag, *Mathematical Control Theory*, 2<sup>nd</sup> Edition, Springer, 1998.

**Course Code:** MAT-6402

**Title:** Mathematical Modeling

**Credit Hrs:** 03

**Course Outline:** Introduction to modeling, Basic Guide line of mathematical modeling, Collection and interpretation of data, Technique of mathematical modeling, Classification of mathematical modeling, modeling through algebra, modeling through Geometry, modeling through Trigonometry, modeling through Calculus, Limitation of modeling, Development of Models', , Discrete and Continuous models,, Linear Growth and Decay Model, Non-linear Growth and decay models, Mathematical modeling in population dynamic, Traffic flow models.

#### **Texts and Reference Books**

1. Banerjee, *Mathematical modeling* (Modell analysis and Application)
2. J. J. Batzel, M. Bachar, and F. Kappel, *Mathematical Modeling and Validation in Physiology*, 2013
3. D. Edwards and M. Hamson, *Mathematical modeling Skills*, MacMillan Press Ltd., 1996
4. F. R. Giordano, M. D. Weir, and W. P. Fox, *A First Course in Mathematical modeling*, Thomson Brooks/Cole, 2003
5. J. N. Kapur, *Mathematical modeling*, New Age International Limited, 2015.

**Course Code:** MAT-6403

**Title:** Integral Equations

**Credit Hrs:** 03

**Course Outline:** Linear integral equations of the first and second kind. Relationship between differential equation and Volterra integral equation. Neumann series. Fredholm Integral equation of the second kind with separable Kernels. Eigenvalues and eigenvectors. Iterated functions. Quadrature methods. Least square methods. Homogeneous integral equations of the second kind. Fredholm integral equations of the first kind. Fredholm integral equations of the second kind. Abel's integral equations. Hilbert Schmidt theory of integral equations with symmetric Kernels. Regularization and filtering techniques, Introduction to Wiener-Hopf Technique.

#### Texts and Reference Books

1. J. J. Abdul, *Introduction to Integral Equations with Applications*, Marcel Dekker Inc. New York, 1985.
2. V. Lovitt, *Linear Integral Equations*, Dover Publications, Inc., New York, 1950.
3. B. Noble, *Methods Based on the Wiener-Hopf Technique*, Pergamon Press, 1988
4. F. Smith, *Integral Equations*, Cambridge University Press, 2003.
5. F. G. Tricomi, *Integral Equations*, Interscience, 1957.

**Course Code:** MAT-6404

**Title:** Special Functions

**Credit Hrs:** 03

**Course Outline:** Infinite Products: introduction, Definition of an infinite product, A necessary condition for convergence, Associated series of logarithms, Convergences types, The Gamma and Beta Functions: The Euler constant, The Gamma function, A series for logarithmic differential of Gamma function, The order symbols  $o$  and  $O$ , Evaluation of certain infinite products, The Beta Function, Factorial function, Asymptotic Series: Definition of an asymptotic expansion, Algebraic properties, Term by term integration, Uniqueness, The Hypergeometric function : Simple integral form, The function  $F(a,b;c,z)$  and its properties, The Hypergeometric differential equation, Logarithmic solution of the hypergeometric function,  $F(a,b;c,z)$  as a function of parameters, Elementary series manipulation, Kummer Theorem, Generalized Hypergeometric functions, the exponential and binomial functions, A differential equation, Saalschutz theorem, Contour integral integrals of Barnes' type, the Barnes integrals and the generalized hypergeometric function, Bessel Functions and its properties, The Confluent Hypergeometric functions and its properties, Generating Functions.

#### Texts and Reference Books

1. E. D. Rainville, *Special Functions*, 1st Edition, The Macmillan Company New York, 1965.
2. L. J. Slater, and D. Lit, *Confluent Hypergeometric Functions*, Cambridge University Press, London, 1960.
3. A. Erdelyi, *Higher Transcendental Functions*, Volume I, II, & III, McGraw Hill Book Company, Inc. 1953.
4. J. E. Andrews, R. Asky and R. Roy, *Special Functions*, 1<sup>st</sup> Edition, Cambridge University Press, 2001.
5. C. Viola, *Special Functions*, 1<sup>st</sup> Edition, Springer, 2016.

**Course Code:** MAT-6405

**Title:** Fluid Mechanics-II

**Credit Hrs:** 03

**Course Outline:** Circular Cylinder without Circulation, Circular Cylinder with Circulation Blasius Theorem, Kutta Condition and the Flat-Plate Airfoil, Joukowski Airfoil, Vortex Motion, Karman's Vortex Street, Method of Images, Velocity Potential, Stoke's Stream Function, Solution of the Potential Equation, Uniform Flow Source and Sink, Flow Due to A Doublet

Viscous Flows Of Incompressible Fluids: Constitutive Equations, Navier-Stokes's Equations, Exact Solutions of Navier-Stokes's Equations, Steady Unidirectional Flow, Poiseuille Flow, Coquette Flow, Flow between Rotating Cylinders, Stoke's First Problem, Stoke's Second Problem

Simplified Approach to Fluid Flow Problems: Similarity from Differential Equations, Dimensional Analysis, One Dimensional Steady Compressible Flow

#### Texts and Reference Books

1. I. G. Curie, *Fundamentals of Mechanics of Fluids*, 3<sup>rd</sup> Edition, CRC, 2002.
2. I. L. Distworth, *Fluid Mechanics*, Mc-Graw Hill, 1972.
3. R.W. Fox, A.T. Mc-Donald and P.J. Pritchard, *Introduction to Fluid Mechanics*, John Wiley and Sons, 2003.
4. H. Schlichting, K. Gersten, E. Krause and H. Oertel, Jr, *Boundary-Layer Theory*, 8<sup>th</sup> Edition, Springer-Verlag, 2004.
5. Y. C-Shun, *Fluid Mechanics*, Mc-Graw Hill, 1974.

**Course Code:** MAT-6406

**Title:** Algebraic Topology

**Credit Hrs:** 03

**Course Outline:** Path Wise Connectedness with Examples, Notion of Homotopy, Homotopy Classes and its Application, Path Homotopy, Path Homotopy Classes, Fundamental Groups, Covering Mapping with Examples, Covering Spaces, Lifting Properties of Covering Spaces and its Application, Fundamental Group of a Circle (s)

**Texts and Reference Books**

1. M. J. Greeberge, *Algebraic Topology, A first Course*, Benjamin Commings, 1967.
2. C.A. Kosniowski, *First course in Algebraic Topology*, Cambridge University press, 1980.
3. A. H. Wallace, *Algebraic Topology, Homology and Cohomology*, Benjamin, 1968.
4. A. Hatcher, *Algebraic Topology*, 1<sup>st</sup> Edition, Cambridge University Press, 2001.
5. W. Fulton, *Algebraic Topology*, Springer, 1997.

**Course Code:** MAT-6407

**Title:** Comprehensive Oral Exam

**Credit Hrs:** 01

**Course Outline:**

There will be a comprehensive oral exam at the end of the 4<sup>th</sup> semester. This examination will be conducted by an external examiner and 2 internal examiners together. Questions may be asked from any course which the student has studied during M.Sc.

**Course Code:** MAT-6408

**Title:** Project

**Credit Hrs:** 03

**Course Outline:**

The objective of this course is to train students to learn and use the tools required for writing their project report and the tools for doing their research work. They will do the literature survey, work on some research problem and write a project report by the end of the course.

**Texts and Reference Books**

As per requirements of the topic of the FYP.

**Course Code:** MAT-6409

**Title:** Quantum Mechanics-II

**Credit Hrs:** 03

**Course Outline:** Harmonic Oscillator and Problems in Three-Dimensions: The Harmonic Oscillator, Eigen-Functions of the Harmonic Oscillator, The Harmonic Oscillator in Momentum Space, Motion in Three Dimensions, Spherical Symmetric Potential and the Hydrogen Atom, Angular Momentum: Basic Properties, Eigenvalues of the Angular Momentum Operators, Eigen-Functions of the Orbital Angular Momentum Operators  $L_2$  and  $L_z$ , Commutation Relations between Components of Angular Momentum and Their Representation in Spherical Polar Coordinates, The Scattering Cross-Section, Scattering Amplitude, Scattering Equation, Born Approximation, Partial Wave Analysis, Time Independent Perturbation of Non-Degenerate and Degenerate Cases, Time-Dependent Perturbations

**Texts and Reference Books**

1. D. R. Bes, *Quantum Mechanics: A Modern a Concise Introductory Course*, Springer-Verlag, 2004.
2. H. D. Dehmen, *The Picture Book of Quantum Mechanics*, Springer-Verlag, 2001.
3. H. F. Hameks, *Quantum Mechanics, A Conceptual Approach*, Wiley- IEEE, 2004.
4. R. L. Liboff, *Introduction Quantum Mechanics*, Addison Wesley Publishing Company, 2003.
5. V. K. Thankappan, *Quantum Mechanics*, New Age Publishers, 1993.

**Course Code:** MAT-6410

**Title:** Introduction to Combinatorics

**Credit Hrs:** 03

**Course Outline:** Two Basic Counting Principle, Permutations, Combinations, The Injective and Bijective Principles, Arrangements and Selections with Repetitions, Graphs in Combinatorics, The Binomial Theorem, Combinatorial Identities, Properties of Binomial Coefficients, Multinomial Coefficients, The Multinomial Theorem, The Pigeonhole Principle, Examples, Ramsey Numbers, The Principle of Inclusion and Exclusion, Generalization, Integer Solutions, Surjective Mapping. Stirling Numbers of the Second Kind, The Sieve - Eratosthenes, Euler  $\Phi$ -Function, The Problem Des-Menages Ordinary Generating Functions, Modeling Problems, Partition of Integers, Exponential Generating Functions Linear Homogeneous Recurrence Relations, Algebraic Solutions of Linear Recurrence Relations and Constant Functions, The Method of Generating Functions, A Non-Linear Recurrence Relation and Catalan Numbers

#### Texts and Reference Books

1. V. K. Balakrishnan, *Theory and Problems of Combinatorics*, Schaum's Outline Series, Mc-Graw Hill, Singapore, 1995.
2. C. C. Chen and K. M. Koh, *Principles and Techniques in Combinatorics*, World Scientific Publishing Company, Pvt. Ltd, Singapore, 1992.
3. C. L. Liu, *Introduction to Combinatorial Mathematics*, Mc-Graw Hill, New York, 1968.
4. A. Tucker, *Applied Combinatorics*, John Wiley and Sons, New York, 1985.
5. R. A. Brualdi, *Introductory Combinatorics*, 5<sup>th</sup> Edition, Pearson, 2009.

**Course Code:** MAT-6411

**Title:** Theory of Elasticity

**Credit Hrs:** 03

**Course Outline:** Cartesian Tensors, Analysis of Stress and Strain, Generalized Hooke's Law, Crystalline Structure, Point Groups of Crystals, Reduction in the Number of Elastic Moduli Due to Crystal Symmetry, Equations of Equilibrium, Boundary Conditions, Compatibility Equation, Plane Stress and Plane Strain Problems, Two Dimensional Problem in Rectangular and Polar Coordinates, Torsion of Rods and Beams

#### Texts and Reference Books

1. E. Dieulesaint and D. Royer, *Elastic Waves in Solids*, John Wiley and Sons, New York, 1980.
2. Y. C. Funk, *Foundations of Solid Mechanics*, Prentice-Hall, Englewood Cliffs, 1965.
3. Sokolnikoff, *Mathematical Theory of Elasticity*, Mc-Graw Hill, New York.
4. S. P. Timoshenko and J. N. Goodier, *Theory of Elasticity*, 3<sup>rd</sup> Edition, McGraw Hill Education (India) Private Limited, 2015.
5. A. I. Lurie and A. Belyaev, *Theory of Elasticity*, 2005 Edition, Springer, 2005.

**Course Code:** MAT-6412

**Title:** Optimization Theory

**Credit Hrs:** 03

**Course Outline:** Introduction to optimisation. Relative and absolute extrema. Convex, concave and unimodal functions. Constraints. Mathematical programming problems. Optimisation of one, two and several variables functions and necessary and sufficient conditions for their optima. **Optimisation by equality constraints:** Direct substitution method and Lagrange multiplier method, necessary and sufficient conditions for an equality constrained optimum with bounded independent variables. Inequality constraints and Lagrange multipliers. Kuhn-Tucker Theorem. Multidimensional optimisation by Gradient method. Convex and concave programming. Calculus of variation and Euler Lagrange equations. Functionals depending on several independent variables. Variational problems in parametric form. Generalised mathematical formulation of dynamics programming. Non-linear continuous models. Dynamics programming and variational calculus. Control theory.

#### Texts and Reference Books

1. L. Elsgolts, *DEs and the Calculus of Variations*, Mir Publishers Moscow, 1970.
2. B. S. Gotfried and J. Weisman, *Introduction to Optimization Theory*, Prentice Hall, NJ, USA, 1973.
3. D. G. Luenberger, *Introduction to Linear and Non-Linear Programming*, Addison Wesley, USA, 1973.
4. D. A. Wismer and R. Chattergy, *Introduction to Nonlinear Optimization*, North Holland, New York, 1978.
5. A. Beck, *Introduction to Nonlinear Optimization: Theory, Algorithms, and Applications with MATLAB*, SIAM-Society for Industrial and Applied Mathematics, 2014.



**Course Code:** MAT-6413

**Title:** Special Theory of Relativity

**Credit Hrs:** 03

**Course Outline:** Historical Background and Fundamental Concepts of Special Theory of Relativity, Lorentz Transformations (for Motion Along One Axis), Length Contraction, Time Dilation and Simultaneity, Velocity Addition Formulae, 3-Dimensional Lorentz Transformation, Introduction to 4-Vector Formalism, Lorentz Transformations in the 4-Vector Formalism, The Lorentz and Poincare Groups, Introduction to Classical Mechanics, Minkowski Space-Time and Null Cone, 4-Velocity, 4-Momentum and 4-Force, Application of Special Relativity to Doppler Shift and Compton Effect, Particle Scattering, Binding Energy, Particle Production and Decay, Electromagnetism in Relativity, Electric Current, Maxwell's Equations and Electromagnetic Waves, The 4-Vector Formulation of Maxwell's Equations, Special Relativity with Small Acceleration

**Texts and Reference Books**

1. H. Goldstein, *Classical Mechanics*, Addison Wesley, New York, 1962.
2. D. Inverno, *Introducing Einstein's Relativity*, Oxford University Press, 1992.
3. J. D. Jackson, *Classical Electrodynamics*, John Wiley and Sons, New York, 1962.
4. A. Qadir, *Relativity: An Introduction to the Special Theory*, World Scientific, 1989.
5. W. Rindler, *Essential Relativity*, Springer-Verlag, 1977.

**Course Code:** MAT-6414

**Title:** Electromagnetic Theory-II

**Credit Hrs:** 03

**Course Outline:** The Faraday Induction Law, Induced Electromotance in a Moving System, Inductance and Induced Electromotance, Energy Stored in a Magnetic Field, The Equations of Electromagnetism, Electromagnetic Waves: Plane Electromagnetic Waves in Free Space and Isotropic Media, The Poynting Vector in Free Space, Propagation of Electromagnetic Waves in NON-Conductors, Propagation of Plane Waves in Conducting Media, Reflection and Refraction of Plane Waves, Guided Waves, Coaxial Line, Hollow Rectangular Wave Guide, Radiation of Electromagnetic Waves, Electromagnetic Field of a Moving Charge

**Texts and Reference Books**

1. D. J. Griffiths, *Introduction to Electrodynamics*, Prentice-Hall, 1999.
2. J. D. Jackson, *Classical Electrodynamics*, Wiley, 1999
3. G. E. Owen, *Introduction to Electromagnetic Theory*, Dover, 2003.
4. J. R. Reitz, F. J. Milford and R. W. Christy, *Foundations of Electromagnetic Theory*, Addison-Wesley Publishing Co., 1993.
5. J. V. Stewart, *Intermediate Electromagnetic Theory*, World Scientific, 2001.

**Course Code:** MAT-6415

**Title:** Conference/Seminar/Reading-I

**Credit Hrs:** S/U

**Course Outline:** The purpose of this activity is to introduce students with the importance of conferences, seminars, and reading in scientific and academic development. Through various activities, students will be encouraged and trained to develop reading habits, especially of reference books and scientific articles. They will also be trained on preparing papers and presentations for conferences and seminars.

**Texts and Reference Books**

As per requirement of the students taking the course.

**Course Code:** MAT-6416    **Title:** Measure Theory and Lebesgue Integration    **Credit Hrs:** 03

**Course Outline:** Measure Spaces: Definition and examples of algebras and  $\sigma$ -algebras, Basic properties of measurable spaces, Definition and examples of measure spaces, Outer measure, Lebesgue measure, Measurable sets, Complete measure spaces.

Measurable Functions: Some equivalent formulations of measurable functions, Examples of measurable functions, Various characterization of measurable functions, Property that holds almost everywhere, Egorov's theorem.

Lebesgue Integrations: Definition of Lebesgue integral, basic properties of Lebesgue integrals, Comparison between Riemann integration and Lebesgue integration,  $L^2$ -space, The Riesz-Fischer theorem.

#### **Texts and Reference Books**

1. H. L. Royden, *Real Analysis*, Macmillan, 1968.
2. D. L. Cohn, *Measure Theory*, Birkhauser, 1980.
3. P. R. Halmos, *Measure Theory*, D. Van Nostrand, 1950.
4. T. Tao, *An Introduction to Measure Theory*, American Mathematical Society, 2011.
5. P. R. Halmos, *Measure Theory*, 2<sup>nd</sup> Edition, Springer, 1978.

### 3. Scheme of Studies for M.Phil in Mathematics: General Breakup

#### 3.1 General Requirement for M.Phil. Program

|                               |  |
|-------------------------------|--|
| Entrance                      | As per HEC and University Policy                   |
| Duration                      | 4 (min)-8 (max) semesters                          |
| Courses                       | 24 credits   |
| Thesis (MAT-7302)             | 06 credits   |
| Conference/Seminar (MAT-7301) | 01 credits *Should be offered/registered in Sem IV |
| Total                         | 31 credits   |

#### List of Courses for M.Phil Program

| Code     | Cour8se Title                                       | Credit Hours |
|----------|---|--------------|
| MAT-7101 | Advanced Functional Analysis                        | 03           |
| MAT-7102 | Advanced Topology                                   | 03           |
| MAT-7103 | Advanced Optimization Theory                        | 03           |
| MAT-7104 | Variational Inequalities                            | 03           |
| MAT-7105 | Advanced Partial Differential Equations             | 03           |
| MAT-7106 | Nonlinear Systems and Control                       | 03           |
| MAT-7107 | Advanced Complex Analysis                           | 03           |
| MAT-7108 | Sampling Techniques-I                               | 03           |
| MAT-7109 | Multivariate Analysis                               | 03           |
| MAT-7110 | Advanced Mathematical Statistics                    | 03           |
| MAT-7111 | Advanced Probability Theory                         | 03           |
| MAT-7112 | Introduction to Finite Element Methods              | 03           |
| MAT-7113 | Mathematical Techniques for Boundary Value Problems | 03           |
| MAT-7114 | Convex Analysis                                     | 03           |
| MAT-7115 | Semigroups in Geometric Functions Theory            | 03           |
| MAT-7116 | Conformal Mappings                                  | 03           |
| MAT-7117 | Stochastic Processes                                | 03           |
| MAT-7118 | Basics of the Theory of Fluids                      | 03           |
| MAT-7119 | Finite Mixture Distributions-I                      | 03           |
| MAT-7120 | Approximation Theory                                | 03           |
| MAT-7121 | Perturbation Methods-I                              | 03           |
| MAT-7122 | Lie Algebra   | 03           |
| MAT-7123 | Topological Groups                                  | 03           |
| MAT-7124 | Topological Vector Spaces                           | 03           |
| MAT-7125 | Electrodynamics-I                                   | 03           |
| MAT-7126 | Theory of Group Graphs                              | 03           |
| MAT-7127 | Theory of Group Actions                             | 03           |
| MAT-7128 | Magnetohydrodynamics-I                              | 03           |
| MAT-7129 | Advanced Measure Theory                             | 03           |
| MAT-7130 | Theory of Complex Manifolds                         | 03           |
| MAT-7131 | Complex Analysis of Several Variables               | 03           |
| MAT-7132 | Advanced Analytical Dynamics                        | 03           |
| MAT-7133 | General Relativity                                  | 03           |
| MAT-7134 | Astrophysics  | 03           |
| MAT-7135 | The Classical Theory of Fields                      | 03           |

|          |  |    |    |
|----------|--|----|----|
| MAT-7136 | Graph Theory                                       | 03 |    |
| MAT-7137 | Introduction to Robotics                           | 03 |    |
| MAT-7138 | Advanced Abstract Algebra                          | 03 |    |
| MAT-7201 | Geometric Functions Theory                         | 03 |    |
| MAT-7202 | Selected Topics in Pure Mathematics                | 03 |    |
| MAT-7203 | Advanced Mathematical Modeling                     | 03 |    |
| MAT-7204 | Parameter Estimation and Sensitivity Analysis      | 03 |    |
| MAT-7205 | Numerical Solutions of PDEs                        | 03 |    |
| MAT-7206 | Optimal Control                                    | 03 |    |
| MAT-7207 | Design Methods for Control Systems                 | 03 |    |
| MAT-7208 | Sampling Techniques II                             | 03 |    |
| MAT-7209 | Estimation Theory                                  | 03 |    |
| MAT-7210 | Differential Subordination Theory and Applications | 03 |    |
| MAT-7211 | Advanced Integral Equations                        | 03 |    |
| MAT-7212 | Non-Newtonian Fluid Mechanics                      | 03 |    |
| MAT-7213 | Group Methods for Differential Equations           | 03 |    |
| MAT-7214 | Stochastic Differential Equations                  | 03 |    |
| MAT-7215 | Fixed Point Theory and Applications                | 03 |    |
| MAT-7216 | Integral Inequalities                              |    | 03 |
| MAT-7217 | Selected Topics in Applied Mathematics             | 03 |    |
| MAT-7218 | Banach Algebras                                    | 03 |    |
| MAT-7219 | Finite Mixture Distributions-II                    | 03 |    |
| MAT-7220 | Harmonic Functions Theory                          | 03 |    |
| MAT-7221 | Perturbation Methods-II                            | 03 |    |
| MAT-7222 | Linear Matrix Inequalities                         | 03 |    |
| MAT-7223 | Time Series  | 03 |    |
| MAT-7224 | General Theory of Relativity                       | 03 |    |
| MAT-7225 | Electrodynamics-II                                 |    | 03 |
| MAT-7226 | Cosmology  |    | 03 |
| MAT-7227 | Loop Groups  |    | 03 |
| MAT-7228 | Magnetohydrodynamics II                            | 03 |    |
| MAT-7229 | C* -Algebras                                       |    | 03 |
| MAT-7230 | Topological Algebras                               |    | 03 |
| MAT-7231 | Optimal State Estimation                           | 03 |    |

## Details of the Courses

### Semester I

**Course Code:** MAT-7101

**Title:** Advanced Functional Analysis

**Credit Hrs:** 03

**Course Outline:** Normed Linear Spaces, Bounded Linear Transformation, Finite Dimensional Normed Linear Spaces, Some Dual Spaces, The Hahn Banach Theorem, The Algebra of Bounded Linear Operators, Baire's Theorem, The Principle of Uniform Boundedness, The Open Mapping Theorem, The Closed Graph Theorem, Hilbert Spaces, Spectral Theory in Hilbert Spaces, Hermitian Symmetric Forms, Orthogonality Self Adjoint Bounded Linear Operator, Spectrum of Bounded Linear Operators, Self Adjoint Bounded Linear Operators, Positive Operators, The Spectral Theorem

#### Texts and Reference Books

1. L. Brown, *Elements of Functional Analysis*, Von Nostrand and Renihold Company, 1970.
2. E. Kreyszig, *Introduction to Functional Analysis with Applications*, John Wiley and Sons, New York, 1989.
3. A. Majeed, *Elements of Topological and Functional Analysis*, Ilmi Kitab Khana, 1994.
4. J. T. Oden, *Applied Functional Analysis*, Prentice Hall Inc, 1979.
5. A. E. Taylor, *Introduction to Functional Analysis*, John Wiley and Sons, New York

**Course Code:** MAT-7102

**Title:** Advanced Topology

**Credit Hrs:** 03

**Course Outline:** Convergence: Sequence and Nets, Filterbase in Space, Convergence, Properties of Filterbases, Closure in Terms of Filterbase, Continuity, Convergence in Cartesian Products, Adequacy of Sequences, Maximal Filterbase Compactness: Compact Spaces, Special Properties of Compact, Countable Compactness, Compactness in Metric Spaces, Perfect Maps, Local Compactness, O-Compact Spaces, Compactification, K-Space, Baire Space Category Function Spaces: The Compact Open Topology, Continuity of Composition, The Evaluation Map, Cartesian Products, Application to Identification Topologies, Basis for  $Z'$ , Compact Subsets of  $Z'$  Sequential Convergence in the C-Topology, Metric Topologies, Relation to the C-Topologies, Point-Wise Convergence, Comparison of Topologies in  $Z'$  The Spaces  $C(Y)$ : Continuity of the Algebraic Operations, Algebras in  $C(Y; C)$ , Stone-Weierstrass Theorem, The Metric Space  $C(Y)$ , Embedding of  $Y$  in  $C(Y)$ , The Ring  $C(Y)$ .

The Complete Spaces: Cauchy Sequences, Complete Metrics and Complete Spaces, Cauchy Filterbases, Total Boundedness, Baire's Theorem for Complete Metric Spaces, Extension of Uniformly Continues Maps, Fixed Point Theorem for Complete Spaces, Complete Subspaces of Complete Spaces, Complete Gauge Structure.

#### Texts and Reference Books

1. J. Dugundji, *Topology*, Allyn and Bascon, Boston, 1966.
2. J. L. Kelley, *General Topology*, Ishi Press, 2008.
3. J. R. Munkress, *Topology A First Course*, Prentice Inc. Englewood Cliffis, New Jessy, 2<sup>nd</sup> Edition, 2005.
4. S. Davis, *Topology*, 1<sup>st</sup> Edition, McGraw-Hill Math, 2004.

**Course Code:** MAT-7103

**Title:** Advanced Optimization Theory

**Credit Hrs:** 03

**Course Outline:** Intro to mathematical optimization, objective of constraint functions, basic optimization concepts, mathematical prerequisites, convexity, gradient vectors, Hessian matrix, global and local minima, saddle points, optimality condictions, general structure for line search method, Wolf conditions, Goldstein conditions, convergence of line search method, convergence of steepest decent method, Newton method, Quasi Newton method, Newton method with Hessian approximation, line search algorithm for Wolf conditions, conjugate gradient method, Trust Region Method and Cauchy point, Newton point, Dogleg method.

#### Texts and Reference Books

1. L. Elsgolts, *DEs and the Calculus of Variations*, Mir Publishers Moscow, 1970.
2. B. S. Gotfried and J. Weisman, *Introduction to Optimization Theory*, Prentice Hall, Englewood Cliffs, NJ, USA, 1973.
3. D. G. Luenberger, *Introduction to Linear and Non-Linear Programming*, Addision Wesley, Reading, Ma, USA, 1973.
4. D. A. Pierre, *Optimization Theory with Applications*, Dover Publications, 1986.

**Course Code:** MAT-7104

**Title:** Variational Inequalities

**Credit Hrs:** 03

**Course Outline:** Variational Inequalities in Fixed Points, The Characterization of the Projection onto a Convex Set, A First Theorem about Variational Inequalities, Some Problems about Variational Inequalities, Variational Inequalities in Hilbert Space, The Obstacle Problem, Variational Inequalities for Monotone Operators, A Variational Inequality with Mixed Boundary Conditions, Penalization

**Texts and Reference Books**

1. C. Baiocchi and A. Capelo, *Variational and Quasivariational Inequalities, Applications to Free Boundary Problems*, John Wiley and Sons, New York, 1984.
2. G. Isac, *Complementarity Problems and Variational Inequalities*, Springer-Verlag, 2006.
3. D. Kinderlehrer and G. Stampacchia, *An Introduction to Variational Inequalities and Their Applications*, Academic Press, New York, 1980.
4. M. A. Noor, *Principles of Variational Inequalities*, Lambert Academic Publishing, Saarbrücken, Germany, 2009.

**Course Code:** MAT-7105

**Title:** Advanced PDEs

**Credit Hrs:** 03

**Course Outline:** Cauchy's Problems for Linear Second Order Equation in N- Independent Variables, Cauchy Kowalewski Theorem, Characteristic Surface, Adjoint Operations, Bicharacteristics, Spherical and Cylindrical Waves, Heat Equations, Wave, Laplace and Diffusion Equations in Spherical and Cylindrical Polar Coordinates, Maximum-Minimum Principle, Non-Homogeneous Partial Differential Equations.

**Texts and Reference Books**

1. C. B. Chester, *Techniques in Partial Differential Equations*, McGraw Hill Book Company, 1971.
2. R. Dennemyer, *Introduction to Partial Differential Equations and Boundary Value Problems*, McGraw Hill Book Company, 1968.
3. H. F. Weinberger, *A First Course in Partial Differential Equations: with Complex Variables and Transform Methods*, Dover Publications, 1995.
4. E. C. Zachmanoglou and D. W. Thoe, *Introduction to Partial Differential Equations with applications*, Dover Publications, 1987.

**Course Code:** MAT-7106

**Title:** Nonlinear Systems and Control

**Credit Hrs:** 03

**Course Outline:**

**Analysis techniques for nonlinear systems:** phase portraits and their symmetries, singular points, phase plan analysis of linear and nonlinear systems, existence of limit cycles,

Fundamentals of Lyapunov Theory: Nonlinear systems and equilibrium points, concept of stability, linearization and local stability, Lyapunov's direct method and stability analysis, Krasovskii and variable gradient methods, performance analysis, control design based on Lyapunov's direct method

Advanced Stability Analysis: Stability of non-autonomous systems, Linearization and Lyapunov's direct methods for nonlinear autonomous systems, Asymptotic properties of functions and their derivatives, Barbalat Lemma, positive real and strictly positive real transfer functions, Kalman-Yakubovich lemma, passivity of linear systems,

Describing Function Analysis: Fundamentals of describing function analysis, common nonlinearities in control systems and their describing functions, Nyquist criterion and its extensions, existence and stability of limit cycles, reliability of describing function analysis,

**Nonlinear Control Systems Design:** Feedback Linearization: Canonical form, Lie derivatives and Lie brackets, diffeomorphism and state transformations, the Frobenius theorem, input-state and input-output linearization of SISO systems, the normal forms and zero dynamics, local and global asymptotic stabilizations, tracking control and inverse dynamics, feedback linearization of multi-input systems,

**Adaptive Control:** Basic concepts in Adaptive Control, Adaptive control of first order systems, Adaptive control of linear systems of relative degree 1 and higher with full state-feedback and output feedback, Adaptive Control of nonlinear systems, robustness of adaptive control systems,

### Texts and Reference Books

1. H. K. Khalil, *Nonlinear Control*, Prentice Hall, 2002.
2. Slotine and Li, *Applied Nonlinear Control*, Prentice Hall, 1991.
3. A. Isidori, *Nonlinear Control Systems*, 3<sup>rd</sup> Edition, Springer, 1995.
4. B. Friedland, *Control System Design: An Introduction to State-Space Methods*, Dover Publications, 2005.

**Course Code:** MAT-7107

**Title:** Advanced Complex Analysis

**Credit Hrs:** 03

**Course Outline:** An Overview of the Theory of a Complex Variable, Argument Principle, Rouché's Theorem, Conformal Mapping, Harwitz Theorems, Cauchy's Theorem on Partial Fraction Expansions, Inverse and Implicit Functions, Riemann Mapping Theorem, Univalent Functions, Basic Properties of Harmonic, Positive Harmonic and Subharmonic Functions, Poisson Integral Formula, Mittag-Leffler and Weierstrass Theorems, Infinite Products and Weierstrass Factorisation Theorem, Analytic Continuation, Special Functions Including Gamma Function, Riemann Zeta Function, Prime Number Theorem, Elliptic Functions

### Texts and Reference Books

1. L. V. Ahlfors, *Complex Analysis*, M. G. Hill, 1979.
2. R.V. Churchill and J.W. Brown, *Complex Variables and Applications*, 5<sup>th</sup> Edition, M. Graw Hill, 1989.
3. J. B. Conway, *Functions of one Complex Variable*, Springer, 1979.
4. E. Hill, *Analytic Function Theory*, Vol. I and II, Chelsea Publishing Company, New York, 1974.

**Course Code:** MAT-7108

**Title:** Sampling Techniques-I

**Credit Hrs:** 03

**Course Outline:** Equal Probability Sampling: Simple Random Sampling and General Formula for The Derivation of Variance and Variance Estimator, Derivation of Variance and Estimated Variance for The Proportion in one Class to a Group of Classes, Derivation of Variance Estimator for Quantitative and Qualitative Characteristics, Stratified Sampling, Optimum Allocation Effect of Deviation From Optimum Allocation, Two Way Stratification, Controlled Selection, Construction of Strata, Gain Due to Stratification, Unequal Probability Sampling: Probability Proportional to Size Sampling, Sampling with Replacement, Cumulative Method, Hansen-Hurwitz (Multinomial), Pathak, Lahiri Selection Procedures, Sampling with Unequal Probability Sampling, Yates-Grundy, Midzuno-Sen-Ikeda, Brewer, Sampford, Dubin, Raj, Murthy, Rao-Hartly-Cochran Selection Procedures.

### Texts and Reference Books

1. W. G. Cochran, *Sampling Techniques*, John Wiley and Sons, New York, 3<sup>rd</sup> Edition, 1977.
2. I. Kish, *Survey Sampling*, John Wiley and Sons, New York, 1965.
3. D. Raj, *Sampling Theory*, M. Graw Hill, New York, 1968.
4. P. V. Sukatme and B. V. Sukatme, *Sampling Theory of Surveys with Application*, Iowa State University Press, USA, 1970.

**Course Code:** MAT-7109

**Title:** Multivariate Analysis

**Credit Hrs:** 03

**Course Outline:** Introduction: Some Multivariate Problems and Techniques, The Data Matrix, Multivariate Normal Distribution Theory: Characterization and Properties, Linear Forms, The Wishart Distribution, The Hotelling  $T^2$  Distribution, Maximum Likelihood Estimation and Other Techniques, Principal Component Analysis: Definition and Properties of Principal Components, Testing Hypothesis about Principal Components, Correspondence Analysis, Discarding of Variables, Principal Component Analysis in Regression. Factor Analysis: The Factor Model, Relationship between Factor Analysis and Principal Component Analysis. Canonical Correlation Analysis: Dummy Variable and Qualitative Data, Qualitative and Quantitative Data. Discriminant Analysis.

### Texts and Reference Books

1. M. Kshirsagar, *Multivariate Analysis*, M. Dekker, New York, 1972.
2. K. V. Mardia, J. T. Kent and J. M. Bibby, *Multivariate Analysis*, Academic Press, London, 1982.
3. A. C. Rencher and W. F. Christenson, *Methods of Multivariate Analysis*, 3<sup>rd</sup> Edition, Wiley, 2012.
4. K. V. Mardia, J. T. Kent and J. M. Bibby, *Multivariate Analysis*, 1<sup>st</sup> Edition, 1980.

**Course Code:** MAT-7110

**Title:** Advanced Mathematical Statistics

**Credit Hrs:** 03

**Course Outline:** Probability Distributions, Weighted Probability Distributions, Transmuted probability Distributions, Convergence in Probability, Weak and Strong Law of Large number, Estimation theory, Constructing estimators, Evaluating estimators, Hypothesis testing, Constructing decision rules, Evaluating testing procedures, Interval estimation, Constructing interval estimators, Evaluating interval estimators, Maximum likelihood large sample theory, Decision theory and Bayesian Statistics, Robust methods.

### Texts and Reference Books

1. G. Casella, and R. L. Berger, *Statistical Inference*, 2<sup>nd</sup> Edition, Duxbury, California, 2002.
2. W. Feller, *An introduction to Probability Theory and Its Applications*, 3<sup>rd</sup> Edition, (Volume I & II), John and Wiley Sons, New York, 2008.
3. J. O. Berger, *Statistical Decision Theory and Bayesian Analysis*, 2<sup>nd</sup> Edition, Springer, 2010.
4. M. Peterson, *An introduction to Statistical Decision Theory*, 1<sup>st</sup> edition, Cambridge University Press, 2009.

**Course Code:** MAT-7111

**Title:** Advanced Probability Theory

**Credit Hrs:** 03

**Course Outline:** Probability review, convergence of sequences, characteristic function, transformation of random variables, discrete and continuous probability models, Sets, Indicator functions and classes of sets, measure space and probability space, measurable functions, integration theory and Lebasque measure

### Texts and Reference Books

1. Stirzaker, *Probability and Random Variables*, Cambridge University Press, 1999.
2. Stuart and O. K. Kendall's, *Advanced Theory of Statistics, Vol. I*, Charles Griffin, 1998.
3. Rohatgi, *Introduction to Probability Theory*, M. Graw Hill, 1976.
4. V. S. Borkar, *Probability Theory*, 1<sup>st</sup> Edition, Springer, 1995.

**Course Code:** MAT-7112

**Title:** Introduction to Finite Element Methods

**Credit Hrs:** 03

**Course Outline:** Finite Element Methods: General Approach, The Galarkin Method in One and More Dimensions and Application, Error Bound on the Galarkin Method and Application, The Method of Collocation, Error Bounds on the Collocation Method and Application, Comparison of Efficiency of the Finite Difference and Finite Element Method, Application to Solution of Linear and Non-Linear Partial Differential Equations Appearing in Physical Problems

### Texts and Reference Books

1. S. D. Burnett, *Finite Element Analysis from Concept to Applications*, Addison Wesley, 1987.
2. G. S. Desai, *Elementary Finite Element Method*, Prentice Hall, 1988.
3. G. Strang and G. Fix, *Analysis of Finite Element Method*, Prentice Hall, New Jersey, 1973.
4. J. N. Reddy, *Introduction to the Finite Element Method*, 3<sup>rd</sup> Edition, MHI, 2006.



**Course Code:** MAT-7113

**Title:** Mathematical Techniques for BVPs

**Credit Hrs:** 03

**Course Outline:** Green's Function Method, Perturbation Method: Regular and Singular Perturbation Techniques with Application, Variational Methods, Wiener-Hopf Techniques with Applications to Diffraction Problems.

**Texts and Reference Books**

1. R. Mitra and S. W. Lee, *Analytical Techniques in the Theory of Guided Waves*, Macmillan, 1971.
2. E. J. Hinch, *Perturbation Methods*, Cambridge University Press, 1991.
3. B. Noble, *Methods Based on the Wiener Hopf Techniques for the Solution of Partial Differential Equations*, 2<sup>nd</sup> Edition, American Mathematical Society, 1988.
4. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Society for Industrial and Applied Mathematics, 1987.

**Course Code:** MAT-7114

**Title:** Convex Analysis

**Credit Hrs:** 03

**Course Outline:** Affine Sets, Convex Sets and Cones, The Algebra of Convex Sets, Convex Functions, Functional Operations, Relative Interiors of Convex Sets, Closures of Convex Functions, Recession Cones and Unboundedness, Some Closedness Criteria, Continuity of Convex Functions, Separation Theorems, Conjugates of Convex Functions, Support Functions, Polars of Convex Sets, Polars of Convex Functions, Linear Inequalities, Directional Derivatives and Subgradients, Differential Continuity and Monotonicity, Differentiability of Convex Functions, The Legendre Transformation, The Minimum of a Convex Function, Ordinary Convex Programs and Lagrange

**Texts and Reference Books**

1. G. G. M. Ilyaeve and V. M. Tikhomirov, *Convex Analysis: Theory and Applications*, AMS, 2003.
2. R. T. Rockafellar, *Convex Analysis*, Princeton University Press, 1997.
3. J. V. Tiel, *Convex Analysis: An Introductory Text*, Wiley, 1984.
4. J. B. H. Urruty and C. Lemarechal, *Fundamentals of Convex Analysis*, Springer Verlag, 2001.

**Course Code:** MAT-7115

**Title:** Semigroups in Geometric Functions Theory

**Credit Hrs:** 03

**Course Outline:** Holomorphic Functions and their Convergence, Metric Spaces and Fixed Point Principles, Schwarz-Pick Lemma and Automorphisms, Boundary Behavior of Holomorphic Self-Mappings and Fixed Points and Fixed Point Free Holomorphic Self-Mappings, The Denjoy-Wolff Theorem, Commuting Family of Holomorphic Mappings, Hyperbolic Geometry and Fixed Points, The Poincare Metric and its Compatibility with Convexity, Infinitesimal Poincare Metric and Geodesics, Fixed Points of Non-expansive Mappings

One-Parameter Continuous Semigroup of Holomorphic and Nonexpansive Self-Mappings, Infinitesimal Generator, Nonlinear Resolvent and the Exponential Formula, Monotonicity w.r.t the Hyperbolic Metric, Flow Invariance Conditions, The Berkson-Porta Parametric Representation of Semi-Complete Vector Fields, Asymptotic Behavior of Continuous Flows, Stationary Points of a Flow, Null Points of Complete Vector Fields, Embedding of Discrete Time Group and Rates of Convergence of a Flow with an Interior Stationary Point, A Rate of Convergence in Poincare Metric, Continuous Version of the Julia-Wolff-Caratheodory Theorem, Lower Bounds for Monotone Functions, Asymptotic behavior of Continuous Flows, Dynamical Approach to Starlike and Spirallike Functions

**Texts and Reference Books**

1. D. Shoket, *Semigroups in Geometric Function Theory*, Kluwer Academic Publishers, 2001.
2. S. G. Krantz, *Geometric Function Theory: Explorations in Complex Analysis*, 2006<sup>th</sup> Edition, Birkhäuser, 2005.
3. G. Kohr, G. Graham and I. Graham, *Geometric Function Theory in One and Higher Dimensions*, 1<sup>st</sup> Edition, CRC Press, 2003.
4. L. V. Ahlfors, *Conformal Invariants: Topics in Geometric Function Theory*, McGraw-Hill Inc., US, 1973.

**Course Code:** MAT-7116

**Title:** Conformal Mappings

**Credit Hrs:** 03

**Course Outline:** Conformal Mappings on Simply-connected Domains: Mapping Properties of Analytic Functions, The Linear Transformations, The Schwarz Lemma, The Symmetry Principle, The Schwarz-Christoffel Formula, Domains Bounded by Circular Arcs, The Kernel Functions, Conformal Mappings of Nearly Circular Domains

Mapping Properties of Special Functions: Rational Functions of Second Degree, Exponential and Trigonometric Functions, Elliptic Functions, Domains Bounded by Arcs of Confocal Conics, The Schwarzian  $\delta$ -Functions, the Elliptic Modular Functions

Conformal Mappings on Multiply-Connected Domains: Conical Domains and their Characterizations by Extremal Problems, Green's Function and the Dirichlet Problems, Area Problems, The Kernel Functions and the Orthonormal Sets

**Texts and Reference Books**

1. L. Bieberbach, *Conformal Mappings*, Chelsea Publishing Company, 1964.
2. Z. Nehri, *Conformal Mappings*, Dover Publications, 1975.
3. I. I. Gikhman and A.V. Skorokhod, *Theory of Random Processes*, N. Moskow, 1973.
4. R. Schinzinger and P. A. A. Laura, *Conformal Mappings*, Dover Publications, 2003.

**Course Code:** MAT-7117

**Title:** Stochastics Processes

**Credit Hrs:** 03

**Course Outline:** Definition of a Stochastic Process, Characterization of a Stochastic Process, Discrete-Time and Continuous-Time Stochastic Process and Their First and Second Order Statistics, Continuity, Derivative and Integral of a Stochastic Process, Time-Averages and Ergodic Theorems, Stationarity, Power Spectral Density, Time- Series Analysis, Discrete-Time Markov Chains, Continuous-Time Markov Chains and Introduction To Queuing Theory

**Texts and Reference Books**

1. W. Whitt, *Stochastic-Process Limits: An Introduction to Stochastic-Process Limits and Their Applications to Queues*, Springer, New York, USA, 2002.
2. Z. Brzeźniak and T. Zastawniak, *Basic Stochastic Processes: A Course Through Exercises*, Springer, New York, 2005.
3. S. M. Ross, *Stochastic-Process*, 2<sup>nd</sup> Edition, Wiley, 1995.
4. R. G. Gallager, *Stochastic-Process*, 1<sup>st</sup> Edition, Cambridge University Press, 2014.

**Course Code:** MAT-7118

**Title:** Basics of the Theory of Fluids

**Credit Hrs:** 03

**Course Outline:** Euler's Equations of Motion, Viscosity, Navier-Stokes Equations and Exact Solutions, Dynamical Similarity and Reynolds Number, Energy Equation, Boundary Layer Concept and Governing Equations, Magnetohydrodynamics (MHD) Equations, Fluid Drifts, Stability and Equilibrium Problems, Introduction to Turbulent Flow.

**Texts and Reference Books**

1. G. Astarita and G. Merrucci, *Principles of Non-Newtonian Fluid mechanics*, M. Graw Hill, 1974.
2. R. B. Bird, R. C. Armstrong and O. Hassager, *Dynamic of Polymeric liquids*, Vol. I, 2<sup>nd</sup> Edition, John Wiley and Sons, New York, 1987.
3. J. Harris, *Rheology and Non-Newtonian Flow*, Longman Inc., New York, 1977.
4. Schowalter, *Mechanics of Non-Newtonian Fluids*, Pergamon Press, New York, 1978.

**Course Code:** MAT-7119

**Title:** Finite Mixture Distributions-I

**Credit Hrs:** 03

**Course Outline:** Introduction: Basics Definition and Concepts, Statistical Problem Associated with Mixtures, Application of Finite Models, Mathematical Aspects of Mixture: Identifiability, Multimodality, Properties of General Mixture, Parameters of Mixture: Various Methods of Determining the Parameters of a Mixture.

### Texts and Reference Books

1. B. S. Everitt and D. J. Hand, *Finite Mixture Distribution*, Chapman and Hall London, 1981.
2. D. M. Titterton, A. F. M. Smith and U. E. Makov, *Statistical Analysis of Finite Mixture Distributions*, John Wiley and Sons, New York, 1985.
3. G. McLachlan and D. Peel, *Finite Mixture Models*, 1<sup>st</sup> Edition, Wiley Interscience, 2000.
4. S. F. Schnatter, *Finite Mixture and Markov Switching Models*, 2006 edition, Springer, 2006.

**Course Code:** MAT-7120

**Title:** Approximation Theory

**Credit Hrs:** 03

**Course Outline:** Best Approximation in Metric and Normed Spaces, Least Square Approximation, Rational Approximation, Haar Condition and Best Approximation in Function Spaces, Interpolation, Stone-Weierstrass Theorem for Scalar and Vector-Valued Functions, Spline Approximation.

### Texts and Reference Books

1. E. W. Cheney, *Introduction to Approximation Theory*, M. Graw Hill, New York, 1966.
2. I. Singer, *Best Approximation in Normed Linear Spaces by Elements of Linear Subspaces*, Springer Verlag, 1970.
3. J. R. Rice, *The Approximation of Functions, Vol. I, II*, Addison Wesley, 1969.
4. R. B. Holmes, *A Course on Optimization and Best Approximation, Lecture Notes*, Springer Verlag, 1971.

**Course Code:** MAT-7121

**Title:** Perturbation Methods-I

**Credit Hrs:** 03

**Course Outline:** Introduction, Order Symbols and Gauge Functions, Asymptotic Series and Expansions, Asymptotic Expansion of Integrals, Integration by Parts, Laplace's Method and Watson's Lemma, Method of Stationary Phase and Method of Steepest Descent, Straight Forward Expansions and Sources of Non-uniformity, The Duffing Equation, Small Reynolds Number Flow Past a Sphere, Small Parameter Multiplying The Highest Derivative, The Method of Strained Coordinates, The Lindstedt Poincare Method, Renormalization Method, Variation of Parameters and Method of Averaging, Method of Multiple Scale with Examples.

### Texts and Reference Books

1. A. H. Nayfeh, *Perturbation Methods*, 1<sup>st</sup> Edition, Wiley-VCH, 2000.
2. E. J. Hinch, *Perturbation Methods*, Cambridge University Press, 1991.
3. A. H. Nayfeh and D. T. Mook, *Nonlinear Oscillations*, Wiley-VCH, 1995,
4. A. H. Nayfeh, *Introduction to Perturbation Techniques*, 1<sup>st</sup> Edition, Wiley-VCH, 1993.

**Course Code:** MAT-7122

**Title:** Lie Algebra

**Credit Hrs:** 03

**Course Outline:** Definitions and Example of Lie Algebras, Ideals and Quotients, Simple, Solvable and Nilpotent Lie Algebras, Radical of a Lie Algebra, Semi-simple Lie Algebra, Engel's Nil Potency Criterion, Lie's and Cartan Theorems, Jordan-Chevalley Decomposition, Killing Forms, Criterion for Semisimplicity, Product of Lie Algebra, Classification of Lie Algebra up to Four Dimension, Application of Lie Algebras.

### Texts and Reference Books

1. J. E. Humphreys, *Introduction to the Algebra and Representation Theory*, S. Verlag, 1972.
2. N. Jacobson, *Lie Algebra*, Interscience, New York, 1983.
3. J. Lapowsky and G.W. MacCullum, *Elementary Lie Algebra Theory*, Yale University, 1974.
4. W. Jr. Miller, *Symmetry Groups and Their Groups*, Academic Press, 1972.
5. O. Neill, *Semi-Riemannian Geometry*, Academic Press, 1983.

**Course Code:** MAT-7123

**Title:** Topological Groups

**Credit Hrs:** 03

**Course Outline:** General Theory of Topological Groups, Translations in Topological Groups and some Examples, Neighborhood System of Identity, Separation Axioms in Topological Groups, Uniform Structure on a Topological Groups, Products and Inverse Limits of Groups, General Results on Locally Compact Groups.

**Texts and Reference Books**

1. G. E. Bredon, *Introduction to Compact Transformation Groups*, Academic Press, 1972.
2. I. P. Eisenhart, *Continuous Groups of Transformation*, Princeton University Press, 1933.
3. H. Taqdir, *Introduction to Topological Groups*, W. B. Savder's Company, 1966.
4. N. G. Markley, *Topological Groups an Introduction*, 1<sup>st</sup> Edition, Wiley, 2010.

**Course Code:** MAT-7124

**Title:** Topological Vector Spaces

**Credit Hrs:** 03

**Course Outline:** Topological Vector Spaces, Semi-Norms Locally Convex Spaces, The Hahn Banach Theorem, The Kroin Milan Theorem, Duality and the Weak Topology, Weak Compactness in Normed Vector Spaces, Barrelled Spaces and the Banach Stienhaus Theorem, The Open Mapping and Closed Graph Theorem, The Algebra of Bounded Linear Operators on a Banach Spaces, The Riesz Schuder Theory of Compact Linear Operators, Topological Tensor Products, Nuclear Mapping and Spaces.

**Texts and Reference Books**

1. C. Romulus, *Topological Vector Spaces*, Editura Acadmei Noor dhoff International Publishing Bucurestim Rimania Leuden, Netherland, 1977.
2. J. L. Kelly, *General Topology*, Ishi Press, 2008.
3. H. H. Scheafer, *Topological Vector Spaces*, 2<sup>nd</sup> Edition, Springer, 1999.
4. J. Horwath, *Topological Vector Spaces and Distributions*, Dover Publications, 2012.

**Course Code:** MAT-7125

**Title:** Electrodynamics-I

**Credit Hrs:** 03

**Course Outline:** Maxwell's Equations, Electrodynamics Wave Equations, Boundary Conditions, Wave in Conducting and Non-Conducting Media, Reflection and Polarization, Energy Density and Energy Flux, Lorntz Formula, Wave Guides and Cavity Resonators, Spherical and Cylindrical Waves, Inhomogeneous Wave Equations, Retarded Potentials, Lenard-Wiechart Potentials, Fields of Uniformly Moving Point Charge, Radiation From a Group of Moving Charges, Field of Oscillating Dipole, Field of an Accelerated Point Charge.

**Texts and Reference Books**

1. D. Corson and P. Lorrain, *Introduction to Electromagnetic Fields and Waves*, Freeman, 1962.
2. J. D. Jacson, *Classical Electromagnetic*, 3<sup>rd</sup> Edition, Wiley, 1998.
3. K. Panofsky and M. Philips, *Classical Electricity and Magnetism*, Addison Wesley, 1962.
4. I. R. Retiz and F. J. Malford, *Foundation of Electromagnetic Theory*, Addison Wesley, 1969.

**Course Code:** MAT-7126

**Title:** Theory of Group Graphs

**Credit Hrs:** 03

**Course Outline:** Graphs, Graphs for Group Action, Projective Special Linear Group and its Action in Real, Rational and Irrational Fields, Graphical Representations of Mobius, Orthogonal, Affine and Euclidean Groups.

**Texts and Reference Books**

1. H. S. M. Coxeter, *Generators and Relation for Discrete Groups*, 2<sup>nd</sup> Edition, Springer, 1965.
2. J. F. Humphreys, *A Course in Group Theory*, 1<sup>st</sup> Edition, Oxford University Press, 1996.
3. W. Magnus, A. Karnass and D. Solitar, *Combinatorial Group Theory*, Dover Publishers, 2004.
4. W. Jr. Miller, *Symmetry Groups and Their Groups*, Academic Press, 1972.

**Course Code:** MAT-7127

**Title:** Theory of Group Actions

**Credit Hrs:** 03

**Course Outline:** Preliminaries, The Theory of Groups Actions, Cosets Spaces, Multiplicative Group of a Finite Field, Extension of Finite Fields, Projective Line over Finite Fields, Projective and Linear Groups through Actions.

**Texts and Reference Book**

1. H. S. M. Coxeter , *Generators and Relation for Discrete Groups*, 2<sup>nd</sup> Edition, Springer,1965.
2. J. F. Humphreys, *A Course in Group Theory*, 1<sup>st</sup> Edition, Oxford University Press, 1996.
3. W. Magnus, A. Karnass and D Academic Press, 1972.
4. . Solitar, *Combinatorial Group Theory*, Dover Publishers, 2004.

**Course Code:** MAT-7128

**Title:** Magneto Hydrodynamics-I

**Credit Hrs:** 03

**Course Outline:** Basic Equations: Equations of Electrodynamics, Equations of Fluid Dynamics, Ohm's Law Equations of Magneto Hydrodynamics.

Motion of an Incompressible Fluid: Motion of a Viscous Electrically Conducting Fluid with Linear Current Flow, Steady State Motion along a Magnetic Field, Wave Motion of an Ideal Fluid

Small Amplitude MHD Waves: Magneto-Sonic Waves, Alfven's Waves, Damping and Excitations of MHD Waves, Characteristic Lines and Surfaces.

Simple Wave and Shock Wave in Magneto Hydrodynamics, Stability and Structure of Shock Waves in Relativistic Magneto Hydrodynamics, Stability and Structure of Shock Waves, Discontinuities in Various Quantities, Piston Problem, Oblique Shock Waves.

**Texts and Reference Books**

1. A. Etal, *Plasma Electrodynamics*, Pergamon Press, 1975.
2. H. Alfven, *Cosmical Electrodynamics*, Create Space Independent Publishing Platform, 1950.
3. J. E. Anderson, *Magneto hydrodynamics*, Shock Waves, M. I. T. Press, Cambridge, 1963.
4. T. G. Cowling, *Magnetohydrodynamics*, Interscience Publishers, 1963.

**Course Code:** MAT-7129

**Title:** Advanced Measure Theory

**Credit Hrs:** 03

**Course Outline:** Locally Compact Spaces: Topological Lemmas, Borel Sets and Baire Sets, Regular Measure, Generation of Borel Measures, Regular Contents, The Classes of Continuous Functions, Linear Functional, Haar Measure: Full Subgroups, Existence, Measurable Groups, Uniqueness

Measure and Topological in Groups: Topology in Terms of Measure, Woil Topology, Quotient Group, The Regularity of Haar Measure, General Vector Measure Theory: Elementary Properties of Vector Measure, Countably Additive Vector Measure, The Hikodym Boundedness Theorem, Rosenthal's Lemma and the Structure of a Vector Measure, The Caratheodory Hahn Kluvanek Extension Theorem and Strongly Additive Vector Measure, Notes and Remarks, Integration

**Texts and Reference Books**

1. D. L. Cohn, *Measure Theory*, Birkhausar, Boston, 1980.
2. A. R. Khan, *Introduction to Lebesgue Integration*, Ilmi Kitab Khana, Lahore, 2<sup>nd</sup> Edition, 2003.
3. W. Rudin, *Real and Complex Analysis*, 3<sup>rd</sup> Edition, M. Graw Hill, New York, 1987.
4. P. R. Halmos, *Measure Theory*, 2<sup>nd</sup> Edition, Springer, 1978.

**Course Code:** MAT-7130

**Title:** Theory of Complex Manifolds

**Credit Hrs:** 03

**Course Outline:** Algebraic Preliminaries, Almost Complex Manifolds and Complex Manifolds, Connections in Almost Complex Manifolds, Hermitian Metric and Kaehler Metric, Kaehler Metric in Local Coordinate System, Example of Kaehler Manifolds, Holomorphic Sectional Curvature, Derham Decomposition of Kaehler Manifolds, Curvature of Kaehler Submanifolds, Topology of Kaehler Manifolds with Positive Curvature, Hermitian Connections in Hermitian Vector Bundles, Homogeneous Spaces, Homogeneous Complex Manifolds, Invariant Connections on Homogeneous Spaces, Invariant Connections on Reductive Homogeneous Spaces, Invariant Indefinite Riemannian Matrices, Holonomy Groups of Invariant Connections, The Derham Decomposition and Irreducibility, Invariant Almost Complex Structure.

#### **Texts and Reference Books**

1. S. Kobayashi and K. Nomiza, *Foundations and Differential Geometry*, Vol. II, Interscience Publishers, John Wiley and Sons, 1969.
2. B. V. Shabat, *Introduction to Complex Analysis*, Part II, AMS, 1992.
3. Griffiths and Harris, *Principles of Algebraic Geometry*, Wiley and Sons, 1994.
4. K. Kodaira, *Complex Manifolds and Deformation of Complex Structures*, 2005 Edition, Springer, 2004.

**Course Code:** MAT-7131

**Title:** Complex Analysis of Several Variables

**Credit Hrs:** 03

**Course Outline:** Holomorphic Functions: Review of One Variable Theory, Real and Complex Differentiability, Power Series, Complex Differentiable Functions, Cauchy Inequalities, The Maximum Principles.

Extension of Analytical Functions: Hartogs Figures, Hartogs Theorems, Domains of Holomorphy, Holomorphic Convexity, Theorem of Cartan Thullen.

Levi-Convexity: The Levi Forms, Geometric Interpretation of its Signature, E. E. Levi's Theorem, Connections with Kählerian Geometry, Elementary Properties of Plurisubharmonic Functions.

Introduction to Cohomology: Definition and Example of Complex Manifolds, The  $\bar{\partial}$  Operators, The Poincaré Lemma and the Dolbeault Lemma, The Cousin Problems, Introduction to Sheaf Theory.

#### **Texts and Reference Books**

1. J. Morrow and K. Kodaira, *Complex Manifolds*, Holt, Rinehart and Winston, New York, 1971.
2. L. Hormander, *An Introduction to Complex Analysis in Several Variables*, D. V. Nostad, New York, 1966.
3. H. Grauert and K. Fritsch, *Several Complex Variables*, Springer Verlag, 1976.
4. M. Field, *Several Variables and Complex Manifolds*, Cambridge University Press, 1982.

**Course Code:** MAT-7132

**Title:** Advanced Analytical Dynamics

**Credit Hrs:** 03

**Course Outline:** Equations of Dynamic and its Various Forms, Equations of Lagrange and Euler, Jacobi's Elliptic Functions and the Quantitative and Qualitative Solutions of the Problem of the Euler and Poisson, the Problems of Lagrange and Poisson, Dynamical System, Equations of Hamilton and Appel, Hamilton-Jacobi Theorem, Separable System, Hamilton's Variational Principle and its Consequences. Group of Continuous Transformations and Poincaré's Equations, System with one Degree of Freedom, Singular Points, Cyclic Characteristics of System With N-Degree of Freedom, Ergodic Theorem, Metric Indecomposability, Stability of Motion, Periodic Orbits.

#### **Texts and Reference Books**

1. H. Baruh, *Analytical Dynamics*, Heinmann, 1<sup>st</sup> Edition, WCB/McGraw-Hill, 1998.
2. E. T. Whittaker, *A treatise on Dynamic of Rigid Bodies and Particles*, At the University Press, 1927.
3. V. D. Sapiro, *Advanced Analytical Dynamics: Theory and Applications*, 1st Edition, Cambridge University Press, 2017.
4. L. Meirovitch, *Methods of analytical dynamics*, McGraw-Hill, 1970.

**Course Code:** MAT-7133

**Title:** General Relativity

**Credit Hrs:** 03

**Course Outline:** Review of Special Relativity, Tensor and Field Theory, The Principles on which General Relativity is Based, Einstein's Field Equations, Obtained From Geodesic Deviations, Vacuum Equation, The Schwarzschild Exterior Solution, Solution of the Einstein-Maxwell Field Equations and the Schwarzschild Interior Solution, The Kerr-Newman Solution (Without Derivation), Foliation, Relativistic Corrections to Newtonian Gravity, Black Holes, The Kruskal and Penrose Diagrams, The Field Theoretic Derivation of Einstein's Equations, Weak Field Approximations and Gravitational Waves, Kaluza-Klein Theory, Isometrics, Conformal Transformations, Problems of Quantum Gravity.

**Texts and Reference Books**

1. S. W. Hawking and G. F. R. Ellis, *The Large Scale Structure of Space-Time*, Academic Press, 1972.
2. C. W. Misner, K. S. Thorne and J. A. Wheeler, *Gravitation*, W. H. Freeman, 1974.
3. A. Qadir, *Relativity: An Introduction to the Special Theory*, World Scientific, 1989.
4. R. M. Wald, *General Relativity*, University Of Chicago Press, 1984.

**Course Code:** MAT-7134

**Title:** Astrophysics

**Credit Hrs:** 03

**Course Outline:** Static Stellar Structure and the Equilibrium Conditions, Introduction to Stellar Modeling, The Hertzsprung-Russell Diagram and Stellar Evolution, Gravitational Collapse and Degenerate Stars, White Dwarfs, Neutron Stars and Black Holes, System of Stars, Irregular and Globular Clusters, Galaxies Super Clusters and Filaments, Astrophysical and Galactic Haloes.

**Texts and Reference Books**

1. S. Chandrasekhar, *An Introduction to the Study of Stellar Structure*, Dover Publications, 1967.
2. C. W. Misner, K. S. Thorne and J. A. Wheeler, *Gravitation*, W. H. Freeman and Company, 1973.
3. L. Richard and T. Deeming, *Astrophysics, Vol. I and II*, Jones and Bartlett Publishers, 1984.
4. M. Schwarzschild, *Structure and Evolution of Stars*, Dover Publishers, New York, 1965.

**Course Code:** MAT-7135

**Title:** The Classical Theory of Fields

**Credit Hrs:** 03

**Course Outline:** Review of Continuum Mechanisms, Solid and Fluid Media, Constitutive Equations and Conservation Equations, The Concept of a Field, The Four Dimensional Formulation of Fields and the Stress-Energy Momentum Tensor, The Scalar Fields, Linear Scalar Fields and Klein-Gordon Equations, Non-Linear Scalar Fields and Fluids, The Vector Fields, Linear Massless Scalar Fields and the Maxwell Field Equations, The Electromagnetic Energy-Momentum Tensor, Electromagnetic Waves, Diffraction of Waves, Advanced and Retarded Potential, Multiple Expansion of the Radiation Field, The Massive Vector (Proca) Field, The Tensor Fields, The Massless Tensor Field and Einstein Field Equations, Gravitational Waves, The Massive Tensors Field, Coupled Field Equations.

**Texts and Reference Books**

1. J. D. Jackson, *Classical Electrodynamics*, John Wiley and Sons, New York, 1975.
2. L. D. Landau and M. Lifshitz, *The Classical Theory of Fields*, W. H. Freeman and Company 1973.
3. C. W. Misner, K. S. Thorne and J. A. Wheeler, *Gravitation*, W. H. Freeman and Company, 1973.
4. P. Roman, *Introduction to Quantum Field Theory*, John Wiley and Sons, New York, 1969.
5. L. A. Scipio, *Principals of Continua with Application*, John Wiley and Sons, New York, 1969.

**Course Code:** MAT-7136

**Title:** Graph Theory

**Credit Hrs:** 03

**Course Outline:** Undirected Graphs, Geometric Graphs, Abstract Graphs, Isomorphism, Edge Progressions Chains and Circuits, Rank and Nullity, Degrees, Trees, Bipartite Graphs, Unicursal Graphs, Hamiltonian Graphs. Directed Graphs, Arc Progressions, Paths Progression and Cycle Progression

Partition and Distances in Graphs, Edge Partitions, Arc Partitions, Hamiltonian Chains and Circuits, Vertex Partitions, Radius and Diameter, Minimal Length Problem, Foundation of Electrical Network Theory, Matrix Representation, The Incidence Matrix, The Circuit Matrix, The Cut-Set Matrix, The Vertex or Adjacency Matrix, The Path Matrix, Network Flows, Network Flow Problems.

**Texts and Reference Books**

1. J. A. Bondy and U. S. R. Murty, *Graph Theory*, Springer Verlag, York, 2008.
2. B. W. Douglas, *Introduction to Graph Theory*, Prentice Hall, 2001.
3. G. Jonathan and Y. Jay, *Graph Theory and its Applications*, CRC Press, London 1999.
4. R. J. Wilson, *Introduction to Graph Theory*, Prentice Hall Wesley, 1996.

**Course Code:** MAT-7137

**Title:** Introduction to Robotics

**Credit Hrs:** 03

**Course Outline:** **Fundamental Concepts:** Introduction to Robot (Fundamental notions and Definitions), **Jacobians:** Transformations and Jacobians, Manipulator. **Kinematics:** Kinematics (Forward and Inverse) of manipulator, Manipulator Dynamics, Trajectory Generation, Manipulator Mechanism, Manipulator Design. **Linear Control:** Linear Control of Manipulator, Non-linear Control of Manipulator, Forced Control of Manipulator, **Multivariable Control:** Multivariable control, Feedback linearization, Variable structure and Adaptive Control.

**Texts and Reference Books**

1. J. J. Craig, *Introduction to Robotics*, Addison-Wesley Publishing Company, 1999.
2. Mark, W. Sponge and M. Vidyasagar, *Robot Dynamics Control*, John Wiley and Sons, 2004.
3. Gene Franklin, J. David Powell *Feed-back Control of Dynamic Systems*, A. E. N. Addison-Wesley Publishing Company, 1989.
4. S. M. Shinnars, *Modern Control System Theory and Applications*, Addison-Wesley Publishing Company, 1987.
5. John, J. Craig, *Adaptive Control of Mechanical Manipulators*, Addison-Wesley Publishing Company, 1997.

**Course Code:** MAT-7138

**Title:** Advanced Abstract Algebra

**Credit Hrs:** 03

**Course Outline:** Endomorphism and Automorphism of Groups, Simple Groups (Definition and Examples), Direct Product of Groups, Sylow Groups and Sylow Theorems, Normal Series of a Group, Refinement Theorem, Composition Series and Jordan Holder Theorem, Solvable and Nilpotent Groups, Finitely Generated Abelian Groups.

**Texts and Reference Books**

1. P. M. Cohn, *Algebra*, Vol. I & II, John Wiley & Sons,
2. S. Lang, *Algebra*, Springer Verlag, 2002.
3. D.S. Dummit and R. M. Foote, *Abstract Algebra*, 3rd Edition, Wiley, 2003.
4. J. A. Gallian, *Contemporary abstract algebra*, D.C. Heath, 1986.



## Semester II

**Course Code:** MAT-7201      **Title:** Geometric Functions Theory      **Credit Hrs:** 03

**Course Outline:** Univalent Functions, Some Elementary Transformations of Univalent Functions and Their Properties, Growth and Distortion Theorems for Univalent Functions, Functions with Positive Real Part and Their Related Concepts, Star-Shaped Domains and Starlike Functions, Convex Domains and Convex Functions, Coefficient Bounds, Distortion and Growth Theorem, Functions with Bounded Mocanu Variations Spirallike, Close-to-Convex and Quasi-Convex Functions, Functions with Bounded Boundary and Bounded Radius Rotations, Bazilevic Functions, Subordination and Convolution in Geometric Function Theory and Their Applications, Some Operators

### Texts and Reference Books

1. P.L. Duren, *Univalent Functions*, Grundlehren der Math. Wissen chaften, Springer-Verlag, New York-Berlin, 1983.
2. A. W. Goodman, *Univalent Functions*, Vol. I and II, Polygonal Publishing House, Washington, New Jersey, 1983.
3. D. G. Zill and P. D. Shanahan, *A First Course in Complex Analysis with Applications*, Jones and Bartlet Publishers, Sudbury, Massachusetts, 2008.
4. S. G. Krantz, *Explorations in Complex Geometric Function Theory Analysis*, 2006 Edition, Birkhäuser, 2005.

**Course Code:** MAT-7202      **Title:** Selected Topics in Pure Mathematics      **Credit Hrs:** 03

**Course Outline:** Course out lines of this course will be determined by the concerned teacher as per requirement of a student in connection with his/her research.

**Course Code:** MAT-7203      **Title:** Advanced Mathematical Modeling      **Credit Hrs:** 03

**Course Outline:** Modeling through Differential Equations, Mathematical modeling through Ordinary Differential Equations, Mathematical modeling through system of Ordinary Differential equations of first order, Excursive of some modeling projects to demonstrate the variety of the require equations to formulate essential, control theory as modeling tool, Parameter estimation as optimization problem, Sensitivity analysis, Parameter estimation, Situation giving rise to Partial Differential Equations, Modeling through Delay differential and Differential–Difference equations

### Texts and Reference Books

1. Edwards, D. and Hamson, *Mathematical modeling Skills*, Macmillan Press Ltd, 1996.
2. Giordano, F.R., Weir, M.D. and Fox, W.P., *A First Course in Mathematical modeling*, Thomson Brooks/Cole, 2003.
3. J.N.Kapur, *Mathematical modeling*, New Age international (P) Limited, 2015.
4. M. M. Meerschaert, *Mathematical modeling*, 4<sup>th</sup> Edition, Academic Press, 2013.

**Code:** MAT-7204      **Title:** Parameter Estimation and Sensitivity Analysis      **Credit Hrs:** 03

### Course Outline:

Some Basic Notions from Probability Theory, Probability spaces, random variables and distribution functions, Expected value and variance, Normally distributed random variables, Some simple examples, Parameter Estimation, Problem formulation, First order necessary condition, Second order conditions, The expected value for the least squares estimator, The variance-covariance matrix for the least squares estimator Sensitivity Analysis, definition, classical sensitivity, Sensitivity equations, fisher information matrix.

### Texts and Reference Books

1. J. N. Kapur, *Mathematical Modelling*, New Age International, 01-jan-1988.
2. Sandip Banerjee, *Mathematical Modelling*, CRC press, 07-Feb-2014.
3. J. Berry and J. Stephen, *Mathematical Modelling*, PLC Great Britian 1995.
4. E. A. Bender, *Mathematical Modelling*, 1<sup>st</sup> Edition, Dover Publications, 2000.

**Course Code:** MAT-7205

**Title:** Numerical Solutions of PDEs

**Credit Hrs:** 03

**Course Outline:** Preliminaries, Classification of PDEs, Canonical Forms and Well-Posed Problems, Behavior of Solutions, Characteristics, Introduction to Finite Difference Methods

Basics of Finite Difference Approximations: Derivation of Finite Difference Approximations, Consistency, Stability, and Convergence for Difference Approximations, Lax Theorem, Matrix and Fourier Stability Analysis, Parabolic Equations: Explicit and Implicit Methods for the Heat Equation, Direction Splitting and ADI Schemes, Convection-Diffusion Equations

Hyperbolic Equations: Finite Difference Methods for the Wave Equation and High-Order Methods, First-Order Non-Linear Equations, Quasi-Linear and Conservation Forms, Characteristics, Shock Waves and Contact Discontinuities, Elliptic Equations: Dirichlet and Neumann Problems, Solvability, Direct vs. Iterative Methods of Solution

#### **Texts and Reference Books**

1. R. J. LeVeque, *Finite Difference Methods for ODEs and PDEs*, SIAM, Philadelphia, 2007.
2. K. Morton and D. Mayers, *Numerical Solution of PDEs*, Cambridge University Press, 1994.
3. J. W. Thomas, *Numerical PDEs*, Finite Difference Methods, Springer-Verlag, 1995.
4. J. W. Thomas, *Numerical PDEs: Conservation Laws and Elliptic Equations*, Springer-Verlag, 1999.

**Course Code:** MAT-7206

**Title:** Optimal Control

**Credit Hrs:** 03

**Course Outline:** Calculus of Variation: Principle of calculus of variation, Euler Equation in Calculus of variation, some important theoretical results of calculus of variation and mathematical examples

Optimal Control and the Minimum Principle: Application of calculus of variation in optimal control, simplest problem in the Calculus of variation, Necessary condition for optimality, Lagrange multipliers, and Hamiltonian equations, The minimum principle, solution of Zermelo's problem, Linear quadratic cost problem with finite and infinite horizon: theory and examples,

Optimal Control Theory and Dynamic Programming: Dynamic programming in discrete time, Principle of optimality and Bellman's equation, linear quadratic cost problem with finite and infinite horizon in the dynamic programming perspective: theory and examples,

Differential Games: Introduction, continuous time differential games, intro to Nash and Stackleberg equilibrium solutions concepts, solutions of Nash differential games: theory and examples

#### **Texts and Reference Books**

1. D. Liberzon, *Calculus of Variations and Optimal Control Theory: A Concise Introduction*, Princeton University Press, 2012
2. G. Meisma, *Lecture Notes on Optimal Control*, University of Twente, Enschede, The Netherlands, 2013.
3. D. E. Krik, *Optimal Control Theory: An Introduction*, Dover Publications, 2004.
4. R. F. Stengel, *Optimal Control*, Dover Publications, 1994.

**Code:** MAT-7207

**Title:** Design Methods for Control Systems

**Credit Hrs:** 03

#### **Course Outline:**

Introduction to Feedback Control Theory: Basic feedback theory, closed loop stability, stability robustness, frequency response design goals, loop shaping, limits of performance,

Classical Control System Design: Steady state error behavior, integral control, frequency response plots, classical control system design, lead, lag, and lag-lead compensation, the root locus approach to parameter selection, quantitative feedback theory,

Multivariable Control System Design: Poles and zeros of multivariable systems, MIMO structural requirements and design methods,

LQ, LQG, and  $H_2$  Control System Design: LQ theory, LQG theory,  $H_2$  optimization, feedback system design by  $H_2$  optimization, examples and applications

Uncertainty Models and Robustness: parameter robustness analysis, the basic perturbation model, the small gain theorem, stability robustness of feedback systems, structured singular value robustness analysis, combined performance and stability robustness,

$H_\infty$  – optimization and  $\mu$ -synthesis: The mixed sensitivity problem, the standard  $H_\infty$  problem, suboptimal solutions and examples, state space solutions of standard  $H_\infty$  problem, optimal solutions to the  $H_\infty$  problem, integral control and high frequency roll-off,  $\mu$ -synthesis with applications,

#### Texts and Reference Books

1. O. H. Bosgra, H. Kwakernaak, and G. Meinsma, *Lecture Notes on Design Methods for Systems and Control*, Dutch Institute of Systems and Control, 2006 .
2. B. Friedland, *Control System Design: An Introduction to State-Space Methods*, Dover Publications, 2005.
3. J. Distifano, A. R. Stubberud and L. J. Williams, *Schaum's Outline of Feedback and Control Systems*, 2<sup>nd</sup> Edition, McGraw-Hill Education, 2013.
4. R. F. Stengel, *Optimal Control*, Dover Publications, 1994.

**Course Code:** MAT-7208

**Title:** Sampling Techniques-II

**Credit Hrs:** 03

**Course Outline:** Ratio and Regression Estimators with Application in Equal and Unequal Probabilities, Best Linear Unbiased Estimator (BLUE), Model Based Versus Design Based Estimator, Condition Under which Ratio Estimator Is BLUE, Derivation of Variance and Variance Estimator Under a Model for Ratio and Regression Estimator, Multistage Sampling, Derivation of Variance and Estimator for Equal and Unequal Probability Sampling for Two-Stage Sampling, Multistage Rules-Durbin's Rule, Raj's Rule, Raj's Modified Rule, Brewer-Hanif Rule.

#### Texts and Reference Books

1. W. G. Cochran, *Sampling Techniques*, John Wiley and Sons, New York, 3<sup>rd</sup> Edition, 1977.
2. I. Kish, *Survey Sampling*, John Wiley and Sons, New York, 1965.
3. D. Raj, *Design of Survey*, McGraw-Hill Book Company Ltd, New York, 1970.
4. D. Raj, *Sampling Theory*, Mc-Graw Hill, New York, 1968.
5. P. V. Sukatme and B.V.Sukatme, *Sampling Theory of Surveys with Application*, Llowa State University Press, Ames, USA, 1970.

**Course Code:** MAT-7209

**Title:** Estimation Theory

**Credit Hrs:** 03

**Course Outline:** Properties of Estimator, Unbiaseness, Efficiency, Sufficiency and the minimal sufficient statistic, complete classes, Exponential families, Cramer-Rao lower bound and its extension, bias reduction by Jackknifing, ancilliary and Basu theorem, methods of estimation and their optimal properties, Bayes and minimax estimators, shrinkage estimation, sequential estimation. Non Linear Models, Parameters and estimation using ML method, Transformations of parameters, inference and stable transformations. Computing Methods for Non-linear Modelling, Confidence intervals for parameters and functions. Applications of non-linear modelling.

#### Texts and Reference Books

1. Levy, P. S., and Lemeshow, S., *Sampling of Populations Methods and Applications*, 3rd Ed. John Wiley, New York (1999)
2. Lindgren, B. W., *Statistical Theory*, Chapman and Hall (1998).
3. Lehman, E. L., *Theory of Point Estimation*, John Wiley and sons (1987).
4. Ross, G. J. S., *Non-linear Estimation*, Springer-Verlag, New York Inc., (1990).

**Course Code:** MAT-7210 **Title:** Differential Subordination Theory and Applications **Credit Hrs:** 03

**Course Outline:** History, Definitions and Some Results, Integral Operators, Introduction to the Theory of Second-Order Differential Subordinations, Applications of First-Order Differential Subordinations, First- Order Linear Differential Subordinations, Briot-Bouquet Differential Subordinations and its Applications in Univalent Functions, Generalized Briot-Bouquet Differential Subordinations, Analytic Integral Operators between Classes of Functions, Subordination-Preserving Integral Operators, Applications of Second-Order Differential Subordinations, Second-Order Linear Differential Subordinations, Operators Preserving Functions with Positive Real Part and Bounded Functions, Averaging Integral Operators, The Schwarzian and Starlikeness, Special Differential Subordinations, Higher Order Differential Subordinations, Introduction to Differential Subordinations of Several Complex Variables

#### **Texts and Reference Books**

1. P. L. Duren, *Univalent Functions*, Grundlehren der Math. Wissenschaften, Springer-Verlag, New York-Berlin, 1983.
2. S.S. Miller and P.T. Mocanu, *Differential Subordination Theory and Applications*, Marcel Dekker, Inc., New York, Basel, 2000.
3. E. D. Rainville, *Special Functions*, Brett Macmillan Compnay, 1960.
4. 5. C. Viola, *Special Functions*, 1<sup>st</sup> Edition, Springer, 2016.

**Course Code:** MAT-7211 **Title:** Advanced Integral Equations **Credit Hrs:** 03

**Course Outline:** Existence Theorem, Integral Equations with  $L_2$  Kernal, Applications to Partial differential equations, Integral Transforms, Wiener-Hopt Techniques.

#### **Texts and Reference Books**

1. H. H. Stadl, *Integral Equations*, John Wiley and Sons, 1973.
2. I. Stakgold, *Boundary Value Problems of Mathematical Physics*, Macmillan, New York, 1968.
3. F. G. Tricomi, *Integral Equations*, Inter science, 1957.
4. J. J. Abdul, *Introduction to Integral Equations with Applications*, Marcel Dekker Inc. New York, 1985.

**Course Code:** MAT-7212 **Title:** Non-Newtonian Fluid Mechanics **Credit Hrs:** 03

**Course Outline:** Classification of Non-Newtonian Fluids, Rheological Formulates (Time-Independent Fluids, Thyrotrophic Fluids and Viscoelastic Fluids), Variable Viscosity Fluids. Cross Viscosity Fluids, The Deformation Rate, The Rivlin-Ericksen Fluid, Basic Equation of Memories in Rheological Models. The Linear Viscoelastic Liquid, Couette Flow, Poiseuille Flows, The Current Semi-Infinite Field. Axial Oscillatory Tube Flow, Angular Oscillatory Motion, Periodic Transients, Basic Equations in Boundary Layer Theory, Orders of Magnitude, Truncated Solutions for Viscoelastic Flow, Similarity Solutions. Turbulent Boundary Layers, Stability Analysis.

#### **Texts and Reference Books**

1. G. Astarita and M. G. *Principles of Non-Newtonian Fluid mechanics* McGraw-Hill 1974.
2. R. B. Bird, R. C. Armstrong and O. Hassager, *Dynamic of Polymeric liquids*, Vol. 1 and II, John Wiley and Sons, New York, 1987.
3. W. F. Robert and A. T. McDonald, *Introduction to Fluid Mechanics*, John Wiley and Sons, 1995.
4. W. R. Schowalter, *Mechanics of Non-Newtonian Fluids*, Pergamon Press, New York, 1978.

**Course Code:** MAT-7213    **Title:** Group Methods for Differential Equations    **Credit Hrs:** 03

**Course Outline:** Basic Concept of Groups of Transformation, Parameter Lie Group of Transformation (LGT), Infinitesimal Transformation (I.T), Infinitesimal Generators, Lie's First Fundamental Theorem, Invariance, Canonical Coordinates, Elongations, Multi-Parameter Lie Group of Transformation (MLGT), Lie Algebra, Solvable Lie Algebra, Lie's Second and Third Fundamental Theorems.

Invariance of ODE's Under (LGT) and (MLGT), Mapping Solutions to Other Solutions From Invariance of an ODE and PDE, Determining Equations (I.T) of and  $N^{\text{th}}$  Order ODE and System of PDE's, Determination of  $N^{\text{th}}$  Order ODE Invariant Under a Given Group, Reduction of Order by Canonical Coordinates and Differential Invariants, Invariant Solutions of ODE's and PDE's Separatrices and Envelopes

Noether's Theorem and Lie-Backlund Symmetries, Potential Symmetries, Mapping of Differential Equations

#### **Texts and Reference Books**

1. G. W. Bluman and S. Kumei, *Symmetries and Differential Equations*, Springer-Verlag, New York, 1989.
2. J. M. Hill *Differential Equations and Group Methods*, CRC Press, Inc. New York, 1992.
3. M. A. Armstrong, *Groups and Symmetry*, 2<sup>nd</sup> Edition, Springer, 1997.
4. M. S. Gockenbach, *Partial Differential Equations: Analytical and Numerical Methods*, 2<sup>nd</sup> Edition, Society for Industrial and Applied Mathematics, 2010.

**Course Code:** MAT-7214    **Title:** Stochastic Differential Equations    **Credit Hrs:** 03

**Course Outline:** Brief Introduction to Diffusion Processes and How They Arise as Natural Approximations to Certain Discrete Processes, Review of Some Basic Facts about Brownian Motion and Martingales, ITO Stochastic Integrals Construction and Martingale Properties, ITO's Formula, Integration by Parts, Comparison with Stieltjes Integrals and Ordinary Calculus, Stochastic Differential Equations, Existence and Uniqueness of Solutions, Markov Property, Generators, Martingale Problem Characterization of Weak Solutions, Diffusion Processes, Dynkin's Formula, Calculations of Expectations and Probabilities, Converting to the Natural Scale, Stationary Distributions, Examples from Biology: Wright-Fisher Diffusions, Branching Diffusions

#### **Texts and Reference Books**

1. K.L. Chung and R. J. Williams, *Introduction to stochastic integration*, Second Ed., Probability and its Applications, Birkhauser Boston Inc., MA, 1990.
2. S. Karlin and H. Taylor, *A Second Course in Stochastic Processes*, 1<sup>st</sup> Edition, Academic Press, 1981.
3. F. C. Klebaner, *Introduction to Stochastic Calculus with Applications*, 3<sup>rd</sup> Edition, Imperial College Press, 2012.
4. D. Richard, *Stochastic calculus: A practical introduction*, 1<sup>st</sup> Edition, CRC Press, 1992.

**Course Code:** MAT-7215    **Title:** Fixed Point Theory and Applications    **Credit Hrs:** 03

**Course Outline:** Lipschitzian, Contraction, Contractive and Non-Expansive Mappings, Banach's Contraction Principal with Application to Differential and Integral Equations, Brouwer's Fixed Point Theorem with Applications, Schauder's Fixed Point Theorem with Applications, Uniformly Convex and Strictly Convex Spaces, Properties of Non-Expansive Mappings, Extension's of Banach's Contraction Principal

#### **Texts and Reference Books**

1. A. Granas and J. Dugundji, *Fixed Point Theory*, 2003 Edition, Springer, 2003.
2. R. P. Agarwal, D. O. Regan and D. R. Sahu, *Fixed Point Theory for Lipschitzian-type mappings with applications*, Springer-Verlag, USA.
3. R. P. Agarwal, *Fixed Point Theory and Applications*, Cambridge University Press, 2006.
4. V. I. Istratescu, *Fixed Point Theory: An Introduction (Mathematics and Its Applications)*, 1<sup>st</sup> Edition, Springer, 2001.

**Course Code:** MAT-7216

**Title:** Integral Inequalities

**Credit Hrs:** 03

**Course Outline:** Some Quadrature Rules and Their Applications Ostrowski Inequality in  $L_1$  And  $L_p$ -and  $L_\infty$  Spaces and Applications Gruss Inequality, Its Variant and Applications Ostrowski – Gruss Inequalities, Their Consequences and Applications Perturbed Results for Ostrowski and Ostrowski-Gruss Type Inequalities for Convex Functions, Hadmard, Sinequality, Hadmard,S Inequality for Convex Functions and Applications.

**Texts and Reference Books**

1. S. Dragomir and T. M. Rassias, *Ostrowski Type Inequalities and Applications in Numerical Integration*, 2002 Edition, Springer, 2002.
2. G. A. Anastassiou, *Advanced Inequalities*, World Scientific Publishing Company, Singapore. 2011.
3. D. D. Bainov and P.S. Simeonov, *Integral Inequalities and Applications*, 1<sup>st</sup> Edition, Springer, 1992.
4. D. S. Mitrinovic, J. Picarcic and A.M Fink, *Inequalities Involving Functions and Their Integrals and Derivatives*, 1991 Edition, Springer, 1991.

**Course Code:** MAT-7217 **Title:** Selected Topics in Applied Mathematics **Credits:** 3

**Course Outline:** Course out lines of this course will be determined by the concerned teacher as per requirement of a student in connection with his/her research.

**Course Code:** MAT-7218

**Title:** Banach Algebras

**Credit Hrs:** 03

**Course Outline:** Banach Algebra: Ideals, Homeomorphisms, Quotient Algebra, Wiener's Lemma, Gelfand's Theory of Commutative Banach Algebras: The Notions of Gelfand's Topology, Radicals Gelfand's Transforms. Basic Properties of Spectra, Gelfand-Mazur Theorem and Symbolic Calculus of A-Valued Functions, Normed Rings, Gelfand-Naimark Theorem.

**Texts and Reference Books**

1. M.A. Naimark, *Normed Algebras*, Wolters Noordhoff Publishing Groningen, Netherlands, 1972.
2. C. E. Rickart, *Banach Algebras*, D Van Nostrand Company Inc. New York , 1960.
3. W. Rudin, *Functional Analysis*, McGraw Hill, Inc, New York, 1989.
4. W. Zelazko, *Banach Algebras*, American Elsevier Publishing Company Inc, New York, 1973.

**Course Code:** MAT-7219

**Title:** Finite Mixture Distributions-II

**Credit Hrs:** 03

**Course Outline:** Components of a Mixture: Various Informal and Formal Techniques of Determining the Number of Components of a Mixture, The Structure of Modality, Assessment of Modality. Discriminate Analysis. Sequential Problems and Procedure: Introduction to Unsupervised Learning Problems, Approximate Solutions to Unknown Mixing Parameters, Unknown Component Distribution Parameters, Unknown Mixing and Component Parameters and Dynamic Linear Models.

**Texts and Reference Books:**

1. B. S. Everitt and D. J. Hand, *Finite Mixture Distribution*, Chapman and Hall London, 1981.
2. D. M. Titterington, A. F. M. Smith and U. E. Markov, *Statistical Analysis of Finite Mixture Distributions*, John Wiley and Sons, New York, 1985.
3. G. Mclachlan and D. Peel, *Finite Mixture Models*, 1<sup>st</sup> Edition, Wiley-Inter science, 2000.
4. S. F. Schnatter, *Finite Mixture and Markov Switching Models*, 2006 edition, Springer, 2006.

**Code:** MAT-7220

**Title:** Harmonic Functions Theory

**Credit Hrs:** 03

**Course Outline:** Definition and Examples, Invariance Properties, The Mean-Value Property, The Maximum Principle, The Poisson Kernel, The Dirichlet Problem, Converse of the Mean-Value Property, Real Analyticity and Homogeneous Expansions, Bounded Harmonic Functions Related Properties, Positive Harmonic Functions Related Properties, The Kelvin Transforms, Harmonic Polynomials, Harmonic Hardy Spaces, Harmonic Functions on Half-Spaces, Harmonic Bergman Spaces, The Decomposition Theorem, Annular Regions, The Dirichlet Problem and Boundary Behavior

**Texts and Reference Books**

1. S. Axler, P. Bourdon, W. Ramey, *Harmonic Function Theory*, 2<sup>nd</sup> Edition, Springer, 2001.
2. S. Bergman, *The Kernel Function and Conformal Mapping*, American Mathematical Society, 1950
3. L. L. Helms, *Introduction to Potential Theory*, Wiley-Inter science, 1969.
4. O. D. Kellogg, *Foundations of Potential Theory*, Springer, 1929.
5. John Wermer, *Potential Theory*, Lecture Notes in Mathematics, Springer, 1974

**Course Code:** MAT-7221

**Title:** Perturbation Method-II

**Credit Hrs:** 03

**Course Outline:** Approximate Solution of Linear Differential Equations, Approximate Solution of Nonlinear Differential Equations, Singular Perturbation Theory Perturbation Methods for Linear Eigen Value Problems, Asymptotic Matching Boundary Layer Theory, Mathematical Structure of Boundary Layers, Inner, Outer, And Intermediate Limits Higher-Order Boundary, Layer Theory Distinguished Limits and Boundary Layers Validity of the WKB Approximation Patched Asymptotic Approximations, WKB Solution of Inhomogeneous Linear Quations, Matched Asymptotic Approximation, Solution of the One-Turning-Point Problem.

**Texts and Reference Books**

1. A. H. Nayfeh, *Perturbation Methods*, 1<sup>st</sup> Edition, Wiley-VCH, 2000.
2. E. J. Hinch, *Perturbation Methods*, Cambridge University Press, 1991.
3. A. H. Nayfeh and D. T. Mook, *Nonlinear Oscillations*, Wiley-VCH, 1995,
4. A. H. Nayfeh, *Introduction to Perturbation Techniques*, 1<sup>st</sup> Edition, Wiley-VCH, 1993.

**Code:** MAT-7222

**Title:** Linear Matrix Inequalities

**Credit Hrs:** 03

**Course Outline:** Basic Concepts: Convex Optimization and LMIs, Dissipative Dynamical Systems: Storage functions and quadratic supply rates, Kalman-Yakubovich-Popov Lemma, The Positive Real Lemma, and Bounded Real Lemma, interconnected dissipative systems,

Stability and Nominal Performance: Review of Lyapunov stability, Generalized stability regions for LTI systems, the generalized plane concept, Quadratic, H-infinity, and H2 nominal performances,

Control Synthesis: Analysis to synthesis – a general procedure, Performance Specifications: H-infinity design, positive real design, H2 problem, State feedback problems, Discrete Time Systems,

Systems with Parametric Uncertainty: Affine parameter dependent systems, polytopic parameter dependent systems, Robust stability for autonomous systems: quadratic stability, quadratic stability of affine and polytopic models, parameter dependent Lyapunov functions,

**Texts and Reference Books**

1. C. Scherer and S. Weiland, *Linear Matrix Inequalities in Control*, Dutch Institute of Systems and Control, 2006.
2. S. Boyd, L. E. Ghaoui, E. Feron and E. Balakrishnan, *Linear Matrix Inequalities in System & Control Theory*, Society for Industrial & Applied, 1994.
3. R. Bhatia, *Matrix Analysis*, 1997 Edition, Springer, 1996.
4. F. Zhang, *Matrix Theory*, 2<sup>nd</sup> Edition, Springer, 2011.

**Course Code:** MAT-7223

**Title:** Time Series

**Credit Hrs:** 03

**Course Outline:** Methods of decomposing time-series into its component parts and measuring their effects. Stationary stochastic processes and their properties in the time domain. Frequency domain- Cyclical trend, spectral representation of a stochastic process. Properties of ARMA process and linear filters. Multivariate spectral analysis. Estimation of ARMA models. Model building and forecasting.  
Practicals based on the above topics

**Texts and Reference Books**

1. A. C. Harvey, *Time Series Models*, Philip Allan Publishers, 1981.
2. I. G. Zurbenko, *The Spectral Analysis of Time Series*, Elsevier Science Publishers B.V., Amsterdam, 1986.
3. E. J. Hannan, *Time Series Analysis*, Methuen, London, 1960.
4. M. G. Kendall, *Time-Series*, Griffin, London, 1973.

**Course Code:** MAT-7224

**Title:** General Theory of Relativity

**Credit Hrs:** 03

**Course Outline:** The Einstein Fields Equations, The Principles of General Relativity, The Stress-Energy Momentum Tensor, The Vacuum Einstein Equations and the Schwarzschild Solution, The Three Classical Tests of General Relativity, The Homogeneous Sphere and the Interior Schwarzschild Solution, Birkhoff's Theorems, The Reissner-Nordstrom Solution and the Generalized Birkhoff's Theorem, The Kerr and Kerr-Neumann Solution, Essential and Coordinate Singularities, Event Horizon and Black Holes, Eddington-Finkelstein, Kruskal-Szekres Coordinates, Penrose Diagrams for Schwarzschild, Reissner-Nordstrom Solutions

**Texts and Reference Books**

1. R. Adler, M. Bazin and M. Schiffer, *Introduction to General Relativity*, M. Graw Hill, 1965.
2. W. Rindler, *Essential Relativity*, Springer-Verlag, 1977.
3. R. M. Wald, *Introduction to General Relativity*, University of Chicago Press, Chicago, 1984.
4. P. A. M. Dirac, *General Theory of Relativity*, Princeton University Press, 1996.

**Course Code:** MAT-7225

**Title:** Electrodynamics-II

**Credit Hrs:** 03

**Course Outline:** General Regular Angular and Frequency Distributions of Radiation from Accelerated Charges, Thomson Scattering, Cherenkov Radiation, Fields and Localized Oscillating Sources, Electric Dipole Fields and Radiation, Magnetic Dipole and Electric Quadratic Fields, Multipole Fields, Expansion of the Electromagnetic Fields, Angular Distribution Sources of Multiple Radiation, Spherical Wave Expansion of a Vector Plane Wave, Scattering of Electromagnetic Wave by a Conducting Sphere

**Texts and Reference Books**

1. A. Etal *Plasma Electrodynamics*, Pergamon Press, 1975.
2. J. E. Anderson, *Magneto hydrodynamics, Shock Waves*, M. I. T. Press, Cambridge, 1963.
3. D. W. Jacson, *Classical Electromagnetic*, John-Wiley, 1962.
4. J. A. Straton, *Electromagnetic Theory*, M. Graw Hill, New York, 1963.

**Course Code:** MAT-7226

**Title:** Cosmology

**Credit Hrs:** 03

**Course Outline:** Review of Relativity, Historical Background, Astronomy, Astrophysics, Cosmology, The Cosmological Principle and its Strong Form, The Einstein and Desitter Universe Models, Measurement of Comic Distance, The Hubble Law and the Friedmann Models, Steady State Models, The Hot Big Bang Models, The Inicrowave Background, Discussion of Significance of a Start of Time, Fundamentals of High Energy Physic, The Chronology and Composition of the Universe, Non-Brayonic Dark Matter, Problems of the Standard Model of Cosmology, Bianch Space-Times, Mixmaster Models, Inflationary Cosmology, Further Development of Inflationary Models, Kaluza-Klein Cosmologies, Review of Material.



### Texts and Reference Books

1. L. F. Abbott and S. Y. Pi, *Inflationary Cosmology*, World Scientific, 1986.
2. E.W. Kolb and M. S. Turner, *The Early Universe*, Addison Wesley, 1990.
3. P. J. E. Peebles, *Principles of Physical*, Princeton University Press, 1993.
4. Ryan M. P. Jr. and Shepley, *Homogeneous Relativistic Cosmologies*, Princeton University Press, 1975.

**Course Code:** MAT-7227

**Title:** Loop Groups

**Credit Hrs:** 03

**Course Outline:** Finite Dimensional Lie Groups: Complex Groups, Compact Groups, Root System, Weyl Groups, Complex Homogeneous Spaces, Borel-Wiel Theorem.

Groups of Smooth Maps: Infinite Dimensional Manifolds Group of Maps as Infinite Dimensional Lie Groups, The Loop Groups  $L(G) = \text{Maps}(S^1, G)$  and Its Basic Properties.

Central Extension: Lie Algebra Extension, The Co-Adjoint Action of The Loop Group on Its Lie Algebra, Kriillov Method of Orbits, Groups Extension of Simply Connected Lie Groups, Circle Bundles, Connections and Curvature.

Kac-Moody Lie Algebra: The Affine Weyl Group and Root System, Generators and Relations.

### Texts and Reference Books

1. V. G. Kac, *Infinite Dimensional Lie Algebra*, Birkhauser, 1983.
2. A. Pressely and G. Segal, *Loop Groups*, Oxford University Press, 1986.
3. L. McMurtry, *Loop Groups*, Simon & Schuster, 2004.
4. M. Benbow, *Loops and Other GRoups : A Kinesthetic Writing System: Level 2 Booklet*, Therapy Skill Builders, 1990.

**Course Code:** MAT-7228

**Title:** Magnetohydrodynamics-II

**Credit Hrs:** 03

**Course Outline:** Flow of Conducting Fluid Past Magnetized Bodies: Flow of an Ideal Fluid Past Magnetizes Bodies, Fluid of Finite Electrical Conductivity Flow Past a Magnetized Body. Dynamo Theories: Elsasser's Theory, Bullard's Theory, Earth's Field Turbulent Motion and Dissipation, Vertically Analogy. Lionized Gasses: Effects of Molecular Structure, Currents in Fully Ionized Gas, Partially Ionized Gases, Interstellar Fields, Dissipation in Hot and Cool Clouds.

### Texts and Reference Books

1. Akhiezer, *Electrodynamics*, Pergamon Press, 1975.
2. J. E. Anderson, *Magneto hydrodynamics, Shock Waves*, M. I. T. Press, Cambridge, 1963.
3. T. G. Cowling, *Magneto hydrodynamics*, Inter science Publishers, 1963.
4. A.G. Kulikowsky and A. G. Lyabimov, *Magnetohydrodynamics*, Adison Wesley, 1965.

**Course Code:** MAT-7228

**Title:** C\*-Algebra

**Credit Hrs:** 03

**Course Outline:** Involutive Algebras, Normed Involutive Algebra C\*-Algebra, Gelfand-Naimark Theorem, Positive Functional, A Characterization of C\*-Algebras, Positive Forms and Representations, Application of C\* -Algebras to Differential Operations

### Texts and Reference Books

1. J. Dixmier, *C\*-Algebras*, North Holland Publishing Company, 1977.
2. M. A. Naimark, *Normed Algebras*, Wolters Noor dhoff Publishing Groningen, Netherlands, 1972.
3. E. Rudin, *Functional Analysis*, M. Graw Hill, New York, 1989.
4. G. J. Murphy, *C\*-Algebras and Operator Theory*, 1<sup>st</sup> Edition, Academic Press, 1990.

**Course Code:** MAT-7230

**Title:** Topological Algebras

**Credit Hrs:** 03

**Course Outline:** Definition of a Topological Algebra and Its Examples, Adjunction of Unity, Locally Convex Algebras, Idempotent and M-Convex Sets, Locally Multiplicatively Convex (L.M.C.) Algebras, Spectrum, Gelfandmazar Theorem, Maximal Ideals, Quotient Algebras, Multiplicative Linear Functional and Their Continuity, Gelfand Transformations, Radial of an Algebra, Semi-Simple Algebras, Involution Algebras, Gelfand-Naimark Theorem, L.M.C. Algebras

**Texts and Reference Books**

1. E. Beckenstein, L. Narici and C. Suffel, *Topological Algebras*, North-Holland Company, 1977.
2. T. Hussain, *Multiplicative Functions on Topological Algebras*, Pitman Advanced Publishing Program, 1983.
3. A. Mallios, *Topological Algebras, Selected Topics* North-Holland Company, 1986.
4. E. Michael, *Locally Multiplicatively-convex Topological Algebras*, M. Amer. Math. Soc. No. 11, 1951.
5. W. Zelazko, *Metric Generalization of Banach Algebras*, Rozprawy Matematyczne, 1956.

**Course Code:** MAT-7231

**Title:** Optimal State Estimation

**Credit Hrs:** 03

**Course Outline:** Least squares estimation, Wiener filtering, propagation of states and covariances for discrete and continuous time systems, the discrete and continuous time Kalman filters, the H-infinity filters, the extended and unscented Kalman filters.

**Texts and Reference Books**

1. D. Simon, *Optimal State Estimation*, John Wiley & Sons, Inc, 2006.
2. J. L. Crassidis and J. L. Junkins, *Optimal Estimation of Dynamic Systems*, 2<sup>nd</sup> Edition, Chapman and Hall, 2011.
3. B. M. Mohan and S. K. Kar, *Continuous Time Dynamical Systems: State Estimation and Optimal Control with Orthogonal Functions*, CRC Press, 2012.
4. R. F. Stengel, *Optimal State Estimation*, Dover Publications, 1994.

#### 4. Scheme of Studies for PhD in Mathematics: General Breakup

##### 4.1 General Requirement for Ph.D. Program

|   |                                  |
|---|----------------------------------|
| Entrance  | As par HEC and University Policy |
| Duration  | 6 (min)-16 (max) semesters       |
| Courses   | 18 credits                       |
| Thesis (MAT-8000)   | 50 credits                       |
| Conference/Seminar I (MAT-7999)                                 | 01 credit                        |
| Conference/Seminar II (MAT-7999)                                | 01 credit                        |
| Comprehensive Examination (Written & Oral) (MAT-7998) P/F basis |                                  |
| Total   | 70 credits                       |

##### List of Courses for Ph.D Program

| Code     | Course Title  | Credit Hours |
|----------|---|--------------|
| MAT-7101 | Advanced Functional Analysis                        | 03           |
| MAT-7102 | Advanced Topology                                   | 03           |
| MAT-7103 | Advanced Optimization Theory                        | 03           |
| MAT-7104 | Variational Inequalities                            | 03           |
| MAT-7105 | Advanced Partial Differential Equations             | 03           |
| MAT-7106 | Nonlinear Systems and Control                       | 03           |
| MAT-7107 | Advanced Complex Analysis                           | 03           |
| MAT-7108 | Sampling Techniques-I                               | 03           |
| MAT-7109 | Multivariate Analysis                               | 03           |
| MAT-7110 | Advanced Mathematical Statistics                    | 03           |
| MAT-7111 | Advanced Probability Theory                         | 03           |
| MAT-7112 | Introduction to Finite Element Methods              | 03           |
| MAT-7113 | Mathematical Techniques for Boundary Value Problems | 03           |
| MAT-7114 | Convex Analysis                                     | 03           |
| MAT-7115 | Semigroups in Geometric Functions Theory            | 03           |
| MAT-7116 | Conformal Mappings                                  | 03           |
| MAT-7117 | Stochastic Processes                                | 03           |
| MAT-7118 | Basics of the Theory of Fluids                      | 03           |
| MAT-7119 | Finite Mixture Distributions-I                      | 03           |
| MAT-7120 | Approximation Theory                                | 03           |
| MAT-7121 | Perturbation Methods-I                              | 03           |
| MAT-7122 | Lie Algebra   | 03           |
| MAT-7123 | Topological Groups                                  | 03           |
| MAT-7124 | Topological Vector Spaces                           | 03           |
| MAT-7125 | Electrodynamics-I                                   | 03           |
| MAT-7126 | Theory of Group Graphs                              | 03           |
| MAT-7127 | Theory of Group Actions                             | 03           |
| MAT-7128 | Magnetohydrodynamics-I                              | 03           |
| MAT-7129 | Advanced Measure Theory                             | 03           |
| MAT-7130 | Theory of Complex Manifolds                         | 03           |
| MAT-7131 | Complex Analysis of Several Variables               | 03           |
| MAT-7132 | Advanced Analytical Dynamics                        | 03           |
| MAT-7133 | General Relativity                                  | 03           |
| MAT-7134 | Astrophysics  | 03           |

|          |  |    |    |
|----------|--|----|----|
| MAT-7135 | The Classical Theory of Fields                     | 03 |    |
| MAT-7136 | Graph Theory                                       | 03 |    |
| MAT-7137 | Introduction to Robotics                           | 03 |    |
| MAT-7138 | Advanced Abstract Algebra                          | 03 |    |
| MAT-7201 | Geometric Functions Theory                         | 03 |    |
| MAT-7202 | Selected Topics in Pure Mathematics                | 03 |    |
| MAT-7203 | Advanced Mathematical Modeling                     | 03 |    |
| MAT-7204 | Parameter Estimation and Sensitivity Analysis      | 03 |    |
| MAT-7205 | Numerical Solutions of PDEs                        | 03 |    |
| MAT-7206 | Optimal Control                                    | 03 |    |
| MAT-7207 | Design Methods for Control Systems                 | 03 |    |
| MAT-7208 | Sampling Techniques II                             | 03 |    |
| MAT-7209 | Estimation Theory                                  |    | 03 |
| MAT-7210 | Differential Subordination Theory and Applications | 03 |    |
| MAT-7211 | Advanced Integral Equations                        |    | 03 |
| MAT-7212 | Non-Newtonian Fluid Mechanics                      | 03 |    |
| MAT-7213 | Group Methods for Differential Equations           | 03 |    |
| MAT-7214 | Stochastic Differential Equations                  | 03 |    |
| MAT-7215 | Fixed Point Theory and Applications                | 03 |    |
| MAT-7216 | Integral Inequalities                              |    | 03 |
| MAT-7217 | Selected Topics in Applied Mathematics             | 03 |    |
| MAT-7218 | Banach Algebras                                    | 03 |    |
| MAT-7219 | Finite Mixture Distributions-II                    | 03 |    |
| MAT-7220 | Harmonic Functions Theory                          | 03 |    |
| MAT-7221 | Perturbation Methods-II                            | 03 |    |
| MAT-7222 | Linear Matrix Inequalities                         | 03 |    |
| MAT-7223 | Time Series  | 03 |    |
| MAT-7224 | General Theory of Relativity                       | 03 |    |
| MAT-7225 | Electrodynamics-II                                 |    | 03 |
| MAT-7226 | Cosmology  |    | 03 |
| MAT-7227 | Loop Groups  |    | 03 |
| MAT-7228 | Magnetohydrodynamics II                            | 03 |    |
| MAT-7229 | C* -Algebras                                       |    | 03 |
| MAT-7230 | Topological Algebras                               |    | 03 |
| MAT-7231 | Optimal State Estimation                           | 03 |    |

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### 4.3 External Examiners for PhD Thesis Evaluation

#### (a) International

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## 5. Scheme of Studies for BSc (Two Years Program) for affiliated colleges

There are three different courses of studies in Mathematics and each course has status of the subject

- i) A-course of Mathematics (200 Marks)
- ii) B-course of Mathematics (200 Marks)
- iii) General Mathematics (200 Marks)

The following division is recommended:

### 5.1 A-Course of Mathematics

- i) Differential and Integral Calculus (50 Marks)
- ii) Complex Number and Analytic Geometry (50 Marks)
- iii) Infinite Series, Differential Equation and Laplace Transform (50 Marks)
- iv) Linear Programming and Application of Calculus (50 Marks)

### 5.2 B-Course of Mathematics

- i) Group Theory and Linear Algebra (50 Marks)
- ii) Number Theory, Topology and inner product space (50 Marks)
- iii) Vector Analysis and Statics (50 Marks)
- iv) Numerical Method and Dynamics (50 Marks)

### 5.3 General Mathematics

- i) Complex Number and linear Algebra and Analytic Geometry (50 Marks)
- ii) Differential and integral calculus (50 Marks)
- iii) Application of calculus and Analytical Geometry of Three Dimension (50 Marks)
- iv) Numerical Method, Infinite Series, Linear Programming and Differential Equation (50 Marks)

### 5.4 Course Contents of A-Course of Mathematics

#### 5.4.1 Paper-I : DIFFERENTIAL AND INTEGRAL CALCULUS (3<sup>rd</sup> Year)

Students have to attempt five **question** out of eight: three from Section-I and two question from Section-II

##### Section-I Differential Calculus (5 out of 8)

A review of real number system, upper and lower bounds, Function and their Graphs, limits, continuity and related theorems, Tangents and the Derivative at a point, Differential rules and their Application, Derivative as a rate of change, Derivatives of trigonometry, exponential, logarithmic hyperbolic function and differentiation of their inverse, Implicit differentiation, Related rates, Linearization and differentials, Higher derivatives, Leibnitz's theorem, Rolle's theorem, Lagrange mean value theorem, increasing and decreasing function, Cauchy's mean-value theorem, indeterminate forms and L'Hospital's rule.

##### Section-II Integral calculus (3 out of 8)

Area and estimating with finite sums, sigma notations and limit of finite sums, definite integral as the limit of a sum, properties of definite integral, fundamental theorem of calculus, indefinite integrals and techniques of integration, reduction formulae, application of definite integral to area, arc length and other problems

#### Recommended Books

- i) G.B.Thomas Jr.M.D.Weir and J.R.Hass, Thomas Calculus, 12<sup>th</sup> edition, Pearson Edu.Inc., 2010.
- ii) H.Anton, Calculus. (Latest edition). John Wiley and sons, New York.
- iii) S.M.Yousaf, Calculus
- iv) Zia-ul-Haq, Calculus and analytical Geometry, Carvan Book, 2001.
- v) C.H.Edwards and D.E.Penny, Calculus and analytical Geometry, (Latest Edition). Prentice Hall, Inc.

#### 5.4.2 Paper-II Complex Number and Analytical Geometry (3<sup>rd</sup> year)

Student have to attempt five question out of eight: two from section-I and three question from section-II

##### Section-I: Complex Numbers (3 out of 8)



Complex Numbers and algebra of complex number, polar representation, Euler's Formula, De-Moivre's theorem and its applications, Trigonometric and Hyperbolic function, Exponential and logarithmic function, Separation of complex valued functions and imaginary parts, Summation of series.

#### **Section-II: Analytical Geometry (5 out of 8)**

##### **Two-dimensional Analytical Geometry (2 out of 8)**

Translation and rotation of axes, General equation of the second degree and the classification of conic sections, Conic sections in polar coordinates, Tangents and normals, Pedal equation of curves, Tracing of polar curves.

##### **Three-dimensional Analytical Geometry (3 out of 8)**

Direction cosines and ratios, angle between two lines, Standard forms of equations of lines and planes, Distances between points, Lines and planes, Spherical polar and cylindrical coordinate systems, Standard form of the equation of sphere, Cylinder, Cone, ellipsoid, paraboloid and hyperboloid, symmetry, intercepts and sections of a surface, tangent planes and normals.

##### **Recommended Books:**

- i) G.B. Thomas Jr. M.D. Weir and J.R. Hass, Thomas Calculus, 12<sup>th</sup> Edition, Pearson Edu. Inc. 2010.
- ii) H. Anton, Calculus. (Latest edition) . John Wiley and Sons, New York.
- iii) S. M. Yousaf, Muhammad Amin, Calculus with Analytical Geometry.
- iv) Zia-ul-Haq, Calculus and analytical Geometry, Carvan Book, 2001.
- v) C.H. Edwards and D.E. Penny, calculus and analytical Geometry, (Latest edition).  
Prentice Hall, Inc.
- vi) E.H. Swokowski, Calculus with Analytical Geometry, (Latest Editor). PWS publishers, Boston, Massachusetts.

#### **5.4.3 PAPER.III: INFINITE SERIES, DIFFERENTIAL EQUATIONS AND LAPLACE TRANSFORMS (4<sup>th</sup> Year)**

Students have to attempt five questions out of eight: two from section-I and three questions from section-II

##### **Section –I: Infinite series (3 out of 8)**

Sequence of numbers and their convergence, Algebra of convergent sequences, Infinite series and their convergences, Convergence tests for infinite series: Comparison, quotient, ratio, root and integral tests, Absolute and conditional convergences, Interval and radius of convergences, Taylor's and Maclaurin's theorems in finite and infinite form and their use in expansion of function.

##### **Section-II: Differential Equations (5 out of 8)**

Definition and types of differential equations and their formations, Different methods of solving first order ordinary differential equations, The Bernoulli, Riccati and Clairaut equations, Families of curves, Orthogonal trajectories, Initial and boundary value problem, Application of first order differential equations in problems of decay and growth of populations of dynamics and logistics, second and higher order linear differential equations with constant coefficients and methods of their solutions, Cauchy-Euler equations, system of second order linear differential Equations, Method of undetermined coefficient, Method of variation of parameters, Reduction of order, Laplace transforms and applications.

##### **Recommended Books**

1. G.B. Thomas Jr. M.D. Weir and J.R. Hass, Thomas Calculus, 12<sup>th</sup> Edition, Pearson Edu. Inc., 2010.
2. D.G. Zill and M.R. Cullen, Differential Equations with boundary – Value problems, 3<sup>rd</sup> Edition, PWS publishing Company, 1997.
3. H. Anton, Calculus. (Latest Edition). John Wiley and Sons, New York.
4. S.M. Yousaf, Mathematical Methods
6. Zia ul Haq, Calculus and Analytical Geometry, The Carvan Book House, 2001.
8. E.H. Swokowski, Calculus with Analytical Geometry (Latest Edition). PWS publishers, Boston, Massachusetts

#### **5.4.4 PAPER-IV: LINEAR PROGRAMMING AND APPLICATIONS OF CALCULUS (4<sup>th</sup> Year)**

Students have to attempt five questions out of eight : three from section-I and two from section-II.

##### **Section-I: (5 out of 8)**

##### **(a) Applications of Differential Calculus 4/5**

Curves and their Cartesian ,polar and parametric representations, Asymptotes ,Maxima and Minima, points of inflexion and their applications, singular points, curve tracing, Curvature ,centre and radius of curvature, Functions of several variables, limits continuity and partial derivatives, Maxima and minima of functions of two variables with applications ,Approximations ,Equations of tangent plane and normal line to a surface.

#### **(b) Linear programming 1/5**

Introduction to Operations Research in general and in particular to linear programming simplex method ,Assignment Models

#### **Section-II: Applications of Integral Calculus (3/8)**

Rectifications and Quadrature, Simple cases of double and triple integrals, Volumes and area of surfaces of revolutions.

#### **Books Recommended**

- G.B Thomas Jr. M.D weir and J.R. Hass, Thomas Calculus, 12<sup>th</sup> Edition, pearson Edu. Inc., 2010.
2. A.Sultan, Linear programming, Academic press.
3. W.A Spivey Linear programming ,McMillan Co.
4. Hamday A. Taha, Operations Research
5. Hiller, Introduction to Operations Research
- 6.Dar,K.H. Mathematical Techniques, Carvan Book House,2001.

### **5.5 B-COURSE OF MATHEMATICS**

#### **5.5.1 PAPER-I: GROUP THEORY AND LINEAR ALGEBRA (3<sup>rd</sup> Year)**

Students have to attempt five questions out of eight :three from section-I and two from section-II.

#### **Section-I Group Theory (3 out of 8)**

Definitions and examples of groups, Groups of residue classes, Cyclic group, Order of a group and order of an element of a group ,subgroup, cosets, Lagrange's theorem and its applications  
Permutations ,even and odd permutations ,Cycles and length, transpositions

#### **Section-II: Linear Algebra (5 out of 8)**

Fields, Vector spaces,subspaces and examples ,Linear dependence and independence,Bases and dimensions ,Linear transformation,Motivations of ,matrices through a system of linear homogenous and non -homogenous equations , Elementary row and column operations on matrices ,Algebra of matrices Determinants of matrices ,their properties and evaluation of various kinds of matrices ,Matrix of a linear transformation , Rank of a matrix , Evaluation of ranks and inverses of matrices ,solution of system of homogenous and non- homogenous linear equations (Elimination and Gauss Method)

#### **Books Recommended**

- i) H.Anton, Elementary Linear Algebra ,(Latest Edition).J. Wiley
- ii) S.M. Yosaf, Mathematical Methods
- iii) A.Majeed .Group Theory.
- iv) K.L. Mir, Linear Algebra, ilmi kutab khana.
- v) C.H Edwards, Jr. and D.E. Penney, Elementary Linear Algebra,(Latest Edition ).prentice Hall, International edition
- vi) S.J.Axler, Linear Algebra, Done Right, Springer-Verlag,1996

#### **5.5.2 Paper-II: NUMBER THEORY, TOPOLOGY AND INNER PRODUCT SPACE(3<sup>rd</sup> Year)**

Student have to attempt five question out of eight: two from section-I and three question from section-II

#### **Section-I: Number Theory (3 out of 8)**

Divisibility Euclid's theorem (Division Algorithm) ,Greatest common divisor and latest common multiple, theory of primes, Linear Equations, Diophantine Equation.

#### **Section-II: Topology & Inner Product Space (5 out of 8)**

Definition and examples of metric space, open balls, open sets in a metric space, interior, exterior, boundary and closure of a set in a metric space, definition and example of topology and topological spaces, open and closed sets in topological spaces, Neighborhood, Limit Point, Interior, exterior, boundary and closure of sets in a topological spaces,

Definition and example of inner product spaces, Orthogonality, orthogonal and orthogonal system, orthogonal matrices.

**Books Recommended**

- i) A. Majeed, Element of topology and functional Analysis, Ilmi kitab Khana, Lahore 1997.
- ii) S. M. Fahfa, Introduction to point set topology.
- iii) B. Ahmad, General Topology, 1998.
- iv) S. Manzur Hussain, Introduction to theory of Number . G. A Jones and J.M. Jones,
- v) Elementary Number Theory, Springer-Varlog, London Limited, 1998.
- vi) M. B. Nathanson, Methods in Number Theory, Springer-Verlog, New York, 2000.
- vii) Introductory set topology by S. M. Yhaya.

**5.5.3 PAPER-III: VECTOR ANALYSIS AND STATICS (4<sup>th</sup> YEAR)**

Students have to attempt five questions out of eight: two from section-I and three from section-II

**Section-I: Vector Analysis (3 out of 8)**

Vectors and their algebra, coordinate systems and bases, Scalar and vector triple products, Differentiation and integration of vectors, Scalar and vector point functions, Concepts of gradient, divergence and curl along with their applications.

**Section-II: Statics (5 out of 8)**

Composition and resolution of forces, Particles in equilibrium, Parallel forces, moments, Couples, General conditions of equilibrium of coplanar forces, Principle of virtual work, Friction, Centre of gravity.

**Books Recommended**

1. G.B. Thomas Jr. M.D. Weir and J.R. Hass, Thomas Calculus, 12<sup>th</sup> Edition, Pearson Edu. Inc., 2010
2. Q. K. Ghor, Introduction to Mechanics (West Pakistan Co., Ltd., Lahore)
3. G.D. Smith, Vector Analysis, (Latest Edition), Oxford University Press.
4. K.L. Mir, Vector Analysis, (Latest Edition), Ilmi Kitab Khana.
5. M.N. Talpur, Calculus with Analytical Geometry.
6. L. Synge and B.A. Griffith, (Latest Edition), Principles of Mechanics. Mc-Graw Hill.
7. R. Whitworth and Dyke, Guide to Mechanics, (Latest Edition), MacMillan

**5.5.4 PAPER-IV NUMERICAL METHODS AND DYNAMICS (4<sup>th</sup> Year)**

Students have to attempt five questions out of eight : three from section-I and two questions from section-II.

**Section-I: Numerical Methods (3 out of 8)**

Introduction to Numerical Analysis, Numerical solution of algebraic and transcendental equations: graphical method, bisection method, iteration method, Newton-Raphson method, secant method and method of false position, System of Linear equations: Gauss-Seidel and Jacobi methods, Numerical integration: Trapezoidal and Simpson's rules. (If possible computer programming may be used for problem solving).

**Section-II: Dynamics of a Particle (5 out of 8)**

Motion in a straight line, Uniformly accelerated and resisted motion. Velocity, acceleration and their components in cartesian and polar coordinates, tangential and normal components, Conservative forces, Projectiles, Central forces and orbits, Simple harmonic motion, Damped and forced vibrations.

**Books Recommended**

1. Robert-W. Hornbeck, Numerical Methods, Quantum Publishers.
2. Alistair Wood, Introduction to Numerical Analysis, Addison Wesley.
3. M. Iqbal, Numerical Analysis, National Book Foundation.
4. S.A. Bhatti, N.A. Bhatti, Numerical Methods
5. Q. L. Ghor, Introduction to Mechanics (West Pakistan Publishing Co., Ltd., Lahore).

## 5.6 GENERAL MATHEMATICS

### 5.6.1 PAPER-I: COMPLEX NUMBER, LINEAR ALGEBRA AND ANALYTICAL GEOMETRY (3<sup>rd</sup> Year)

Students have to attempt five questions out of eight: two from section-I and three questions from section-II.

#### Section-I: Complex Number System (3 out of 8)

Real number system and properties of real numbers, Real-valued functions and their graphs, Complex numbers their algebra and Polar form, De-Moivres' theorem,  $n^{\text{th}}$  roots of complex numbers, Complex functions, Sum of trigonometric series.

#### Section-II: Linear Algebra and Analytical Geometry (5 out of 8)

Matrices: rank and inverse of a matrix. Linear transformation and their matrices, Determinants, System of linear equations, Analytic Geometry of two Dimension, Translation and rotation of axis, Properties of tangents and normal, Polar equation of conics Pedal equation, Tracing of polar curves.

### 5.6.2 PAPER-II: DIFFERENTIAL AND INTEGRAL CALCULAS (3<sup>rd</sup> Year)

Students have to attempt five questions out of eight: three from section-I and two questions from section-II

#### Section-I: Differential Calculus (5 out of 8)

Techniques of finding limits, Continuity of a function, Differentiability, Indeterminate forms, Use of Rolle's theorem, Mean value theorems (Lagrange and Cauchy), Taylor and Maclaurins series, Derivatives, Higher Derivatives and Partial Derivatives, Related rates.

#### Section-II: Integral Calculus (3 out of 8)

Techniques of integration, Definite integral as limit of a sum, Evaluation of a definite integral by definition, Improper integrals, reduction formulae.

### 5.6.3 PAPER-III: APPLICATION OF CALCULUS AND ANALYTICAL GEOMETRY OF THREE DIMENSIONS (4<sup>th</sup> Year)

Students have to attempt five questions out of eight: two from section-I and three questions from section-II.

#### Section-I: Application of differential and Integral Calculus (5 out of 8)

Asymptotes, maxima and minima of a function of one and two variables, Curvatures and centre of curvature, rectification, quadrate, Eulers theorem, Chain Rule, Total derivative, Equation of tangent, Plane and normal lines to surfaces volumes and surface area of revolution, Simple cases of double and triple integrals.

#### Section-II:: Analysis Geometry (3 out of 8)

Direction cosines and ratios, Angle between two lines, Standard form of equations of planes and lines, Intersection of planes and lines, Distance between points, lines and planes, Spherical, polar and cylindrical coordinate systems, Standard form of the equations of a sphere, cylinder, cone, ellipsoid, paraboloid and hyperboloid, Symmetry and intercepts of a surface, Tangent planes and normal.

### 5.6.4 PAPER-IV: NUMERICAL METHODS, INFINITE SERIES, LINEAR PROGRAMMING AND DIFFERENTIAL EQUATIONS (4<sup>th</sup> Year)

Students have to attempt five questions out of eight: two from section-I and three questions from section-II.

#### Section-I: Numerical Methods and Infinite Series (3 out of 8)

Introduction to infinite series and tests for their convergence, Absolute and conditional convergence. Introduction to Numerical Analysis, Numerical Solution of algebraic and transcendental equations: bisection method, Newton-Raphson method.

#### Section-II: Linear Programming and Differential Equations (5 out of 8)

Introduction to linear programming, Simplex methods and their examples from real life, Differential equations of first order, Separable, Homogenous equation, Exact equation, Linear differential equation, Bernoulli's equation, orthogonal trajectories, Differential equations 2<sup>nd</sup> and higher order Cauchy Euler equation, Method of variation of parameters, Method of undetermined Coefficient.

#### Books Recommended for General Mathematics (Papers I to IV)

1. G.B. Thomas Jr. M.D. Weir and J.R. Hass, Thomas Calculus, 12<sup>th</sup> Edition, Pearson. Edu. Inc., 2010.
2. S.T. Tan, Applied Mathematics. For the Managerial, life, and social sciences.

3. H. Anton, Elementary Linear Algebra. (7<sup>th</sup> edition, 1997). Wiley.
4. H. Anton, Calculus, (Latest Edition) John Wiley and Sons, New York.
5. E. Kreysing, Advanced Engineering Mathematics, (Latest Edition), J. Wiley.
6. M. Iqbal Numerical Analysis. (Latest Edition), National Book Foundation.
7. Fiaz Ahmad and M.A. Rana, Elements of Numerical Analysis, (Latest Edition), NBF.
8. S.M. Yousaf, Mathematical Methods.
9. Hmaday A. Taha, Operations Research.
10. A. Sultan, Linear Programming, Academic Press.

#### **Other Books**

1. Calculus S.M. Yousaf
2. Introduction to Mechanics, S.M. Yousaf
3. Topology Ch. M. Amin
4. Introduction to Set Topology S.M. Yousaf.
5. Metric Spaces by Z.R Bhatti
6. Elementary Theory of Numbers by Sayyed Manzoor Hussain
7. Elementary Numerical Analysis by Dr. M. Iqbal
8. Vector Analysis by Dr. Munawwar Hussain.

**Any Other Item**